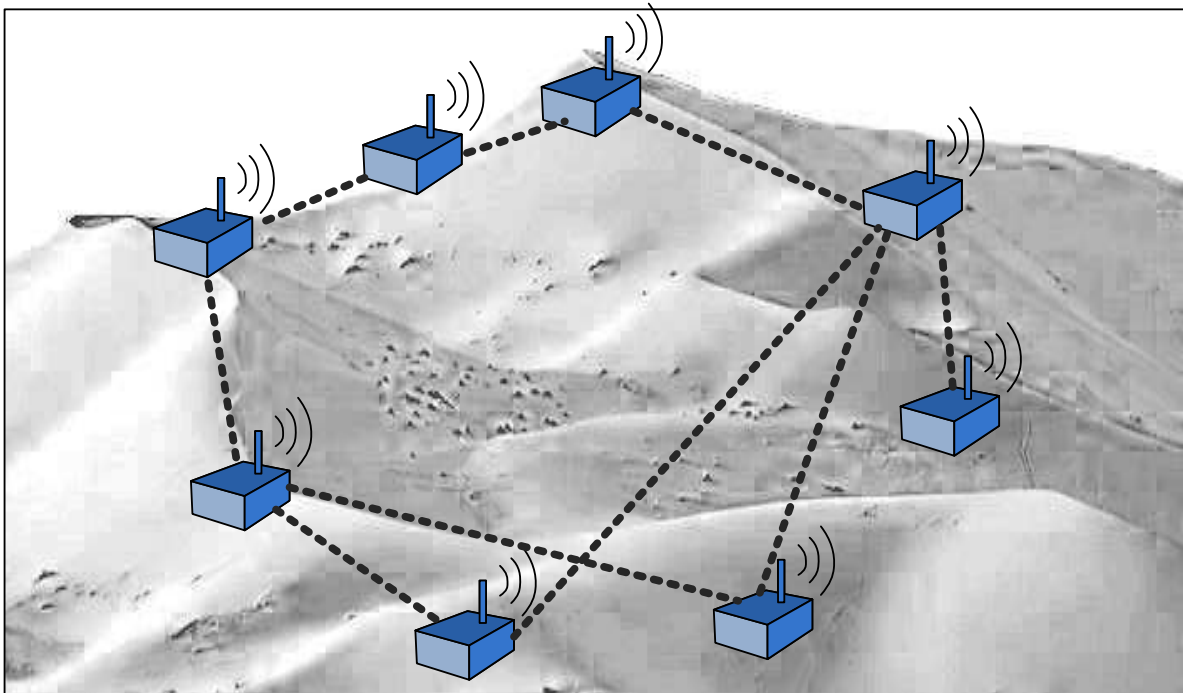


**Jan Lunze**

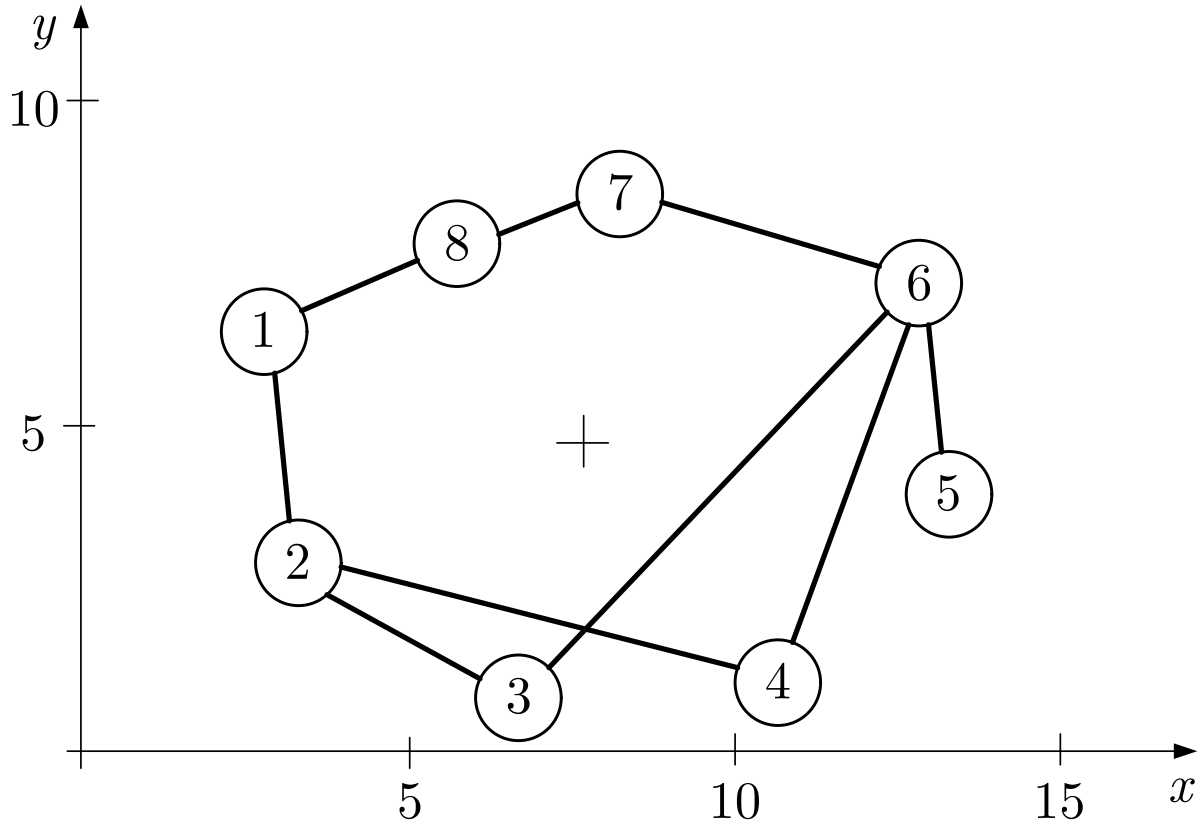
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**Figures**



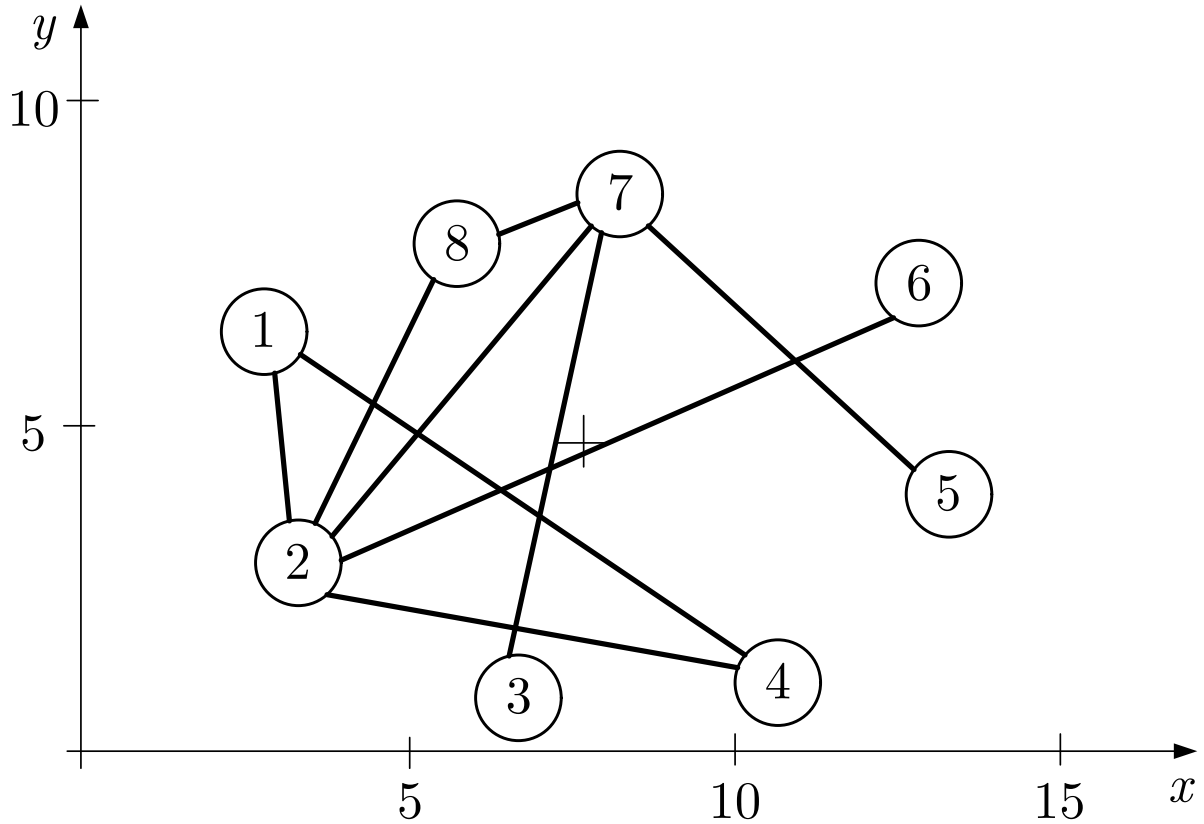
**Fig. 0: Sensor network**

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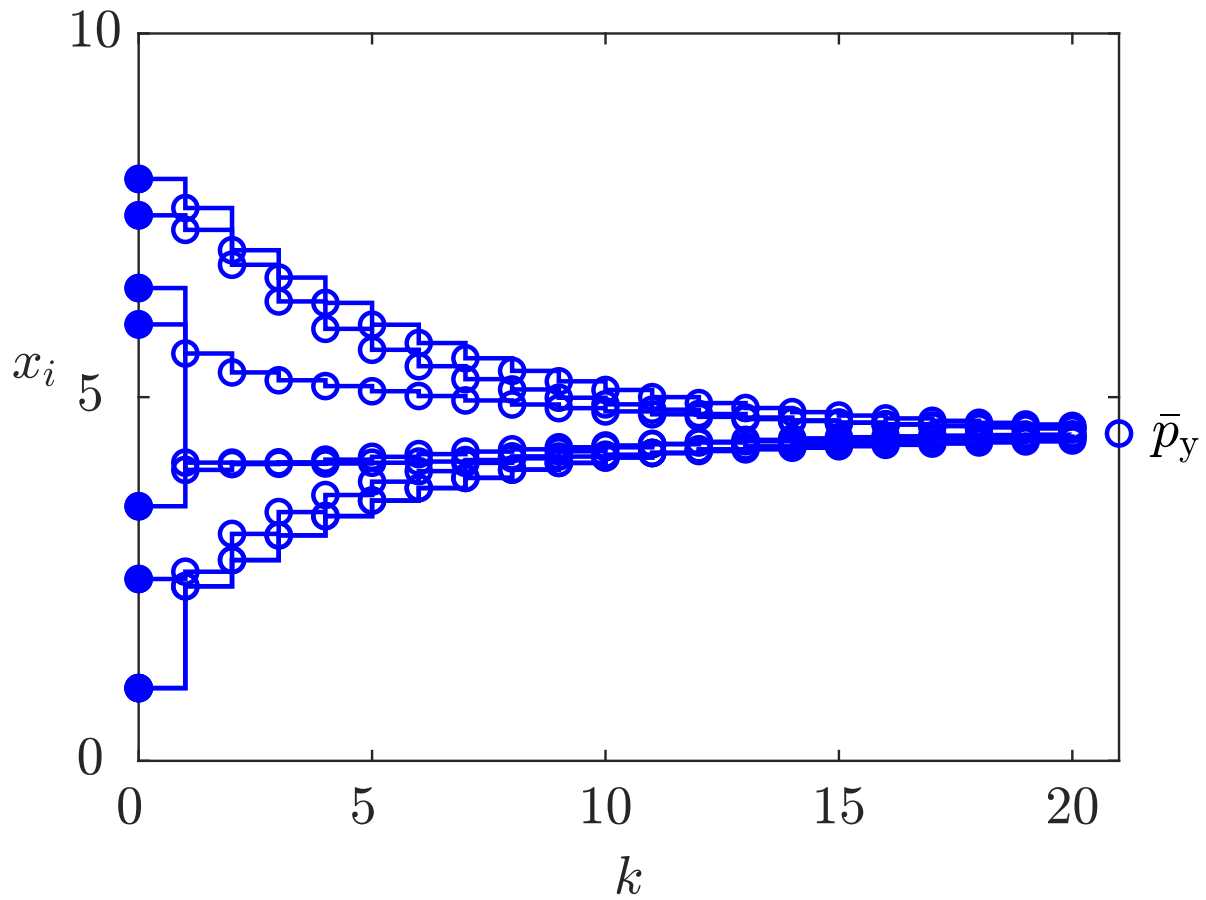
**Fig. 1: Two communication graphs of sensor networks drawn in the  $x/y$ -coordinate system with the centroid marked by “+” (I)**

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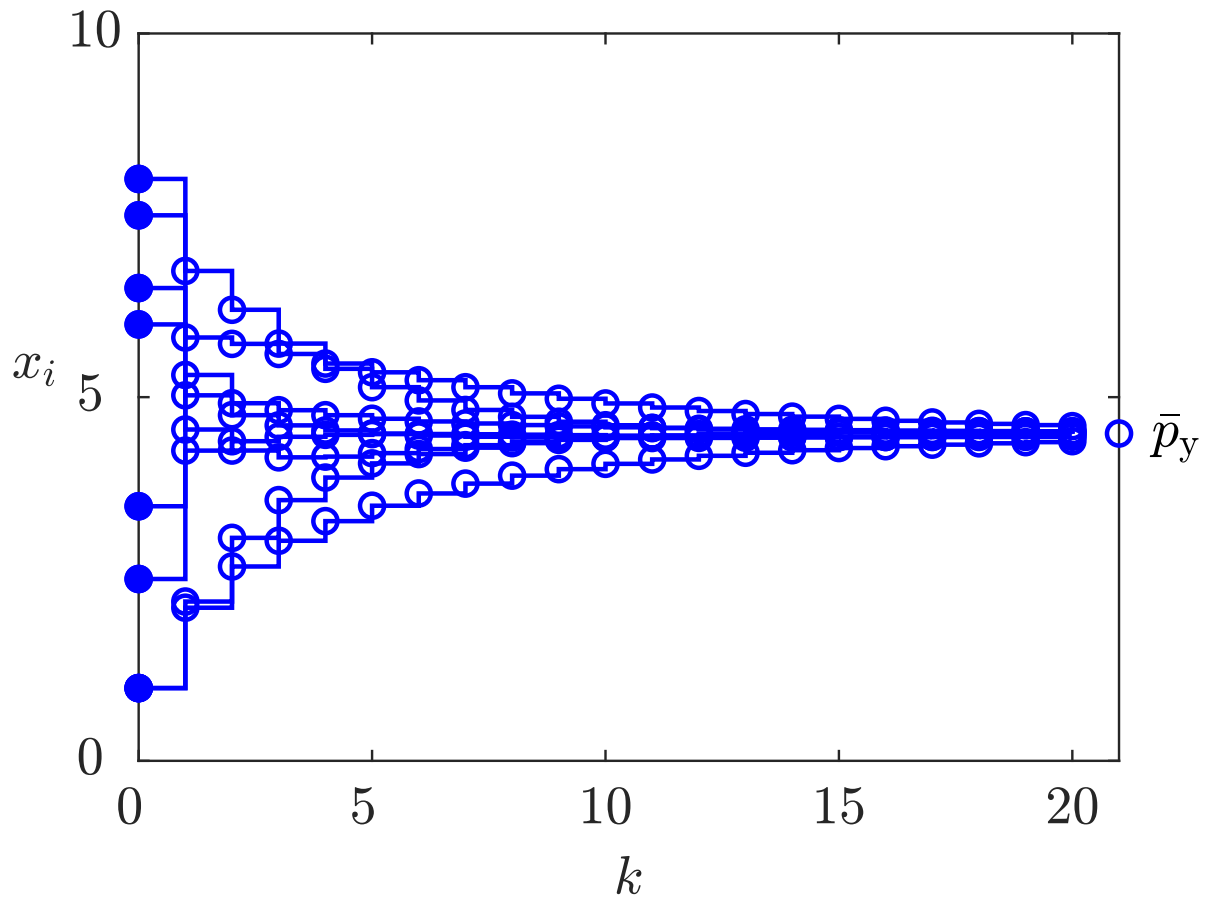
**Fig. 1: Two communication graphs of sensor networks drawn in the  $x/y$ -coordinate system with the centroid marked by “+” (II)**

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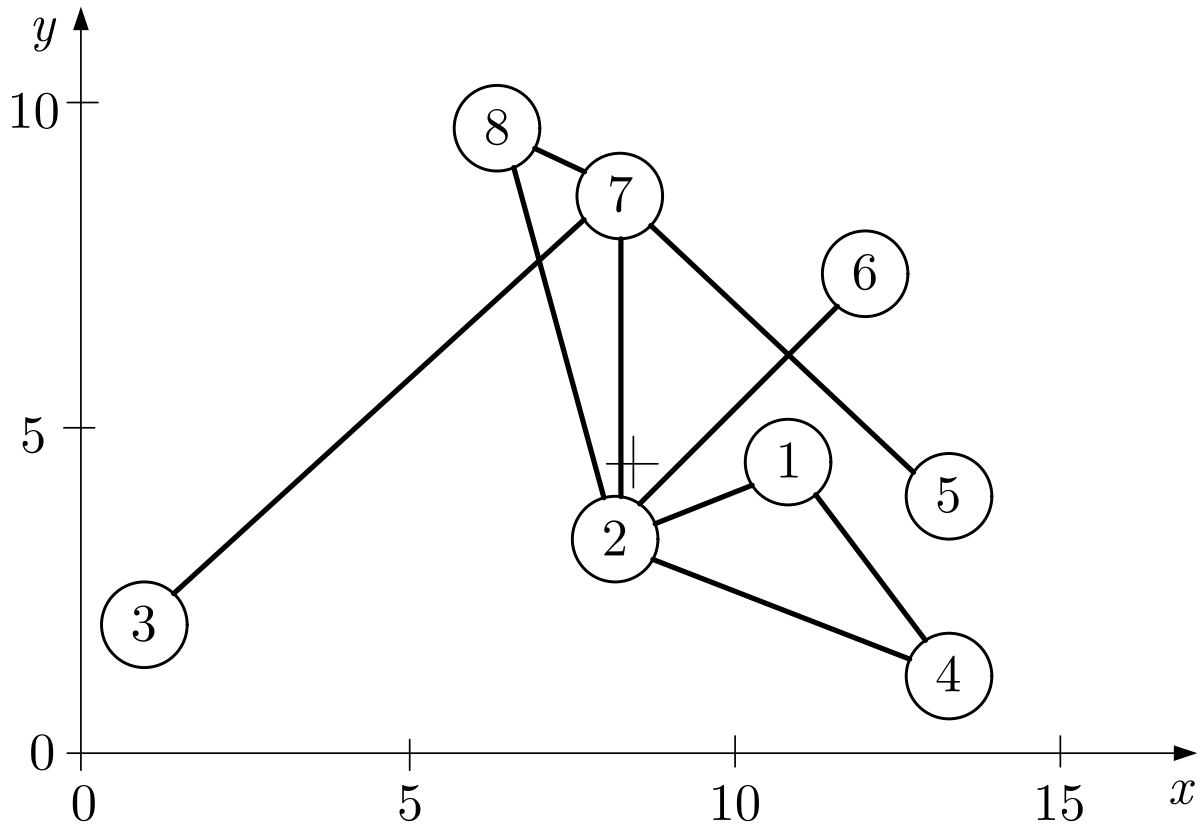
**Fig. 2: Convergence of the sensor states towards the consensus value  $\bar{p}_y$  for the two communication graphs of Fig. 1 (I)**

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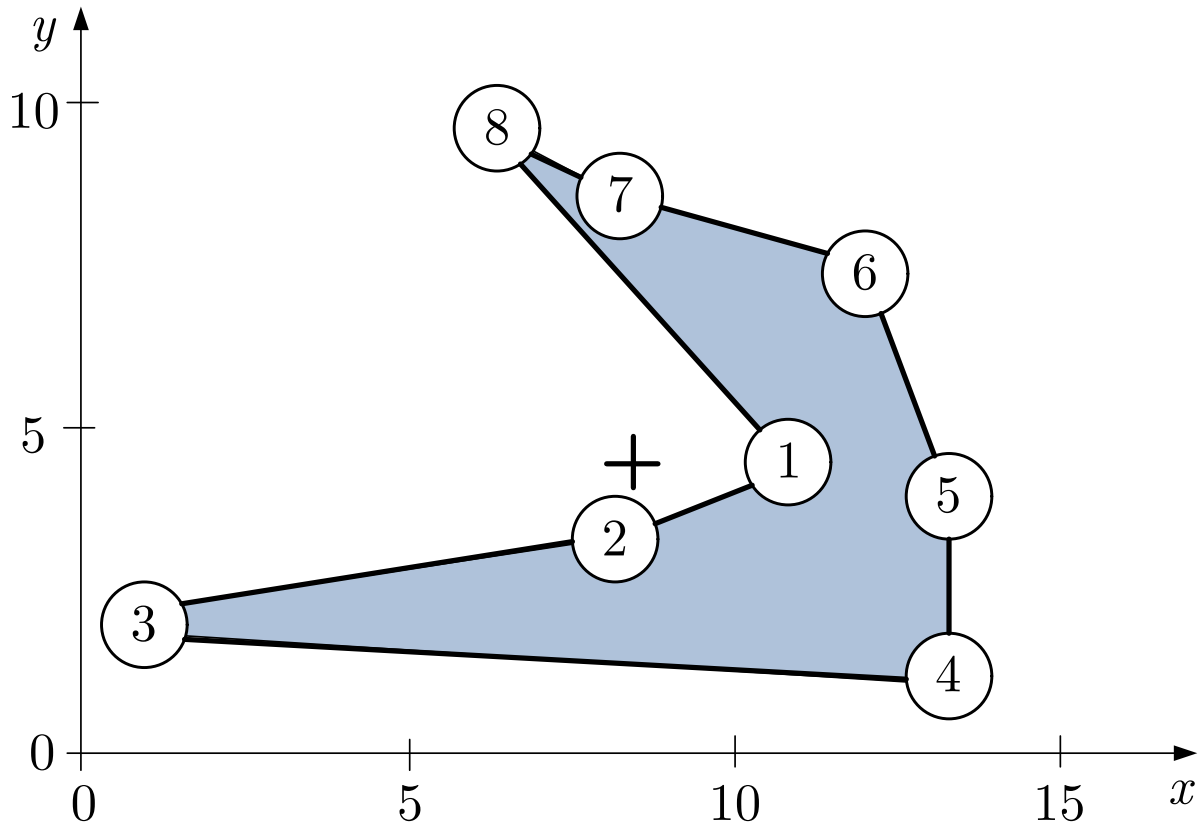
**Fig. 2: Convergence of the sensor states towards the consensus value  $\bar{p}_y$  for the two communication graphs of Fig. 1 (II)**

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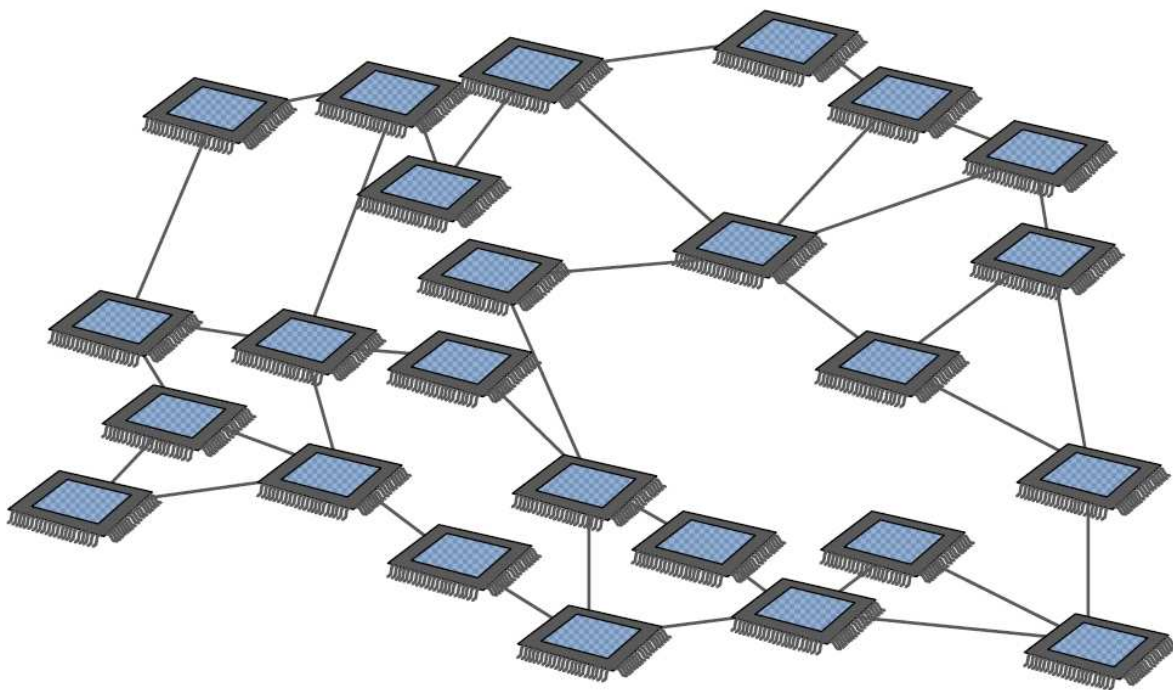
**Fig. 3: Determination of a centroid that lies outside of the polygon. Communication graph of the sensor network**

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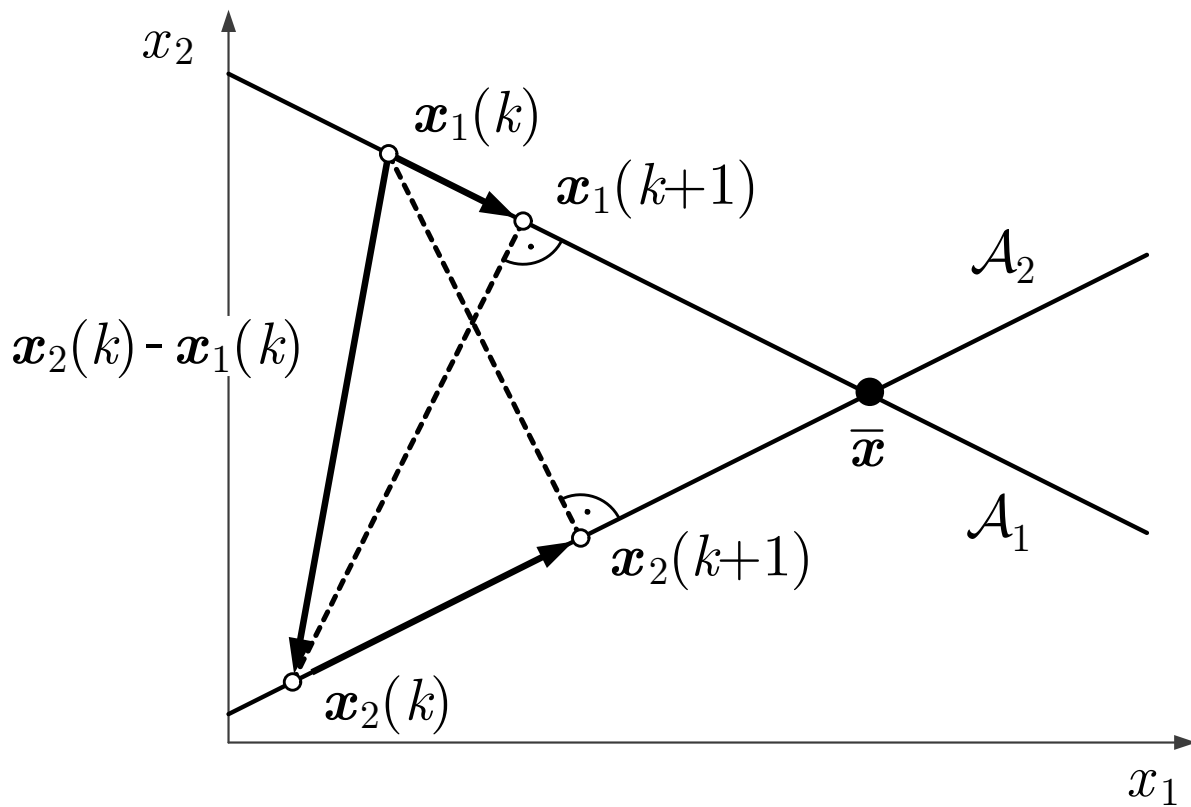
**Fig. 3: Determination of a centroid that lies outside of the polygon. Polygon formed by the sensors**





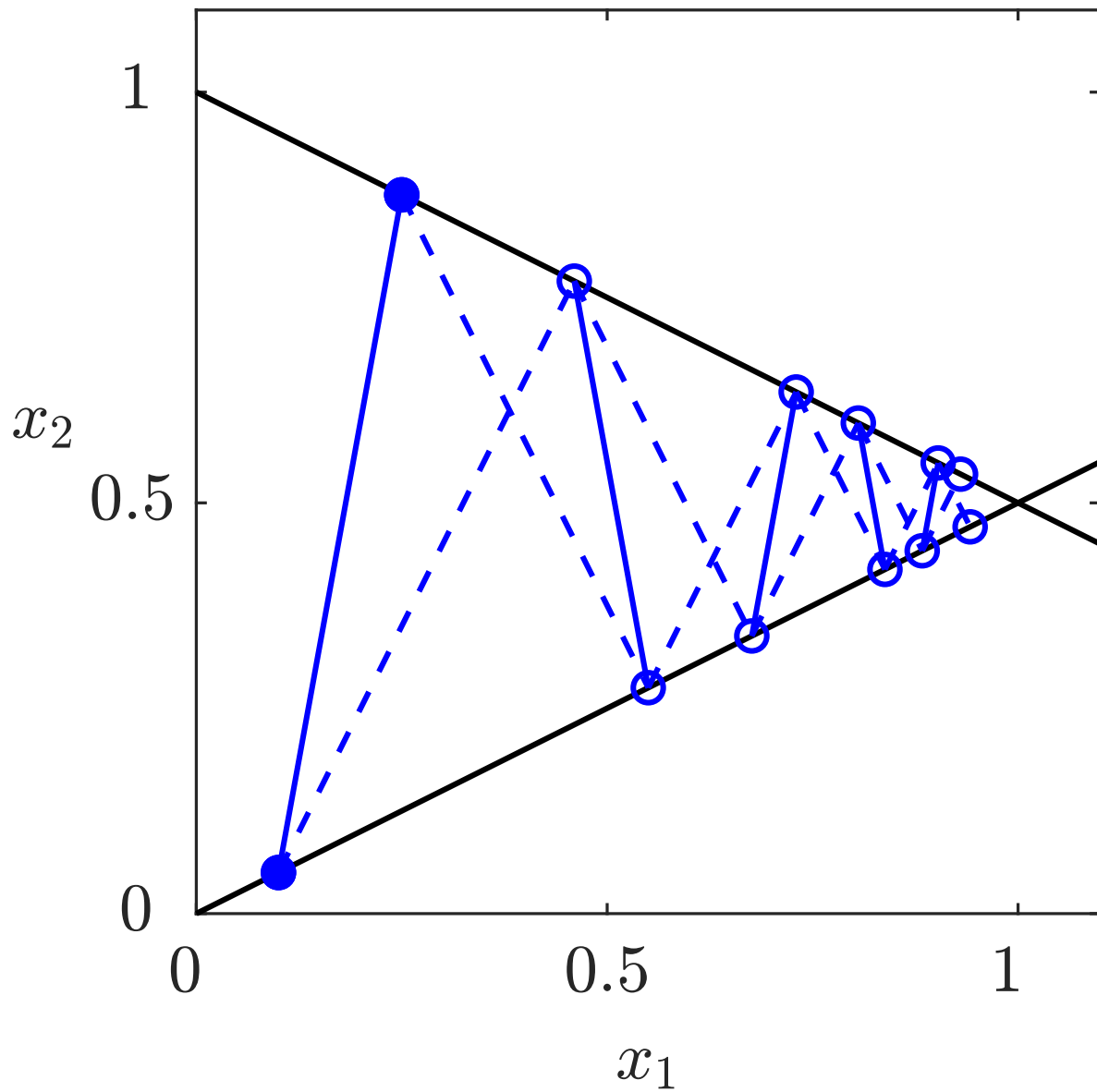
**Fig. 0: Networked processors cooperate to solve a linear equation**

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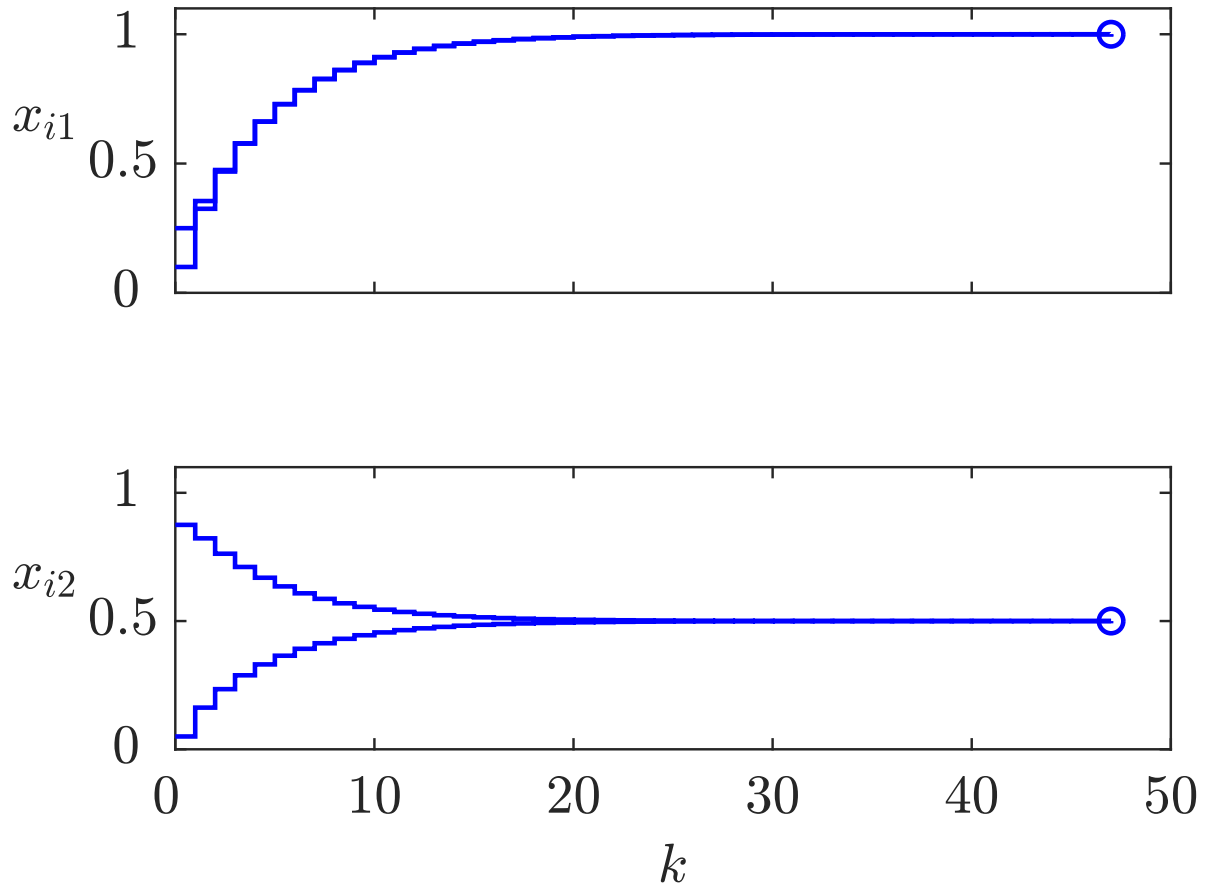
**Fig. 1: One iteration steps of the distributed algorithm**

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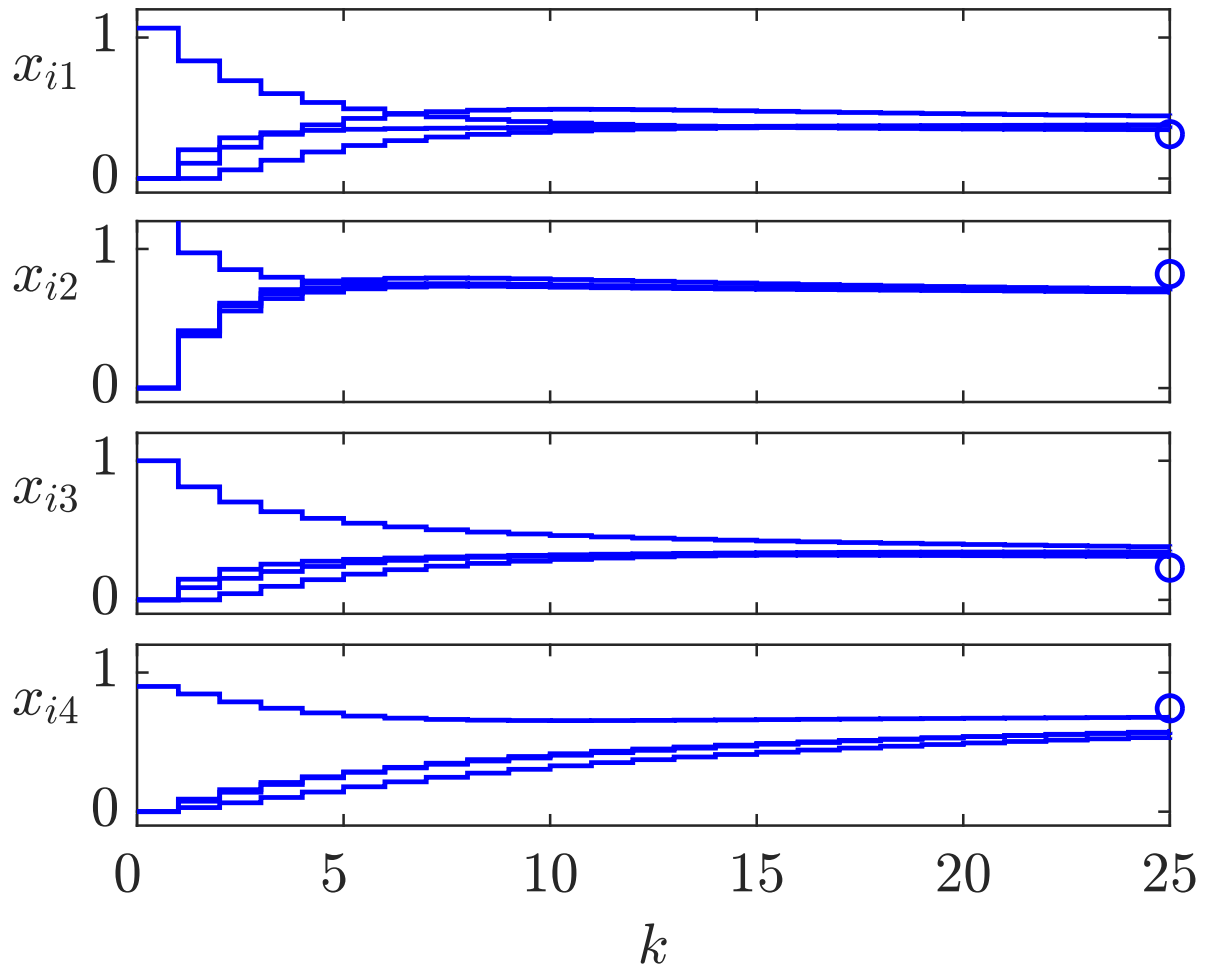
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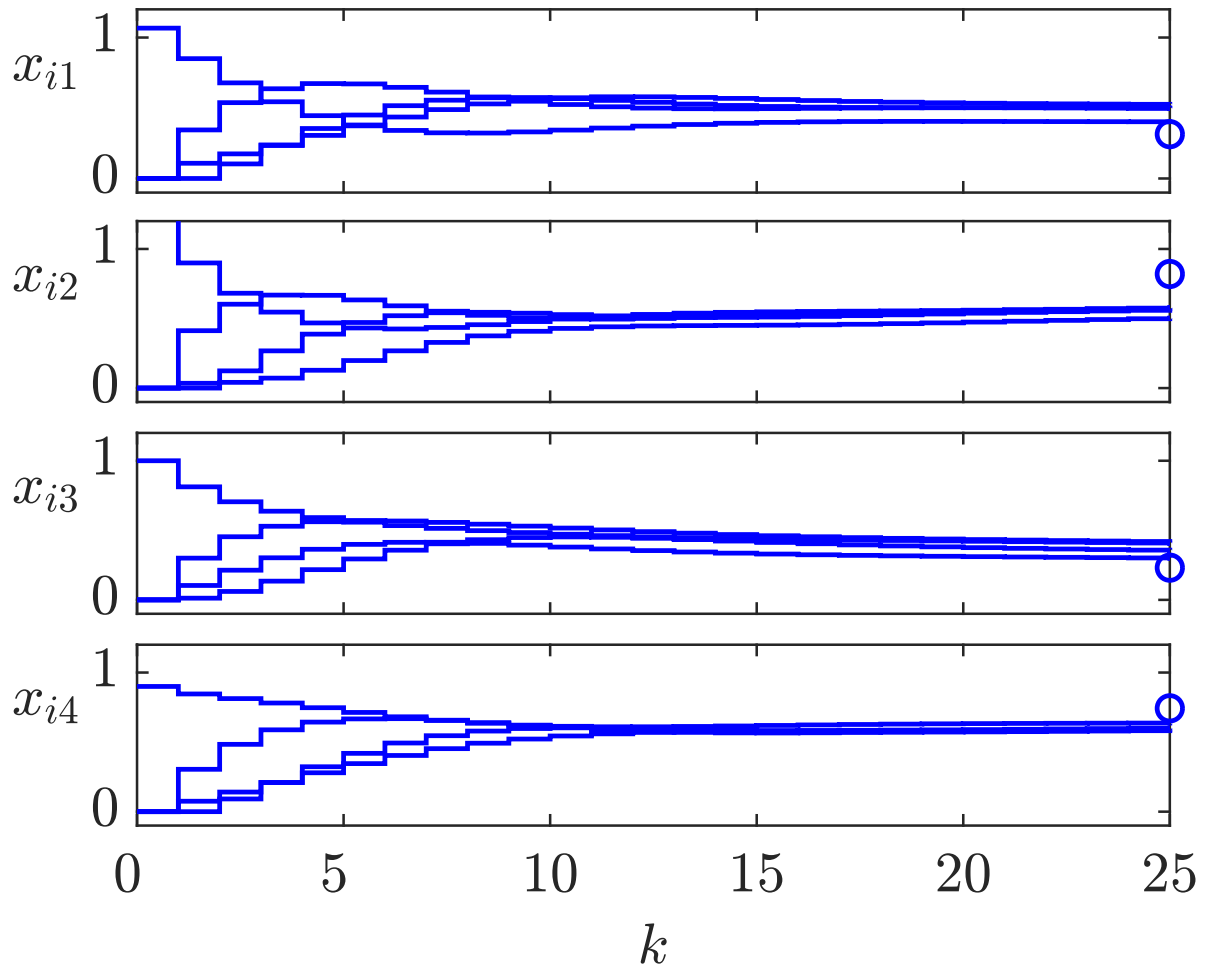
**Fig. 2: Solution of a linear equation as a consensus problem**

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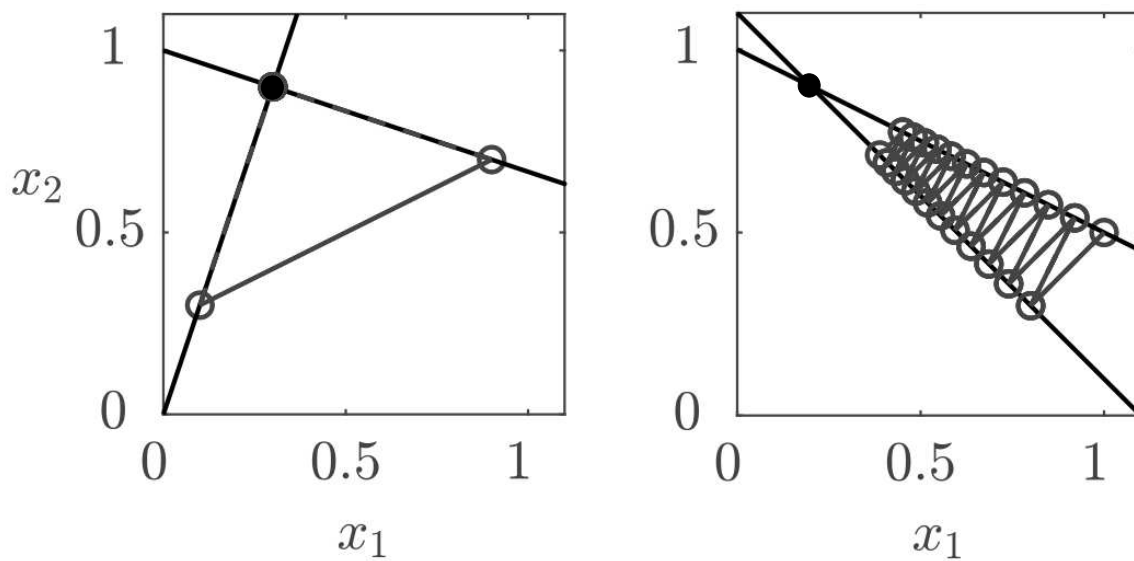
**Fig. 3: Solution of a linear equation with two communication structures**

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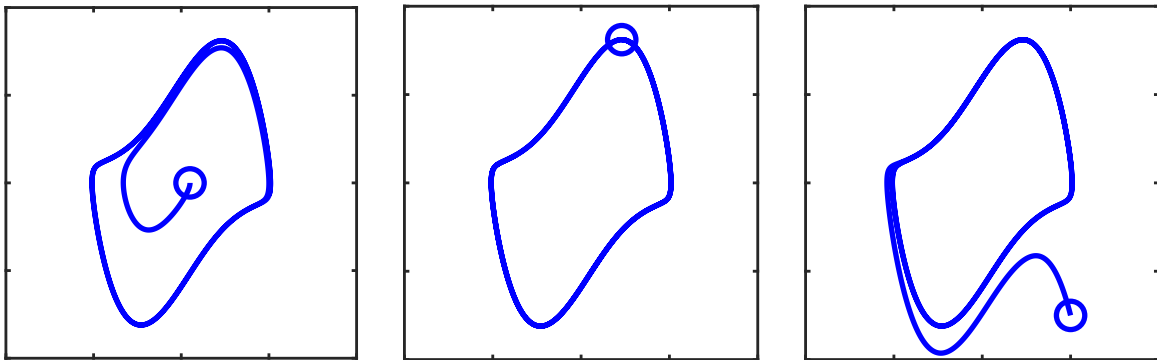
**Fig. 3: Solution of a linear equation with two communication structures**

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**Fig. 4: Two examples with different convergence properties for the same communication structure**

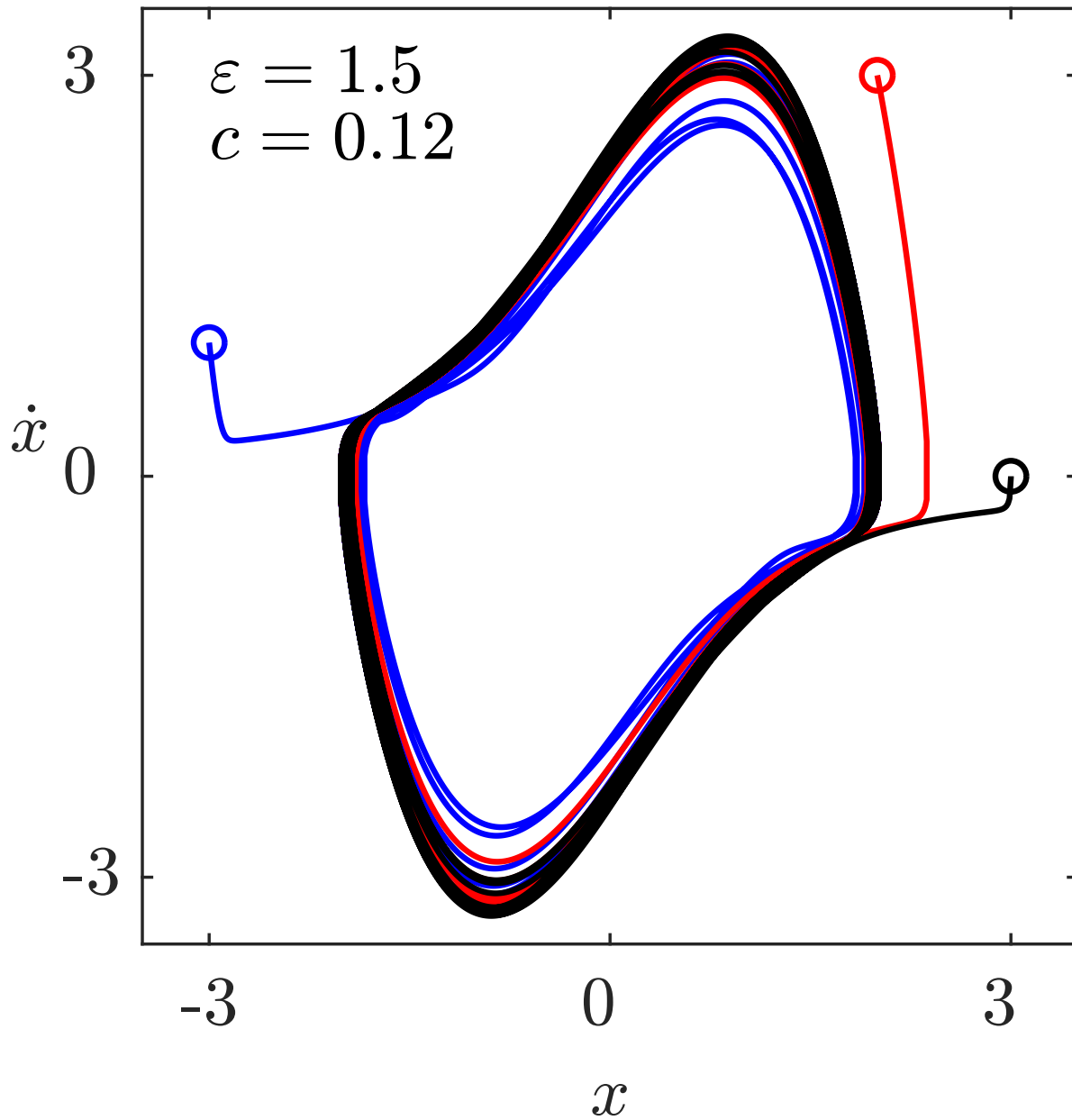
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**Fig. 0: Behaviour of van der Pol oscillators**

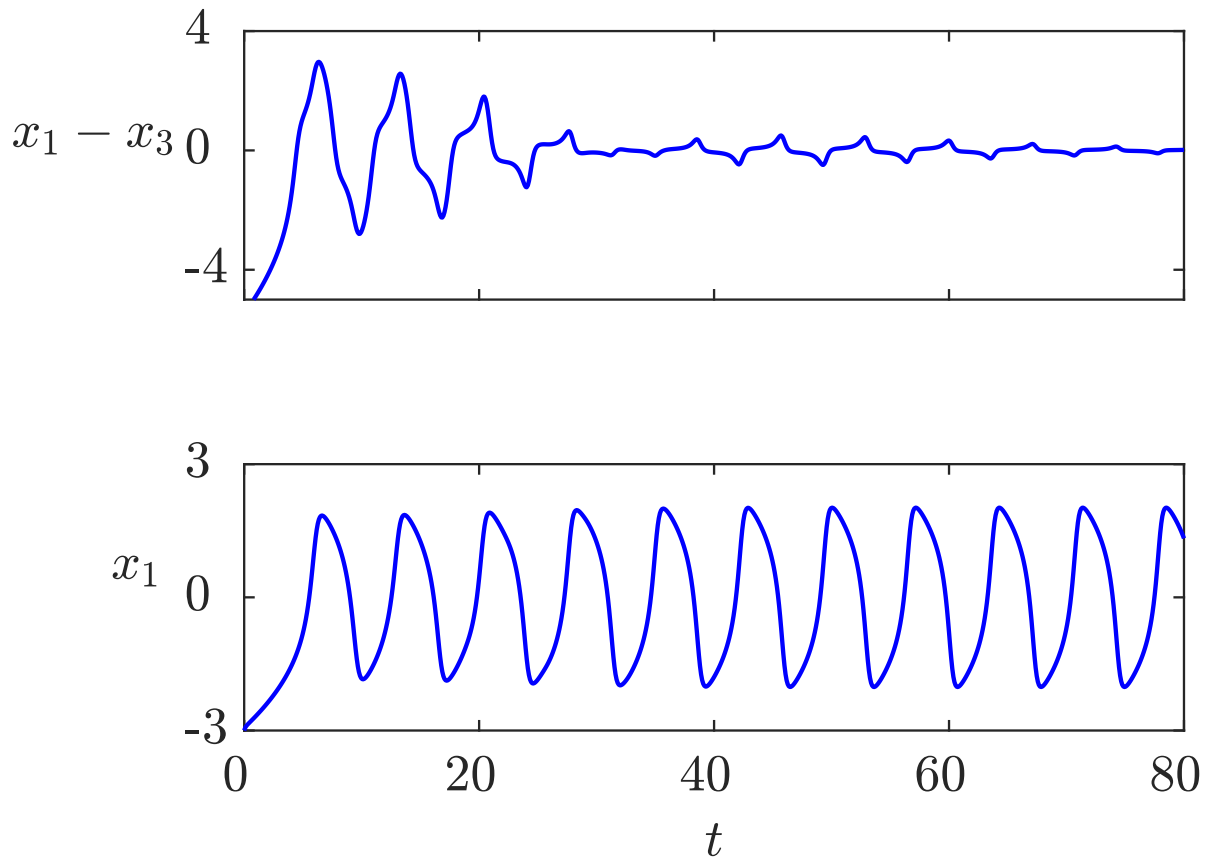
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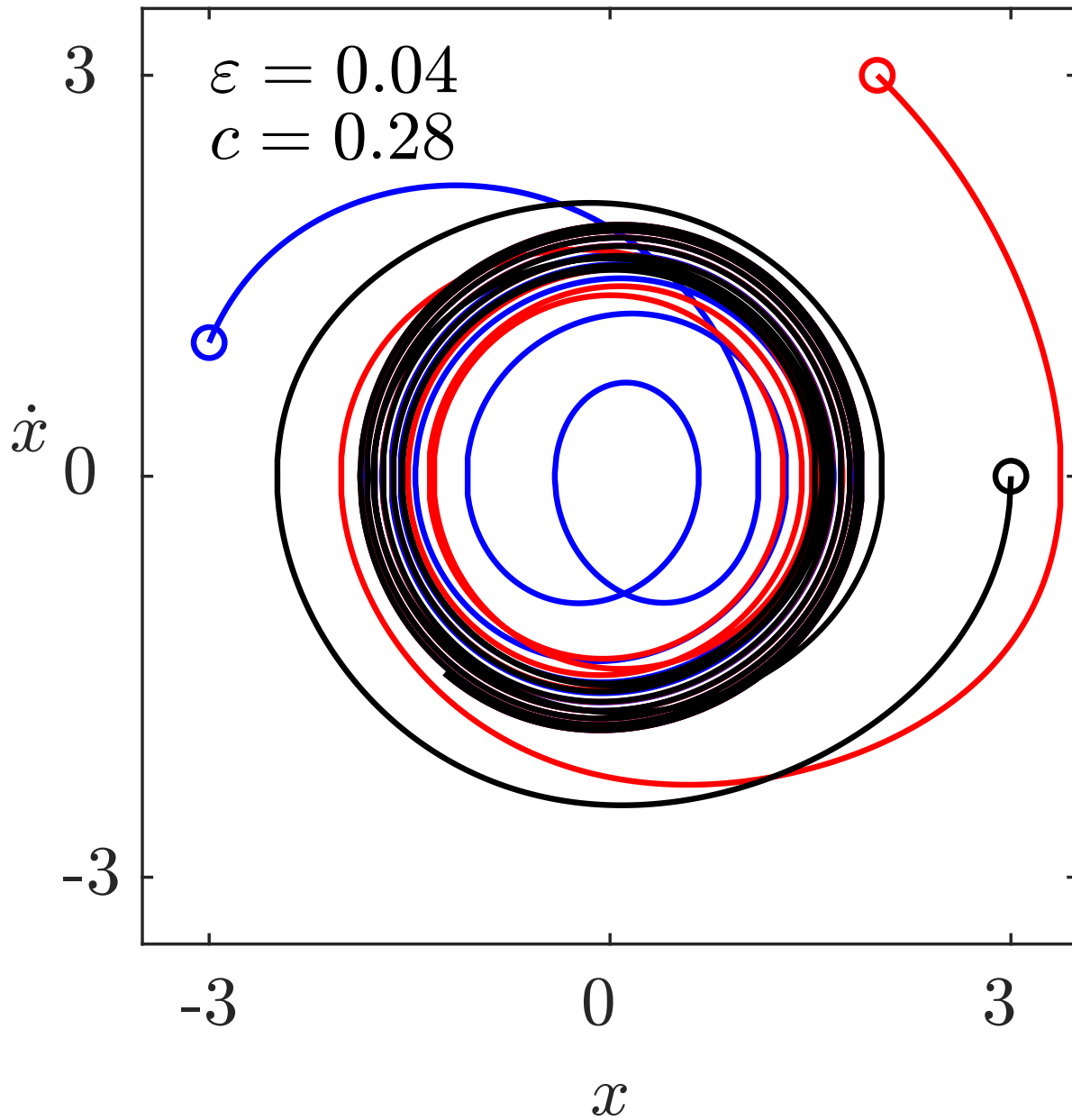
**Fig. 1: Synchronisation of three van der Pol oscillators that are coupled in a directed ring**

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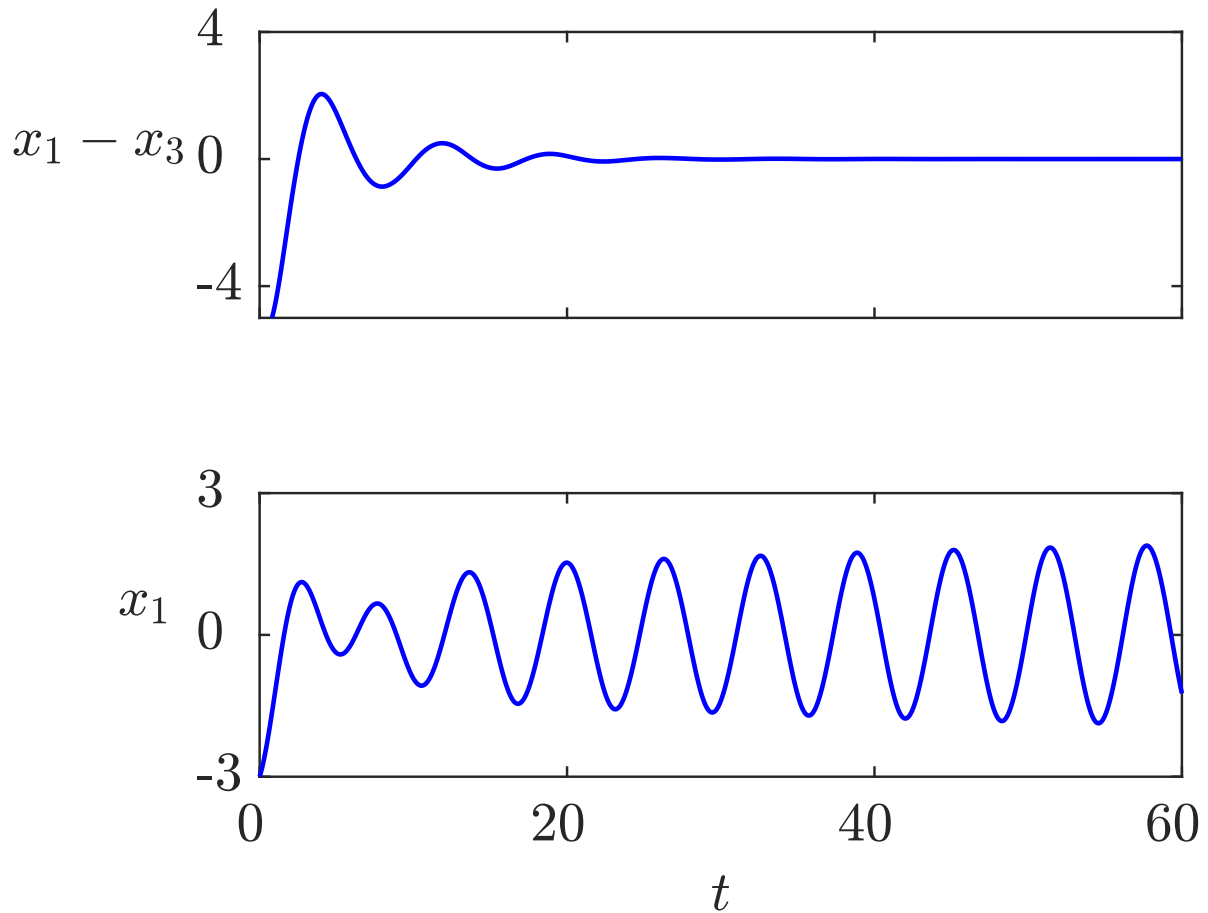
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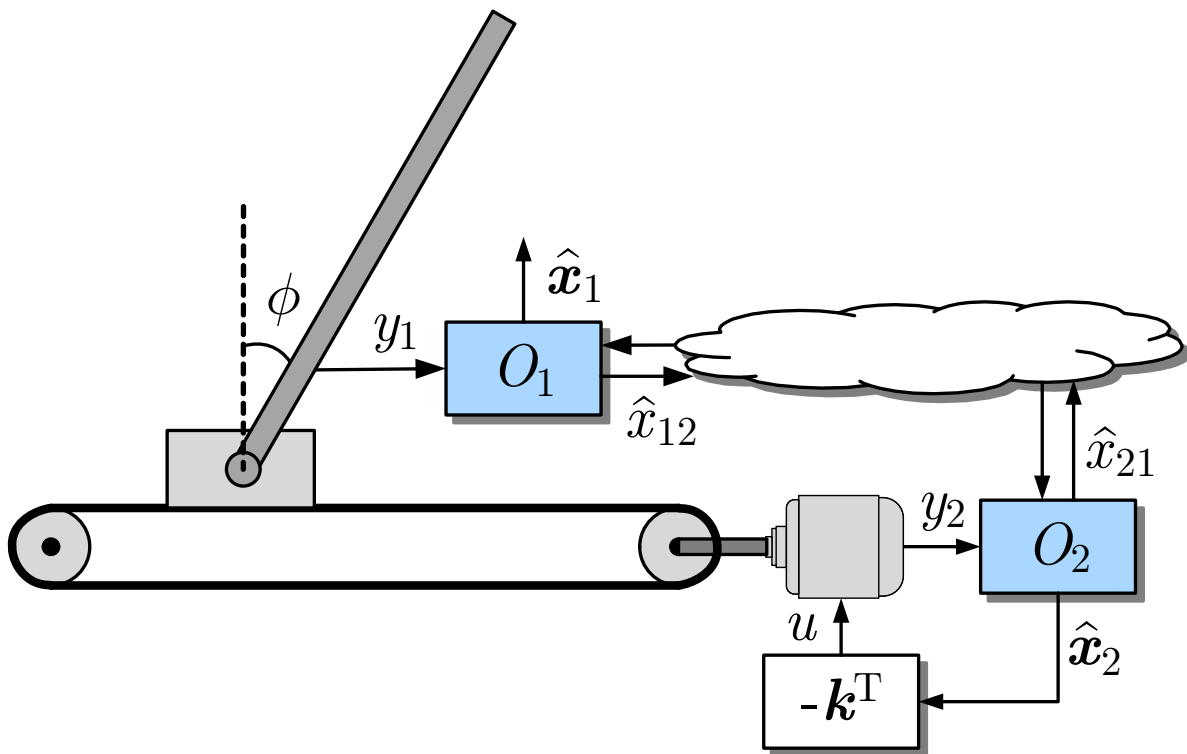
**Fig. 2: Synchronisation of three van der Pol oscillators with small damping factor**

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**Fig. 2: Synchronisation of three van der Pol oscillators with small damping factor**

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**Fig. 0: Inverted pendulum with distributed state observers**

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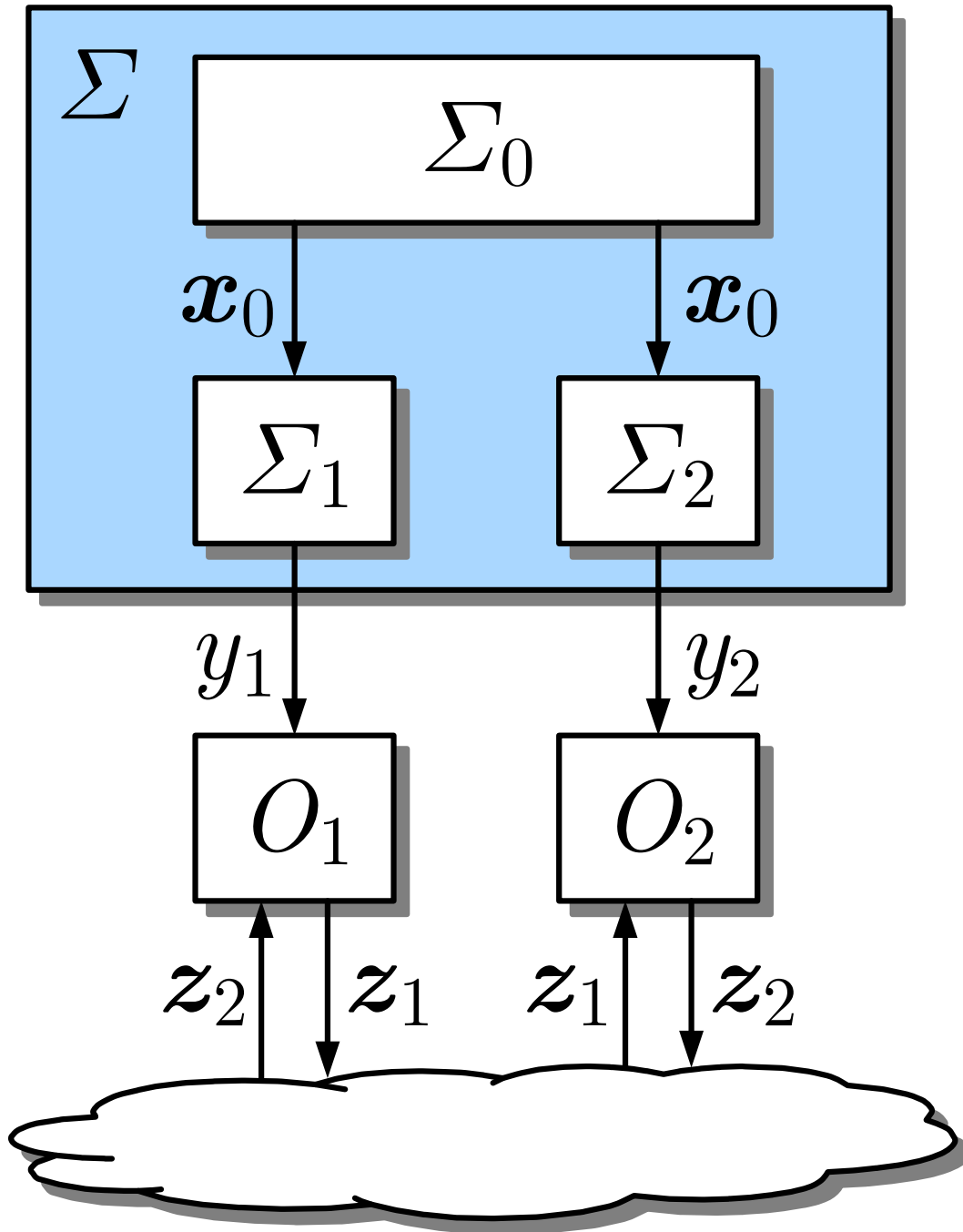
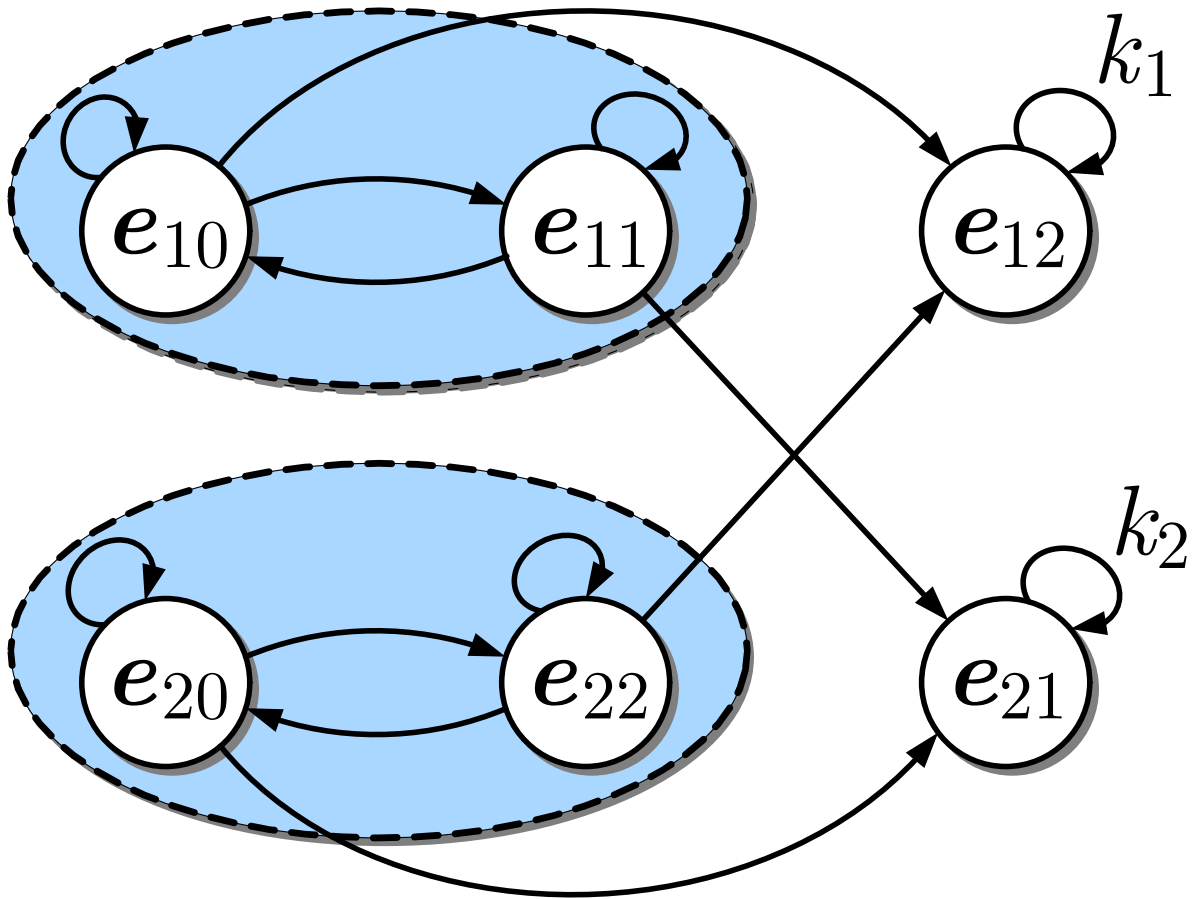
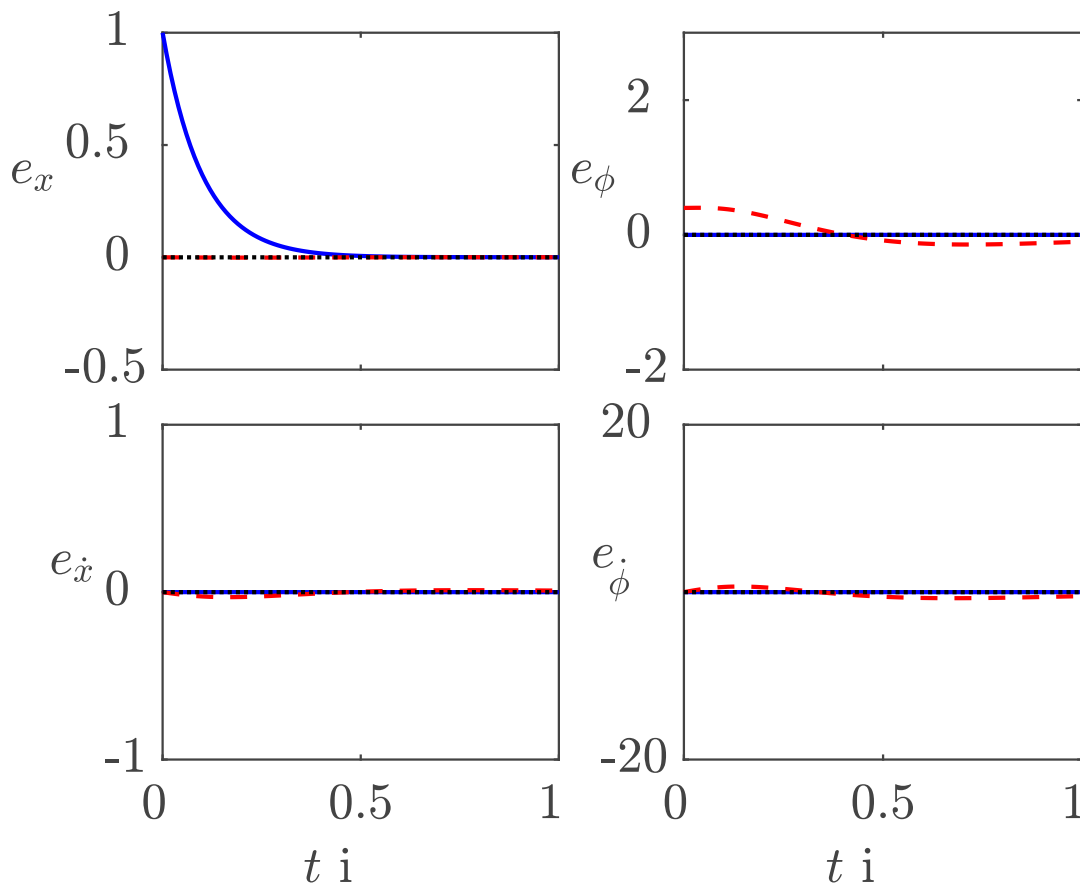


Fig. 1. Distributed observers for the system  $\Sigma$



**Fig. 2: Structure graph of the system matrix of the error representation**

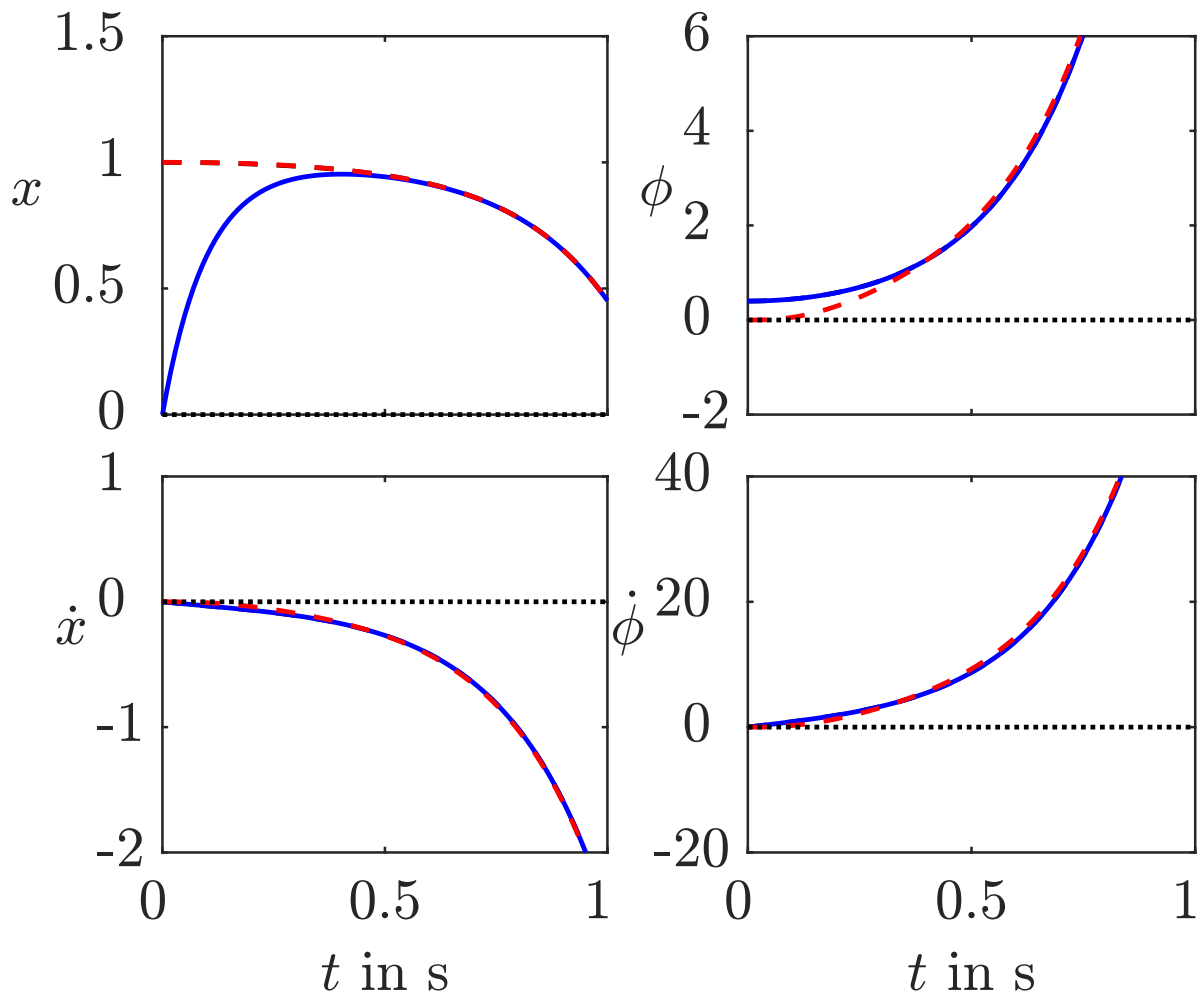
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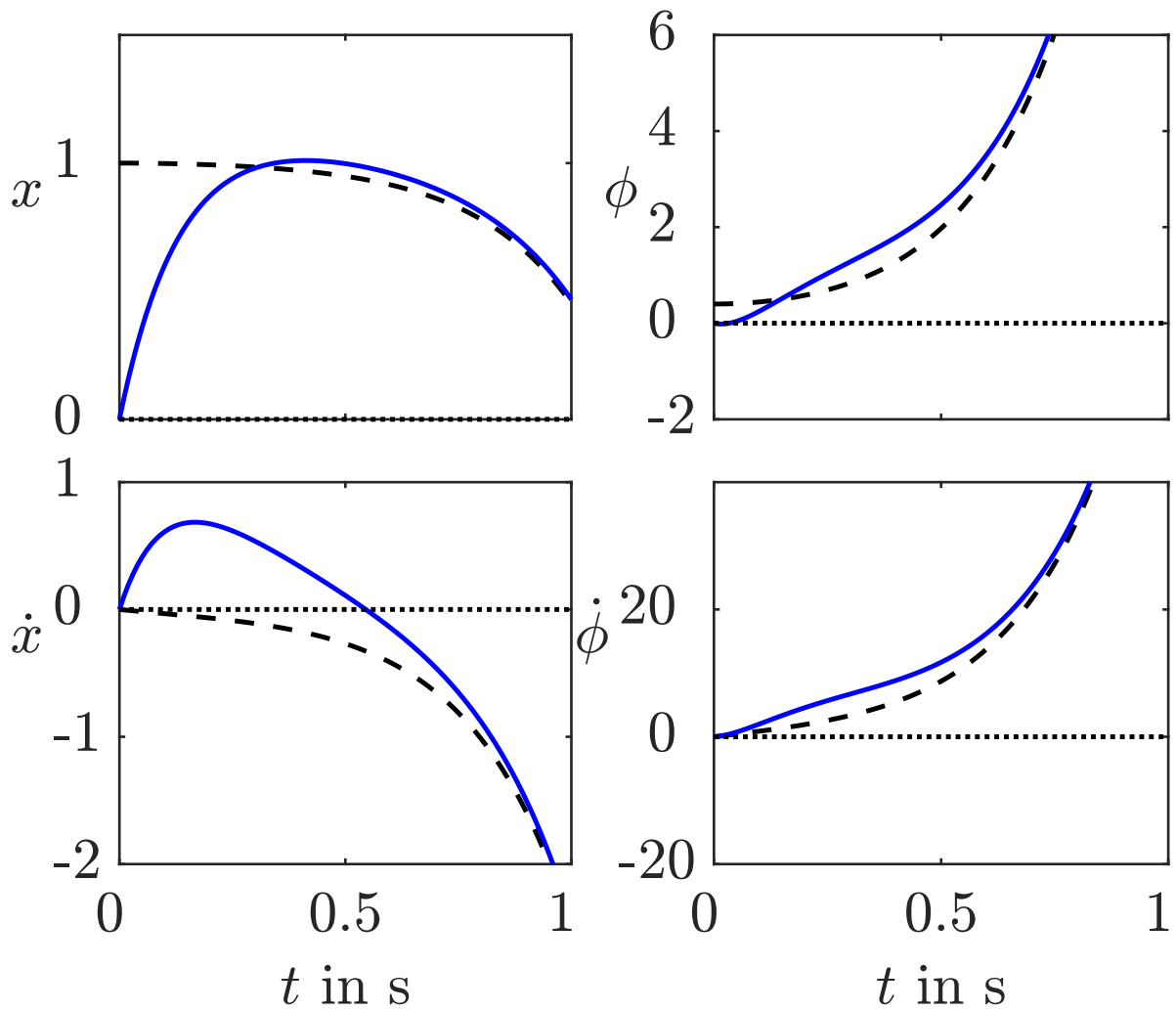
**Fig. 3: Observation errors of the distributed state observer ( $O_1$  —,  $O_2$  - - -)**

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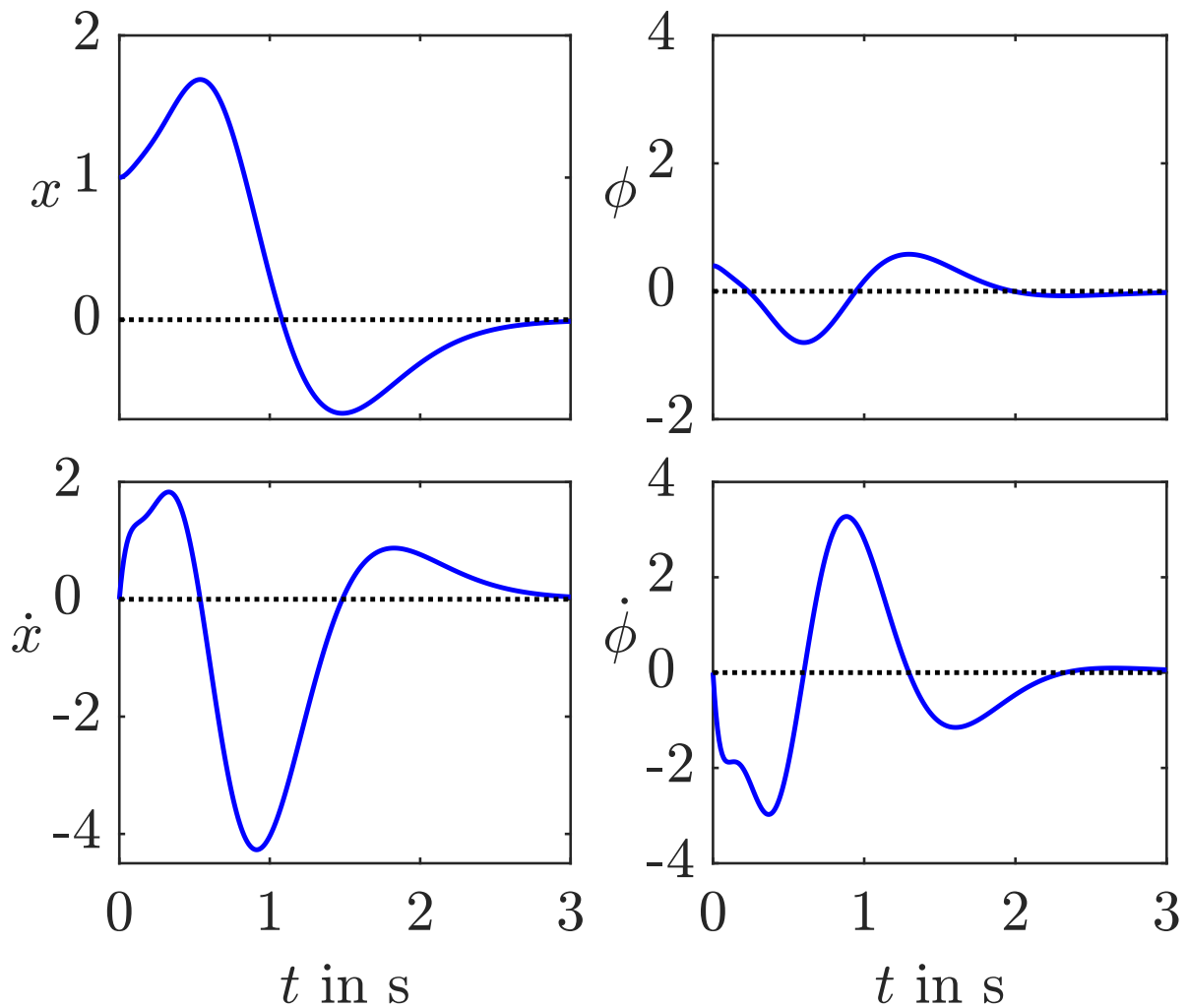




**Fig. 4: Observation results obtained by the distributed observer**

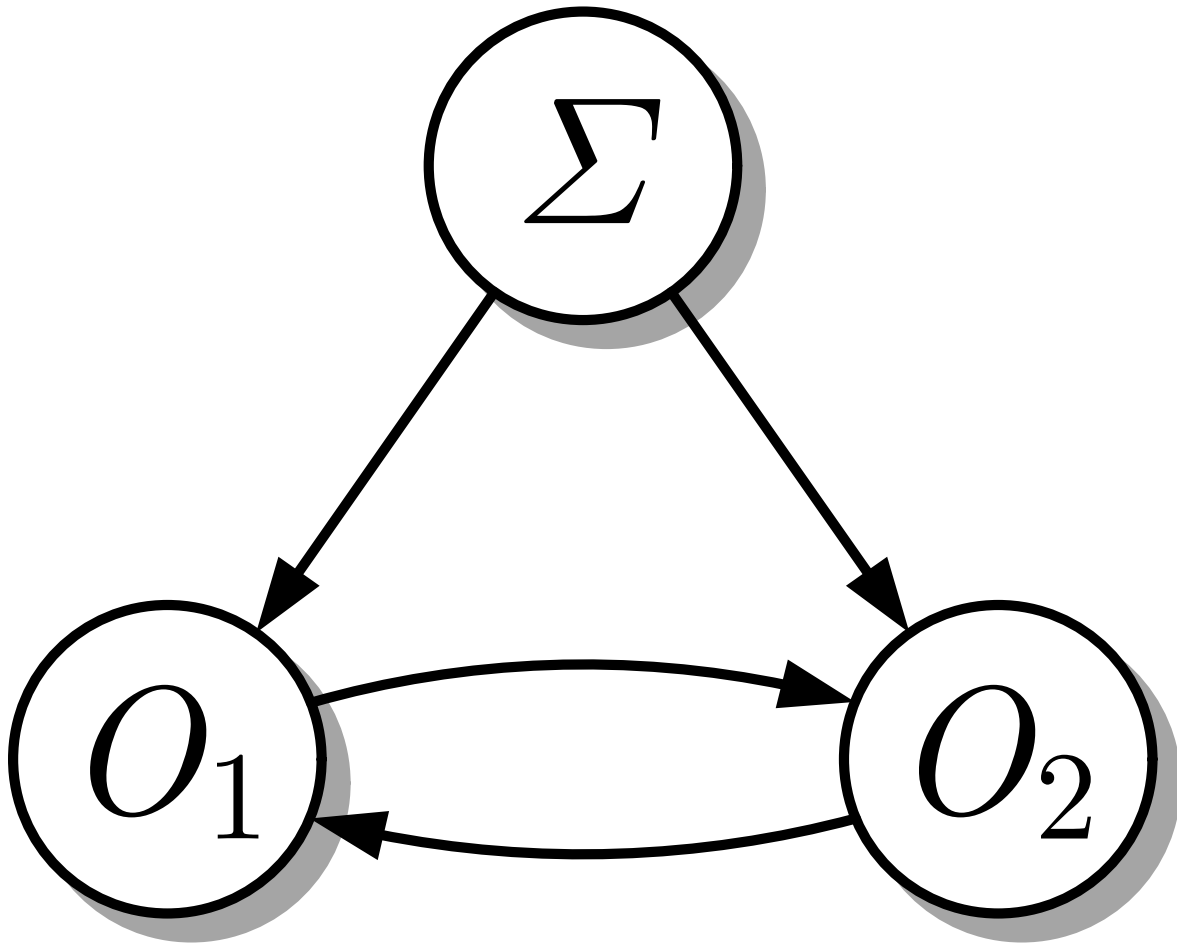


**Fig. 4: Observation results obtained by a centralised state observer**



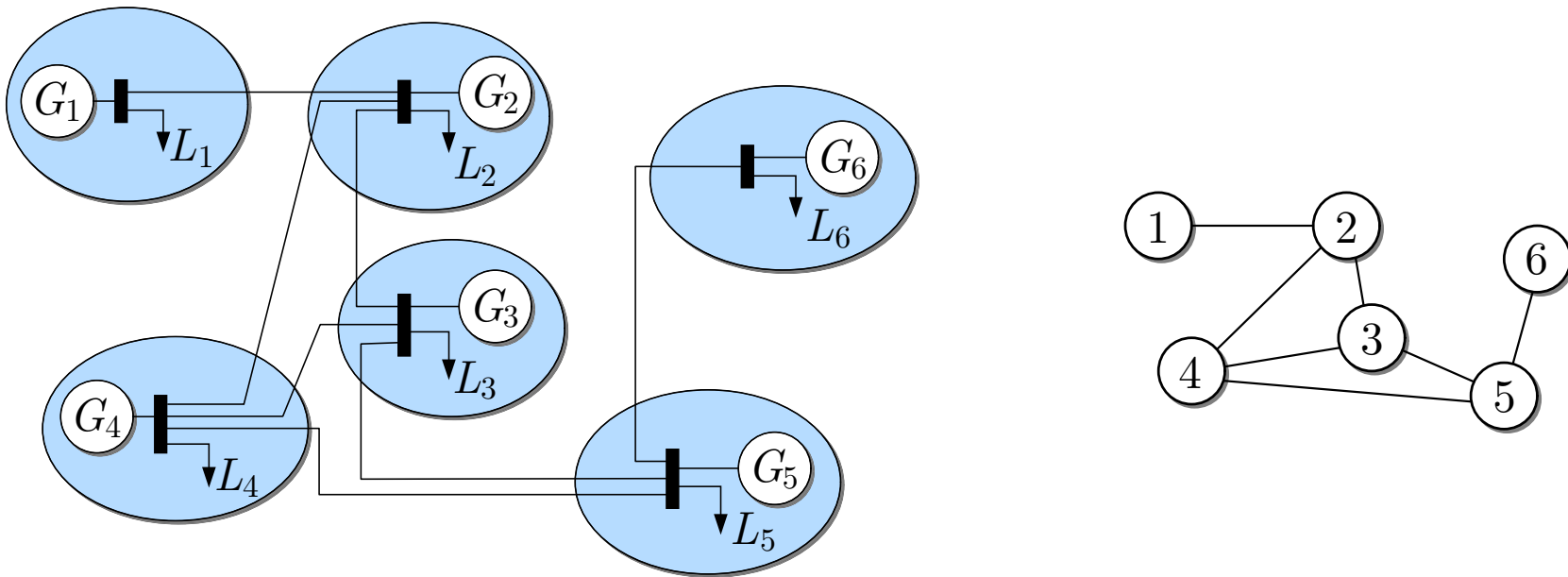
**Fig. 5: Behaviour of the stabilised pendulum**

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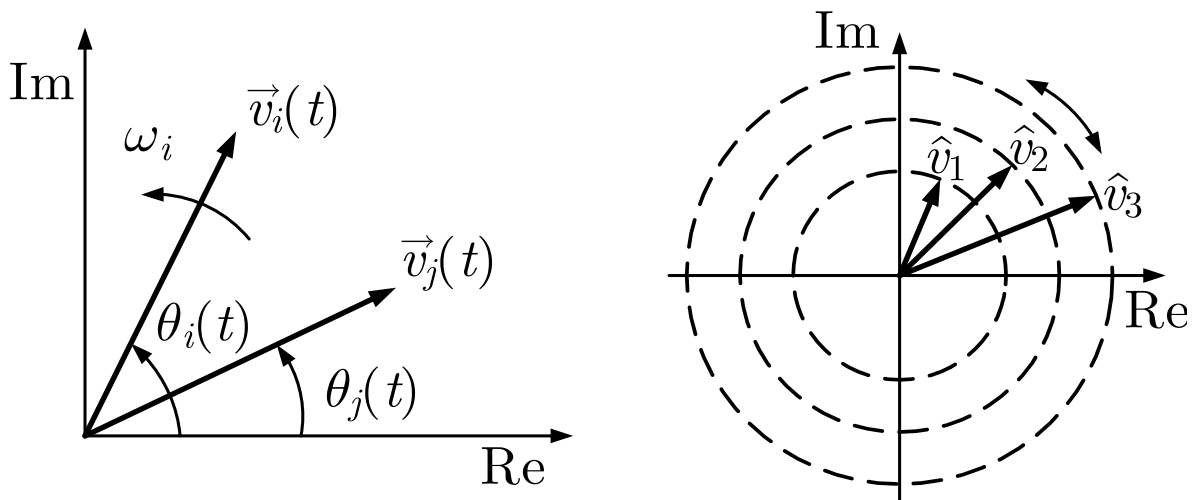
**Fig. 6:** Communication graph of the distributed state observer

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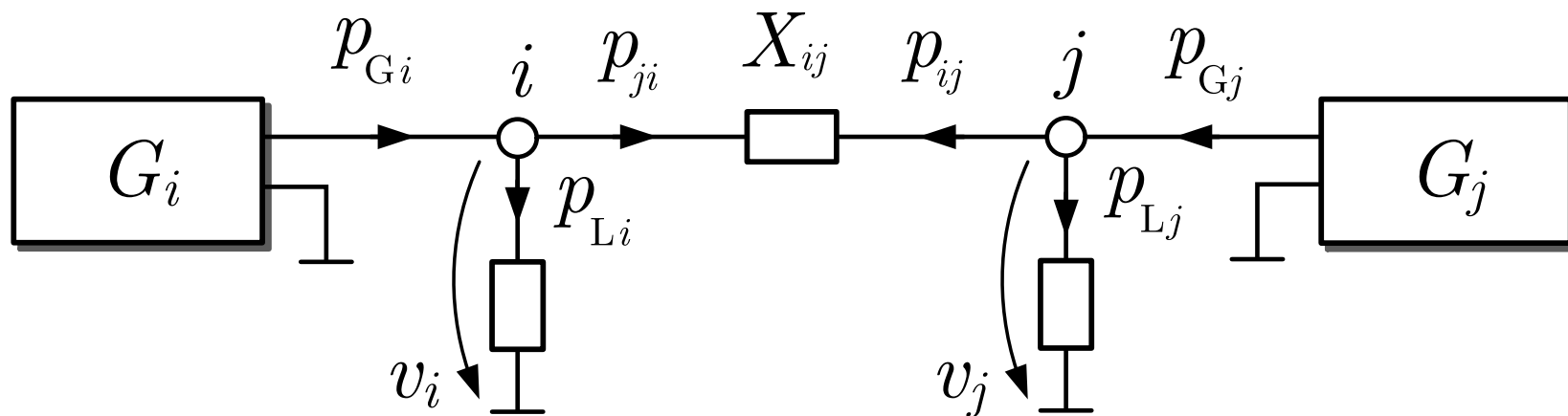
**Fig. 0. Electrical power network**

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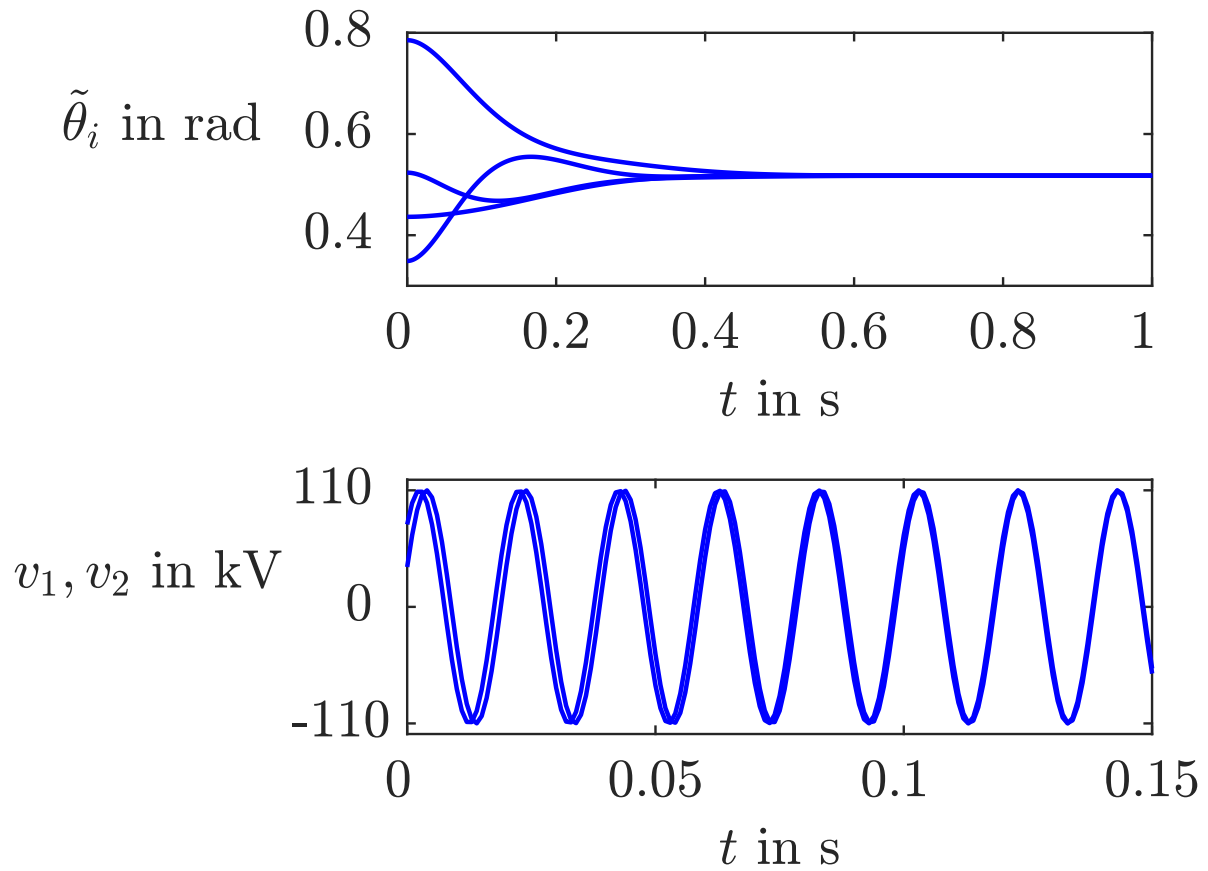
**Fig. 1: Arrow diagram of the area voltages**

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**Fig. 2. Block diagram of two coupled areas**

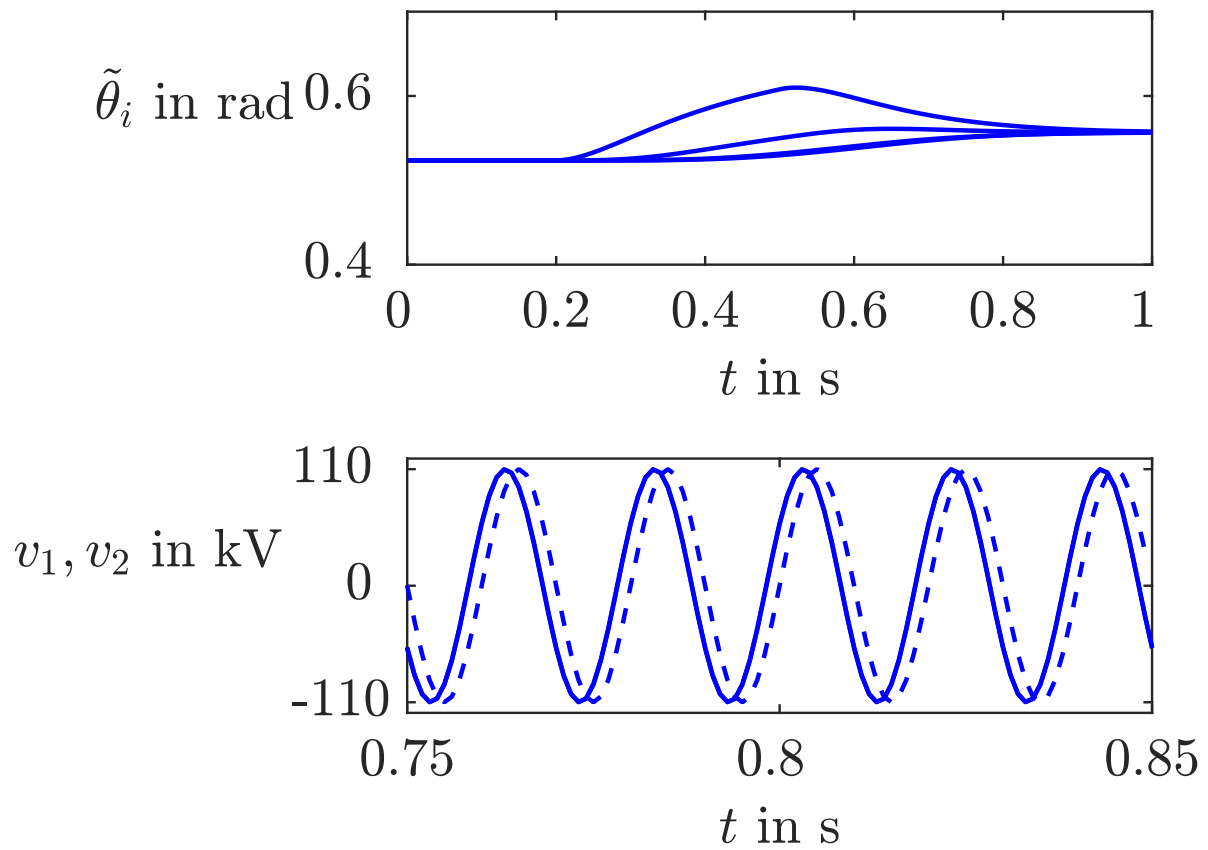
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**Fig. 3: Behaviour of the power network with balanced areas**

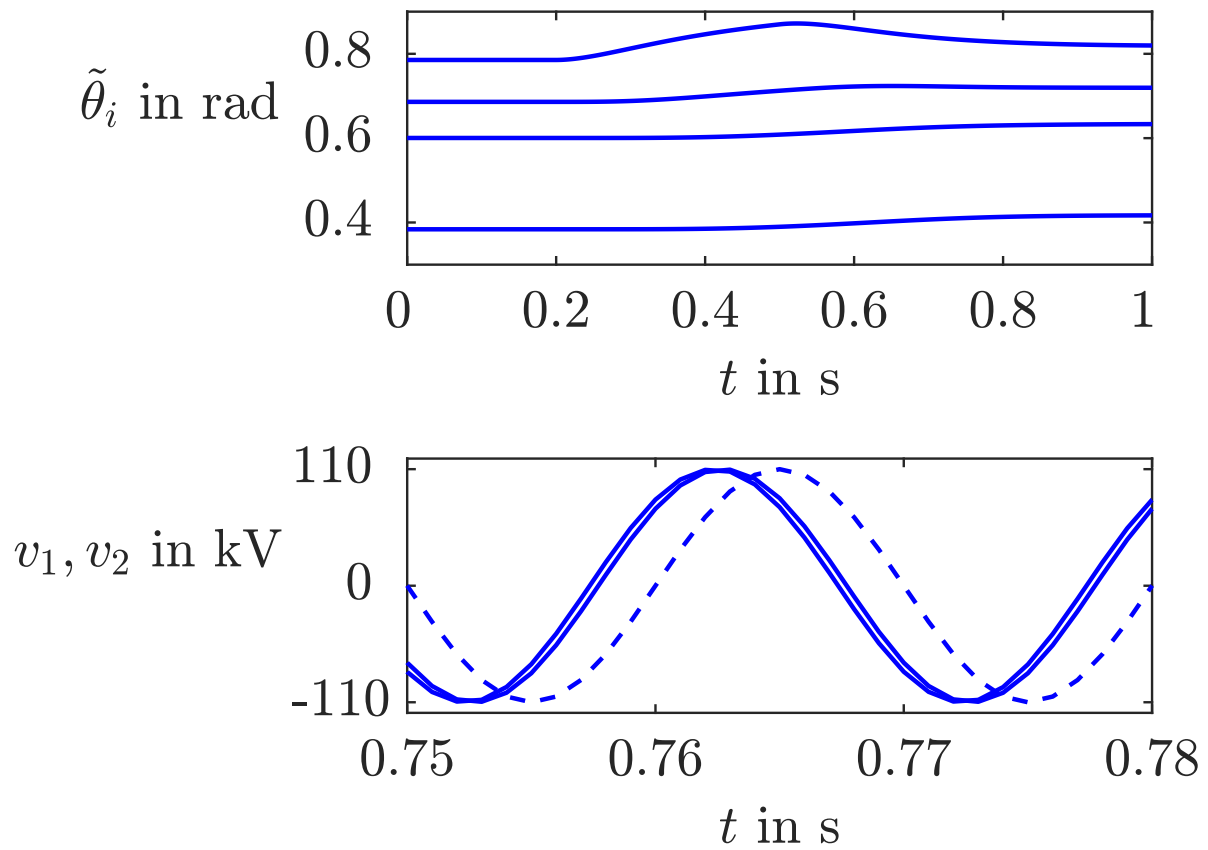
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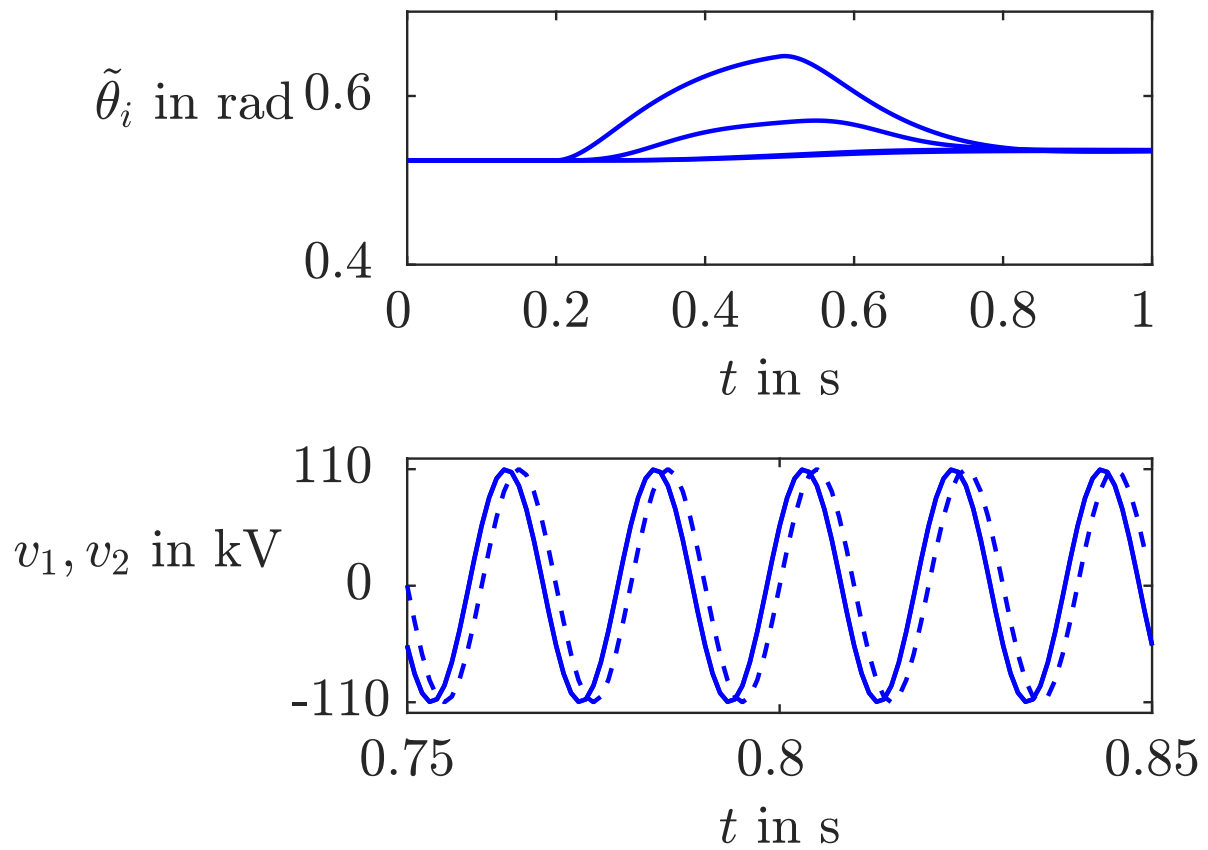
**Fig. 4: Behaviour of the balanced power network subject to a disturbance**

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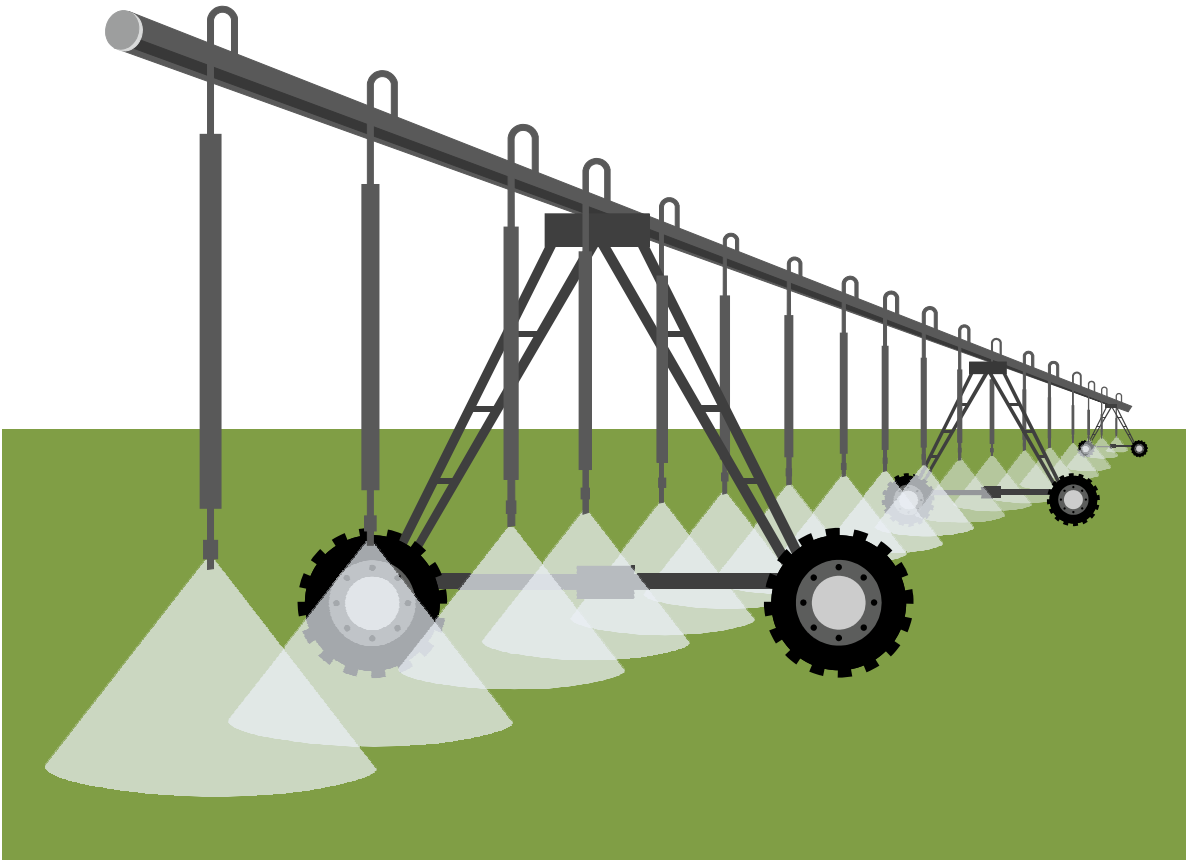
**Fig. 5: Behaviour of the unbalanced power network**

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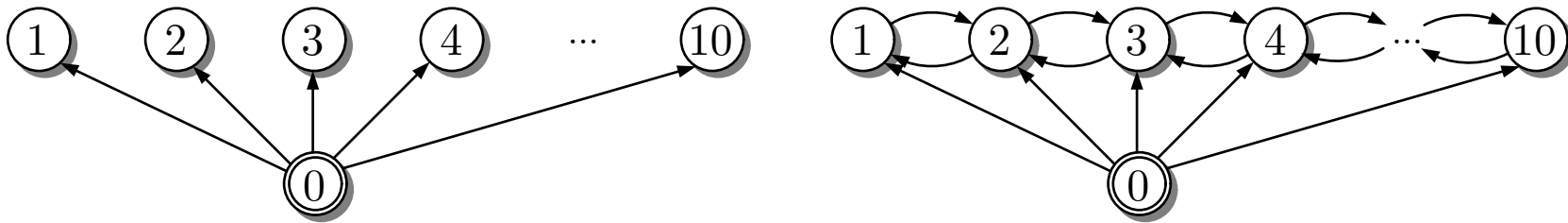
**Fig. 6: Disturbance behaviour of a balanced power network with renewable energy sources**

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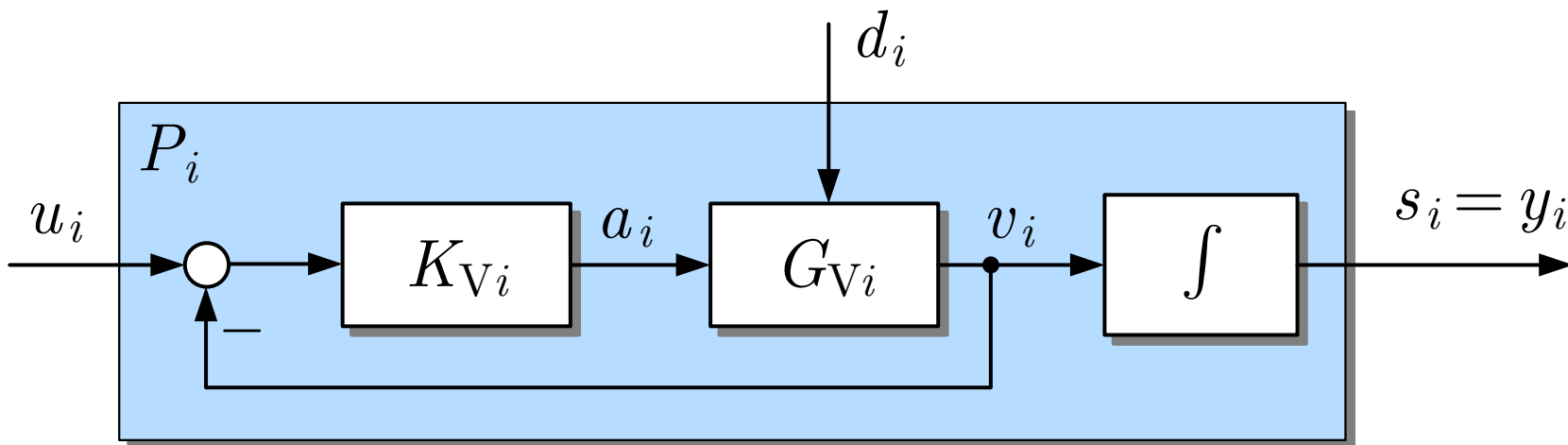
**Fig. 0: Irrigation system**

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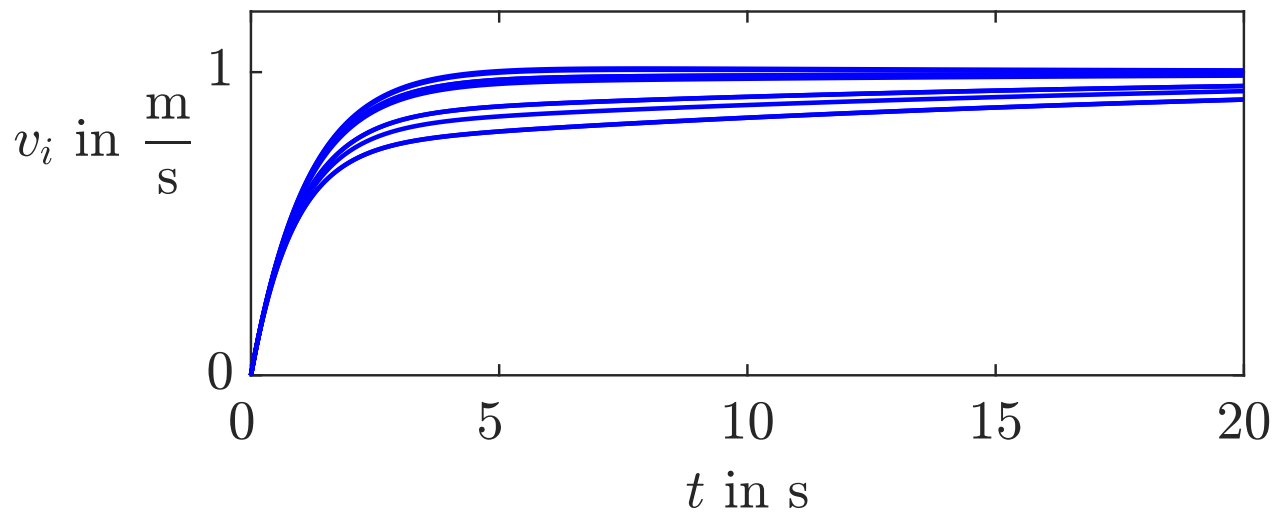
**Fig. 1. Communication graph of the irrigation system**

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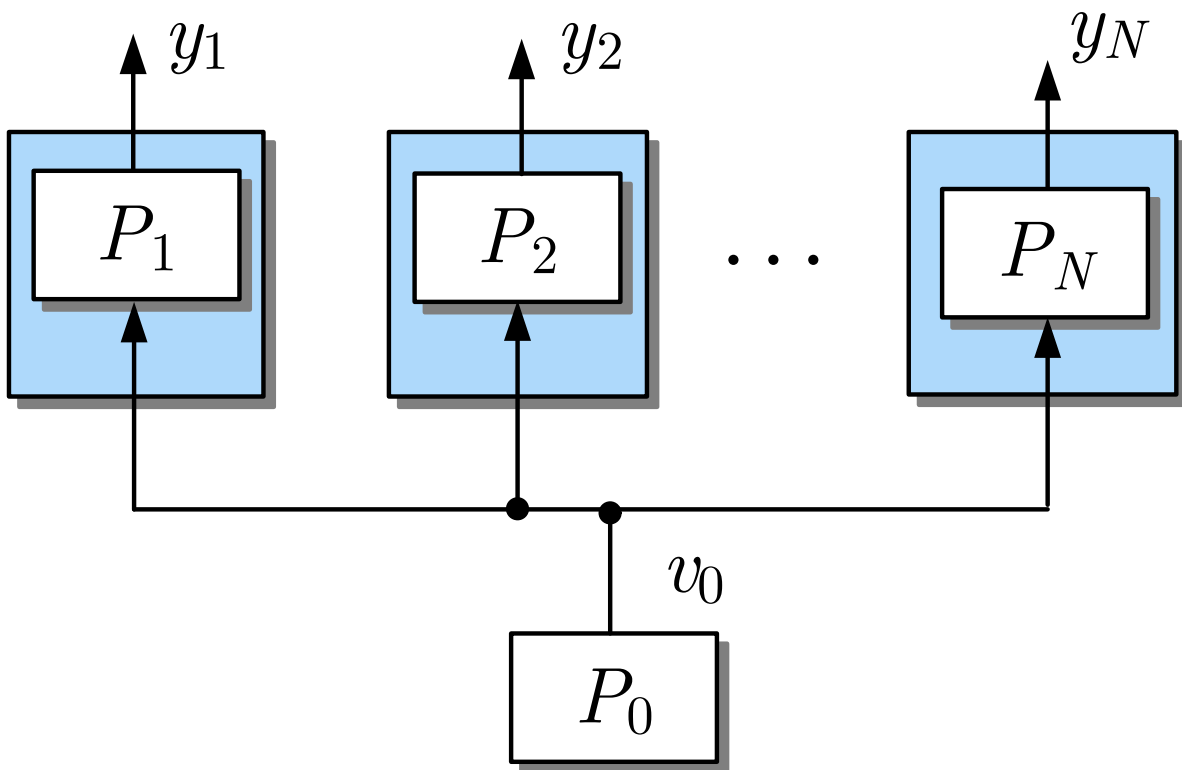
**Fig. 2.** Model of a single pillar

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**Fig. 3: Command step response of the ten pillars**

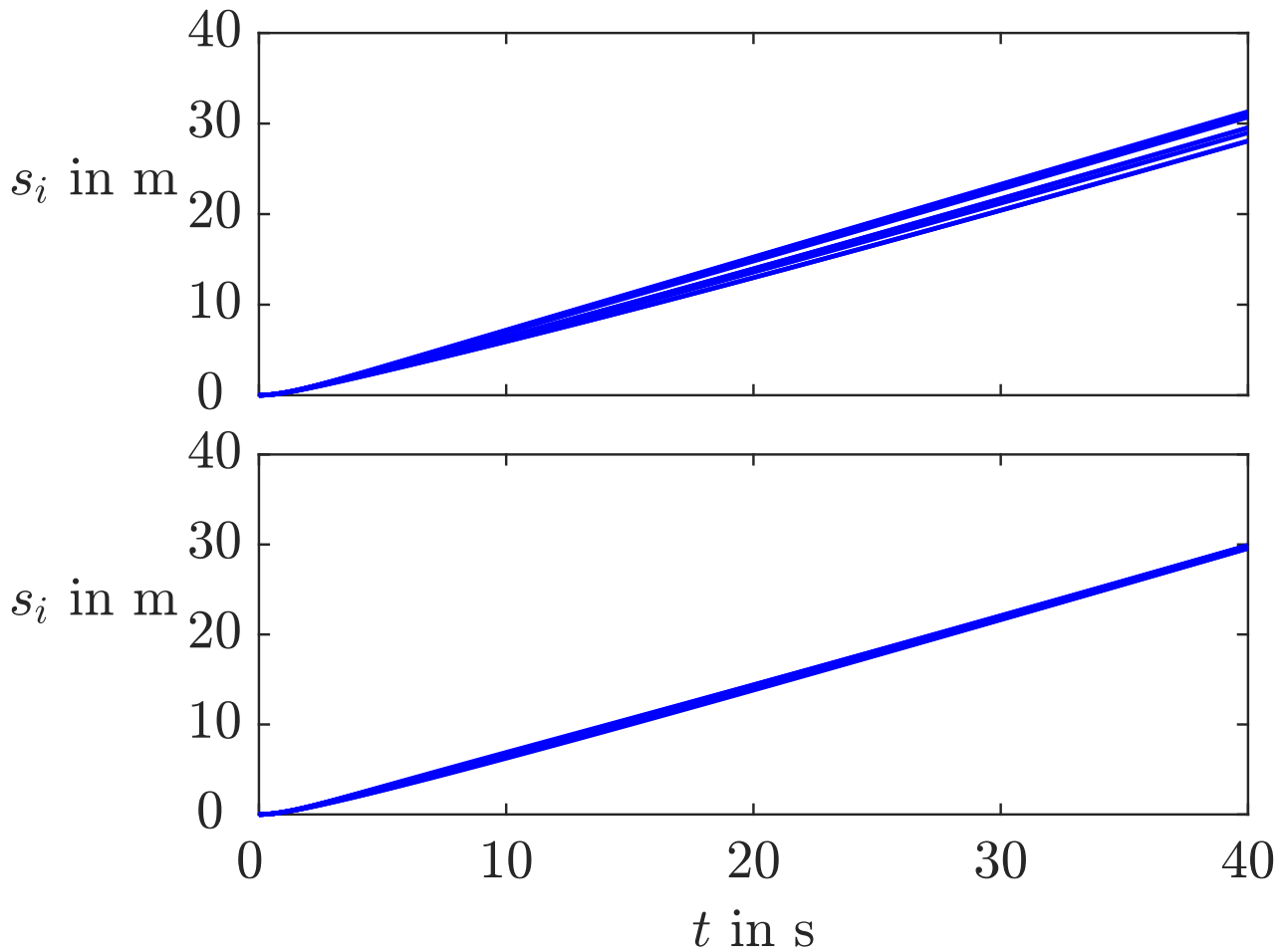
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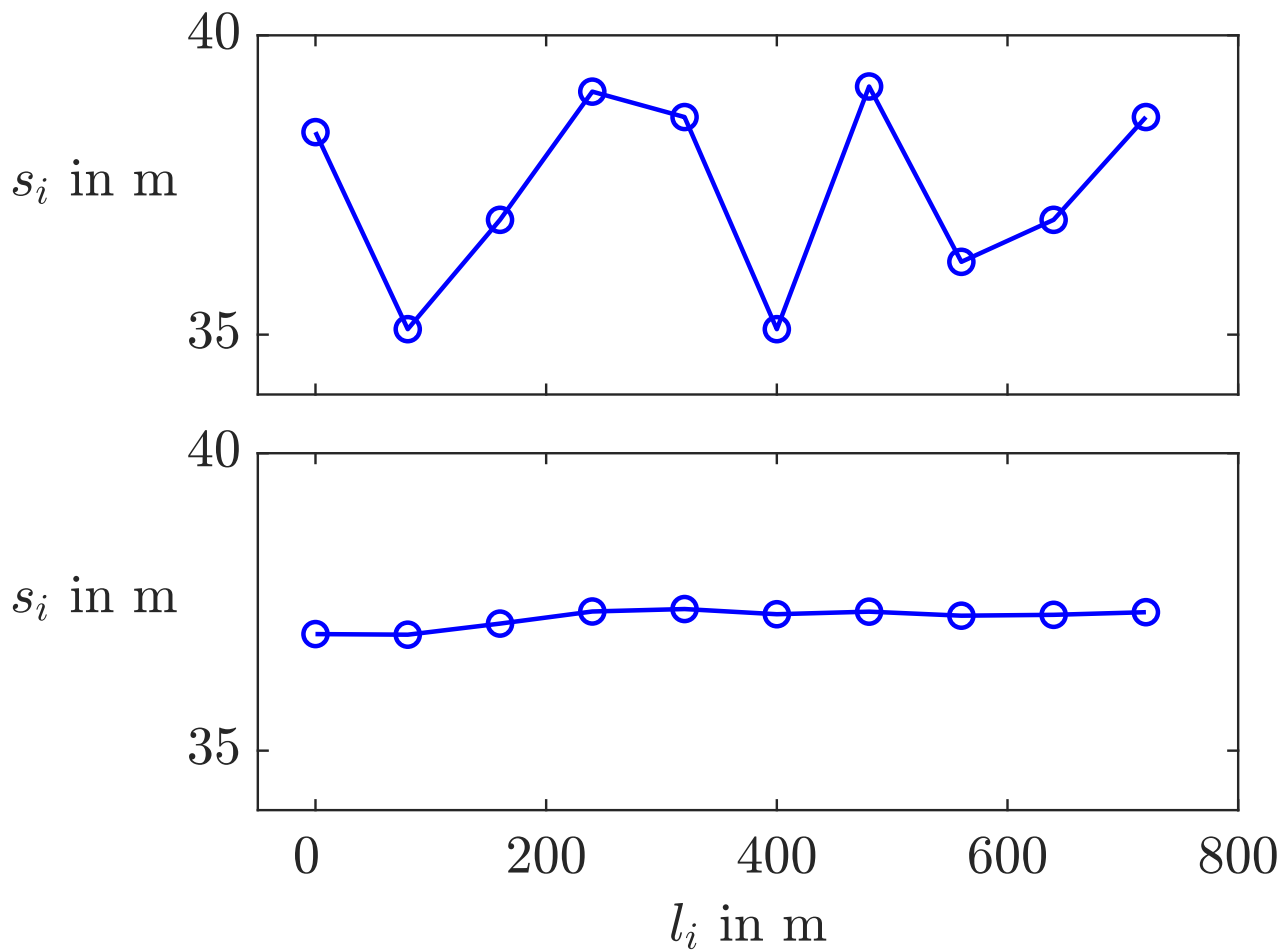
**Fig. 4: Irrigation system with decentralised control**

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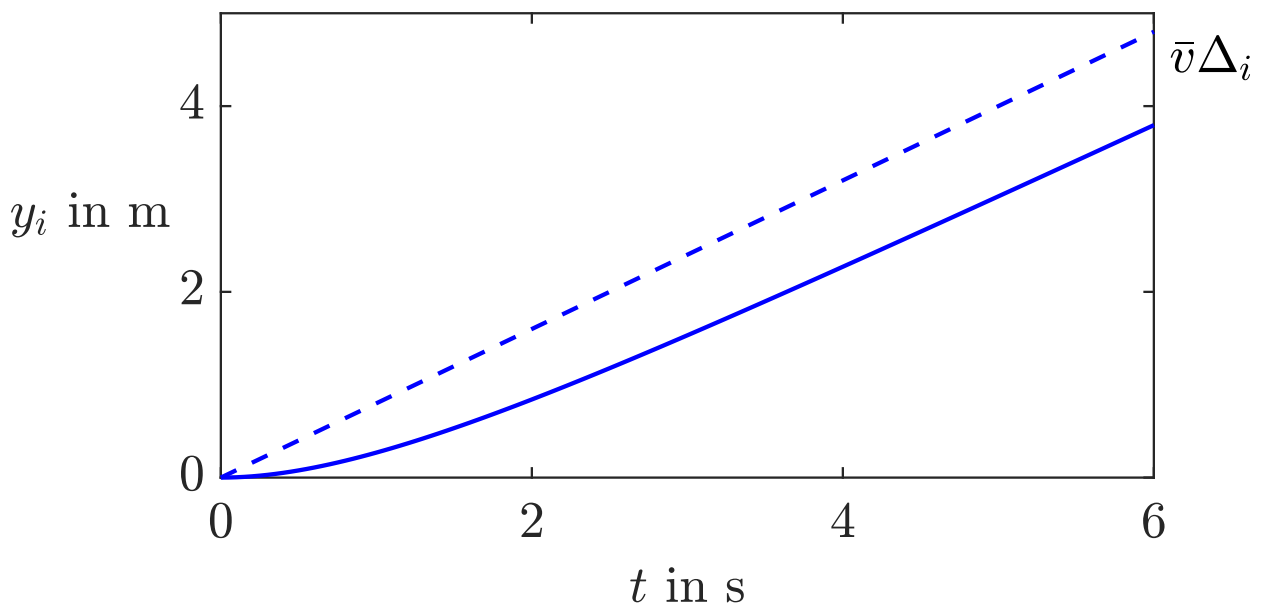


**Fig. 5: Trajectories of ten undisturbed pillars with decentralised controller (top) and with networked controller (bottom) starting in the same initial position**



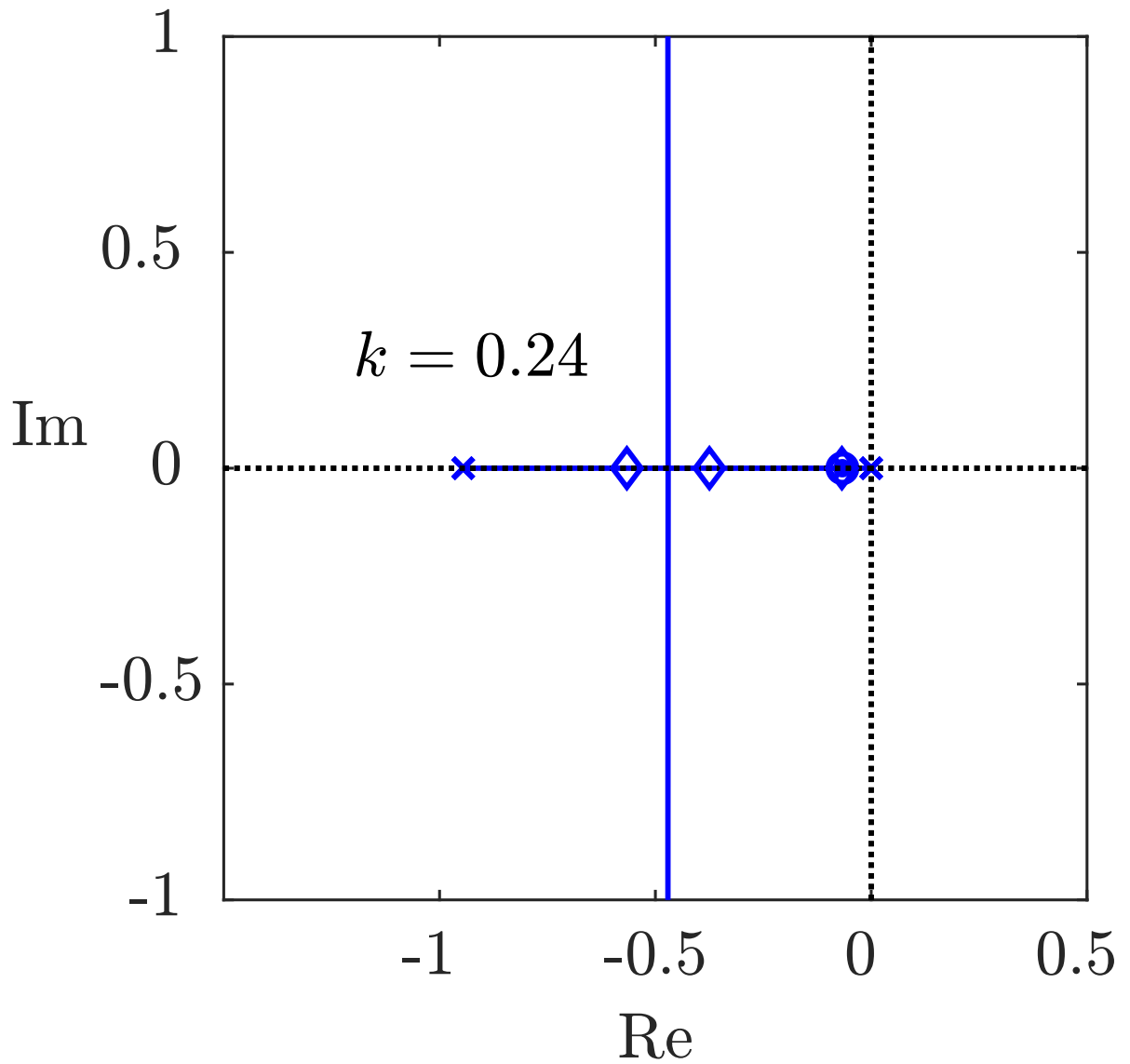
**Fig. 6: Positions of the pillars at time  $t = 40$  s**

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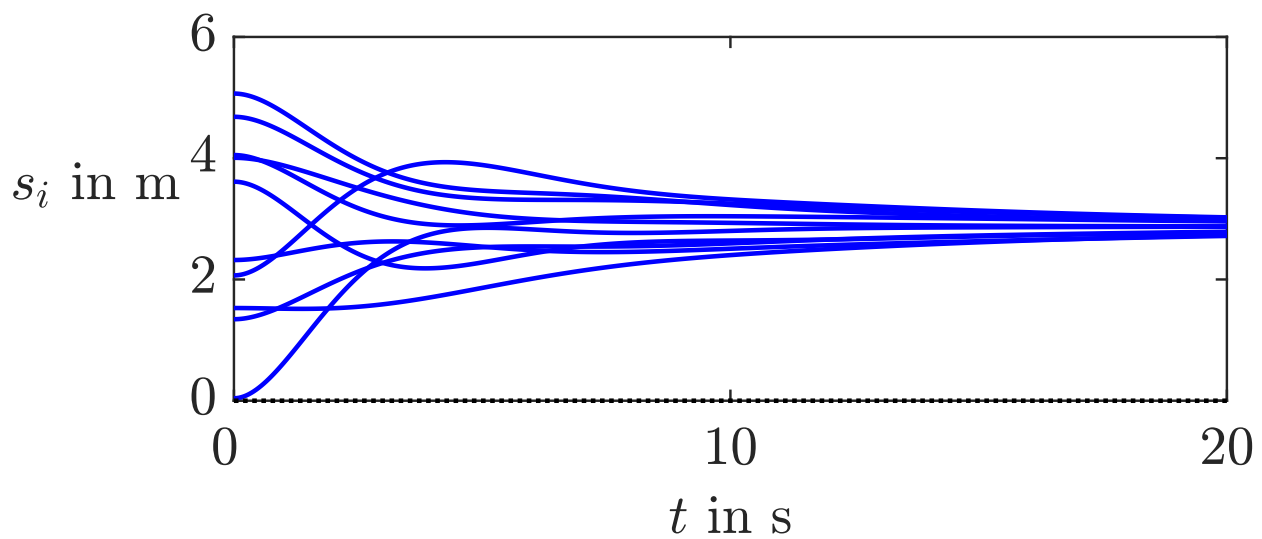
**Fig. 7: Step response of a single pillar; Required position  $s_{\text{ref}}(t)$  (---) and true position  $s_i(t)$  (—)**

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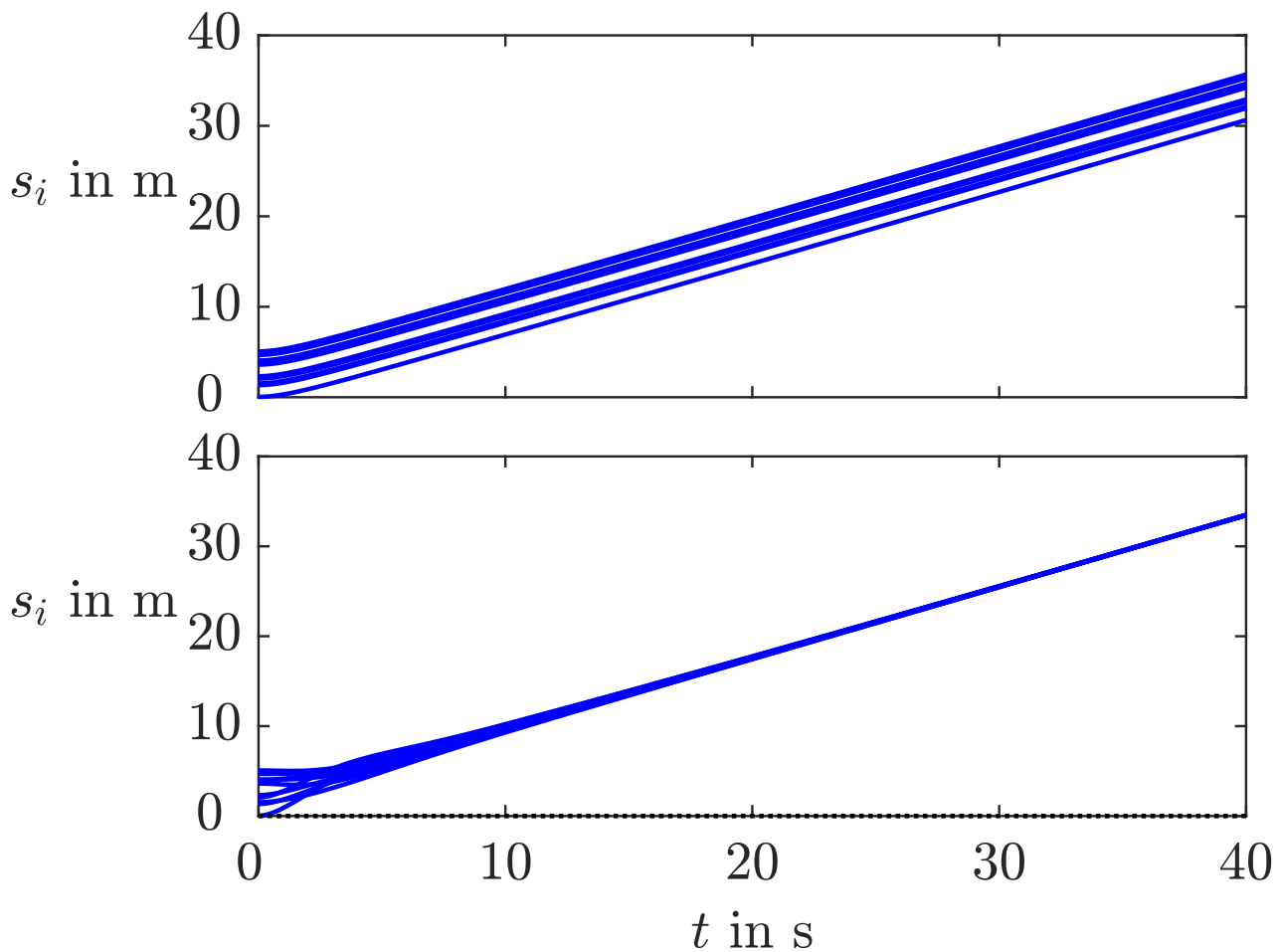
**Fig. 8:** Root locus of a single pillar with the closed-loop eigenvalues for  $k = 0.24$  marked by  $\diamond$

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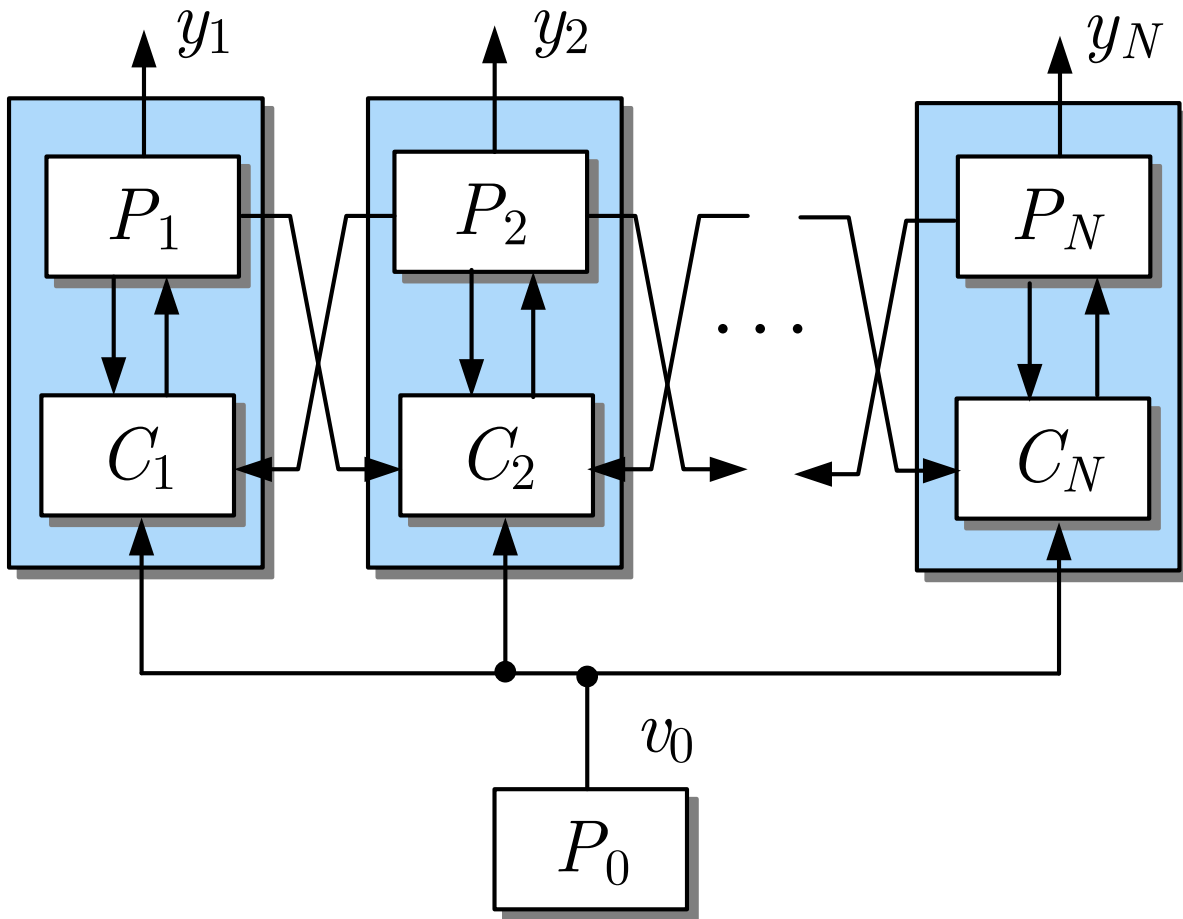
**Fig. 9: Synchronisation of the undisturbed identical pillars**

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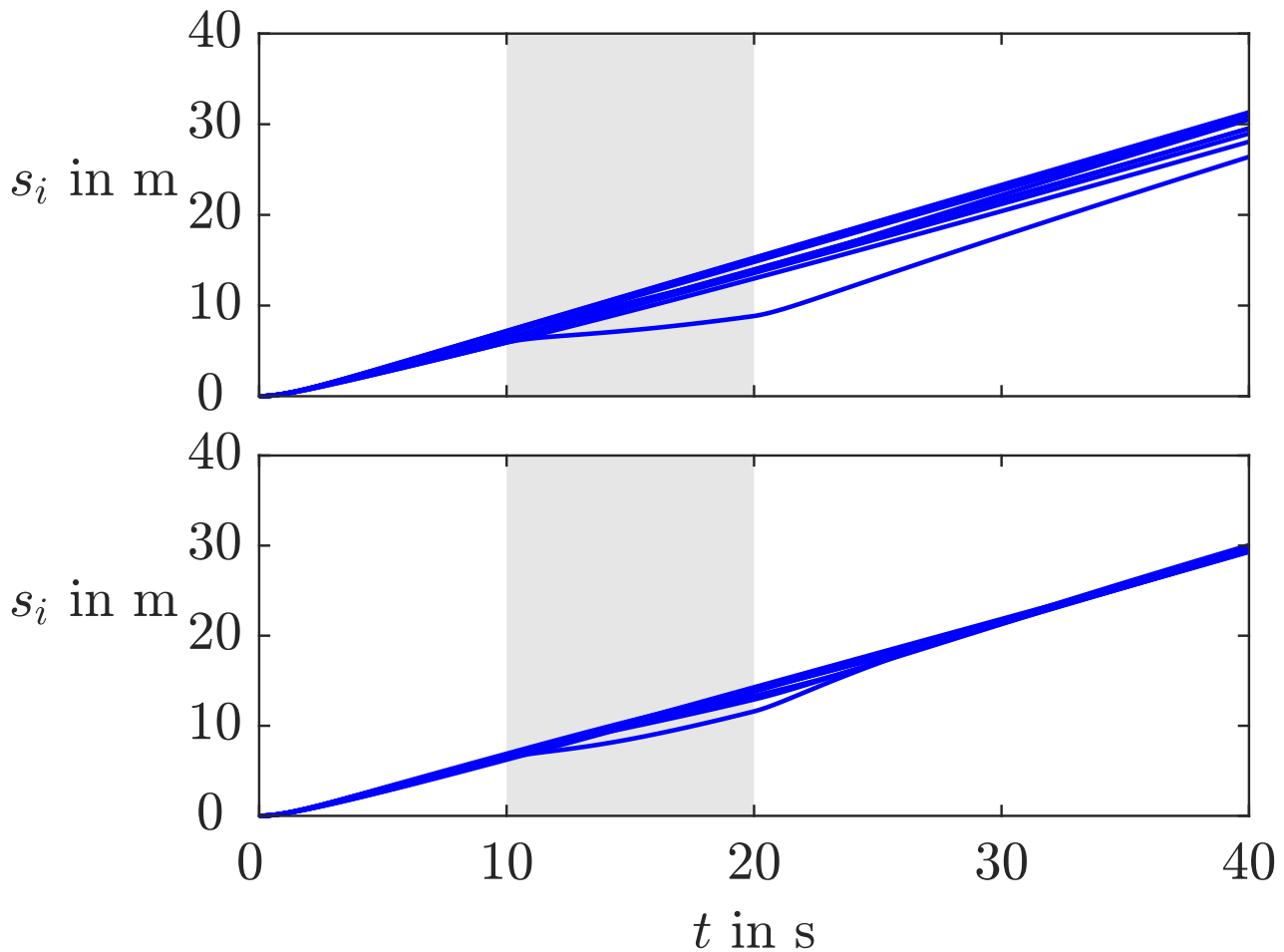
**Fig. 10: Trajectories of ten undisturbed identical pillars with decentralised controller (top) and with networked controller (bottom)**

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**Fig. 11: Irrigation system with networked controller**

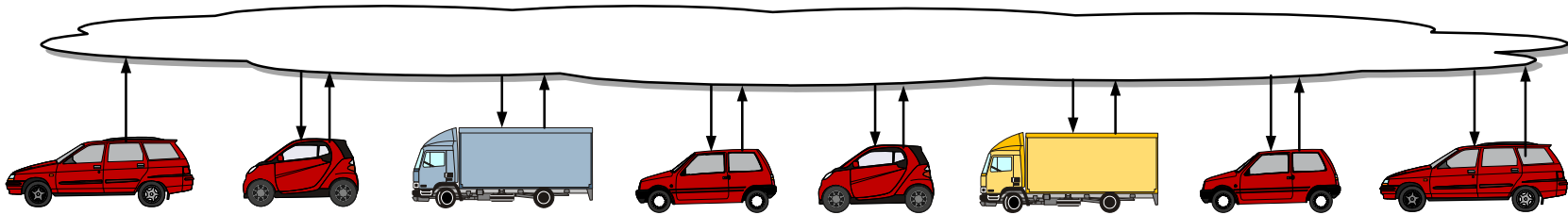
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**Fig. 12: Behaviour of the disturbed irrigation system with networked controller**

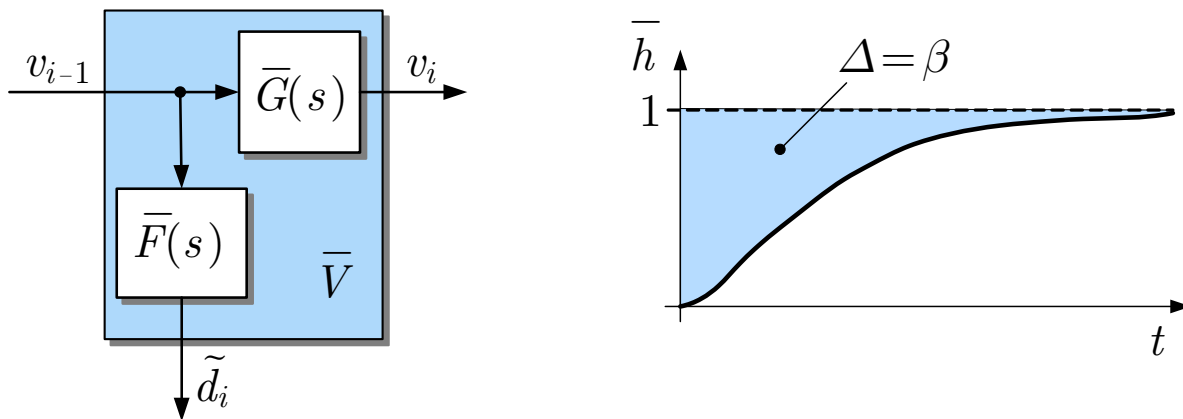
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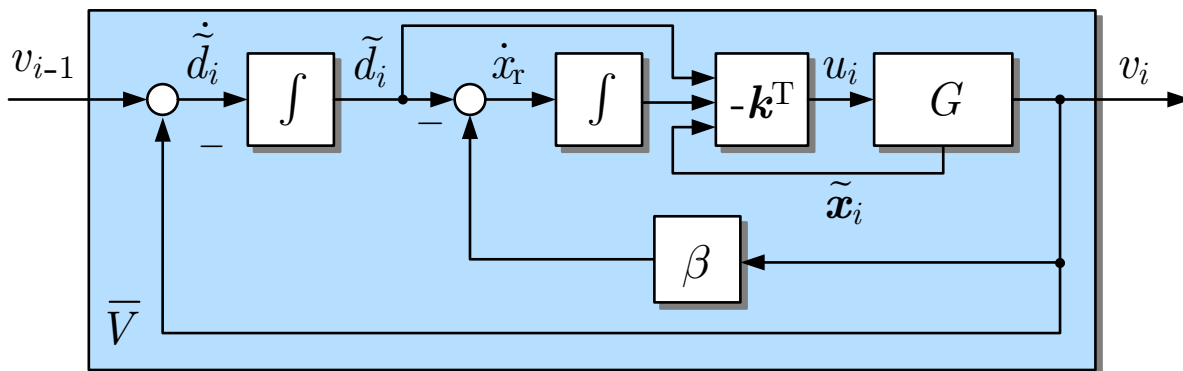
**Fig. 0. Vehicle platoon**

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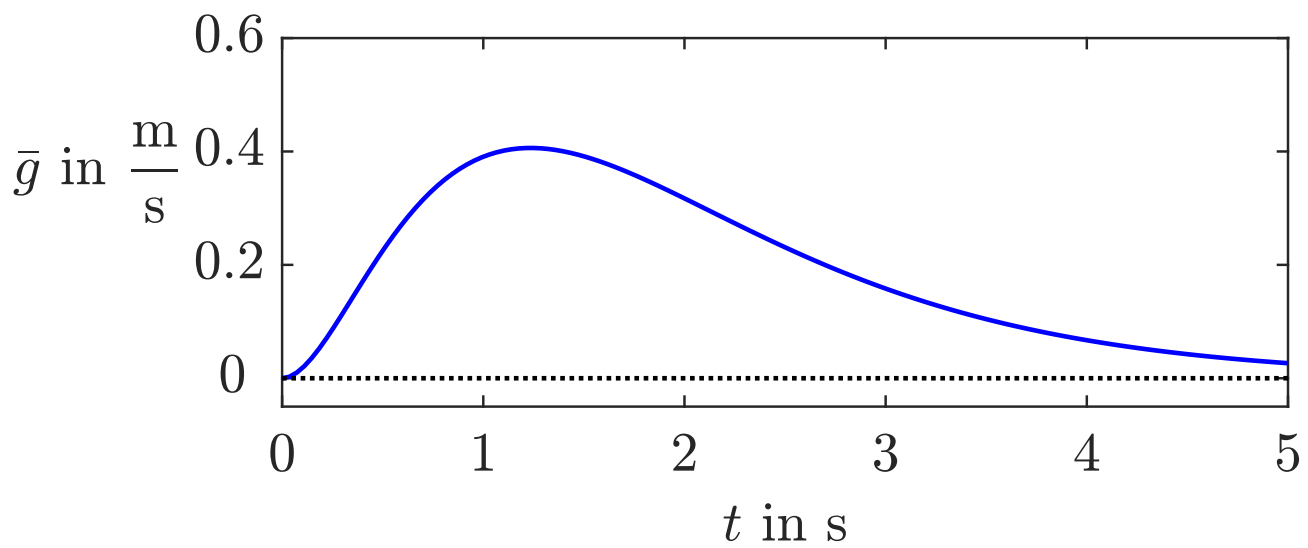
**Fig. 1: Controlled vehicle**

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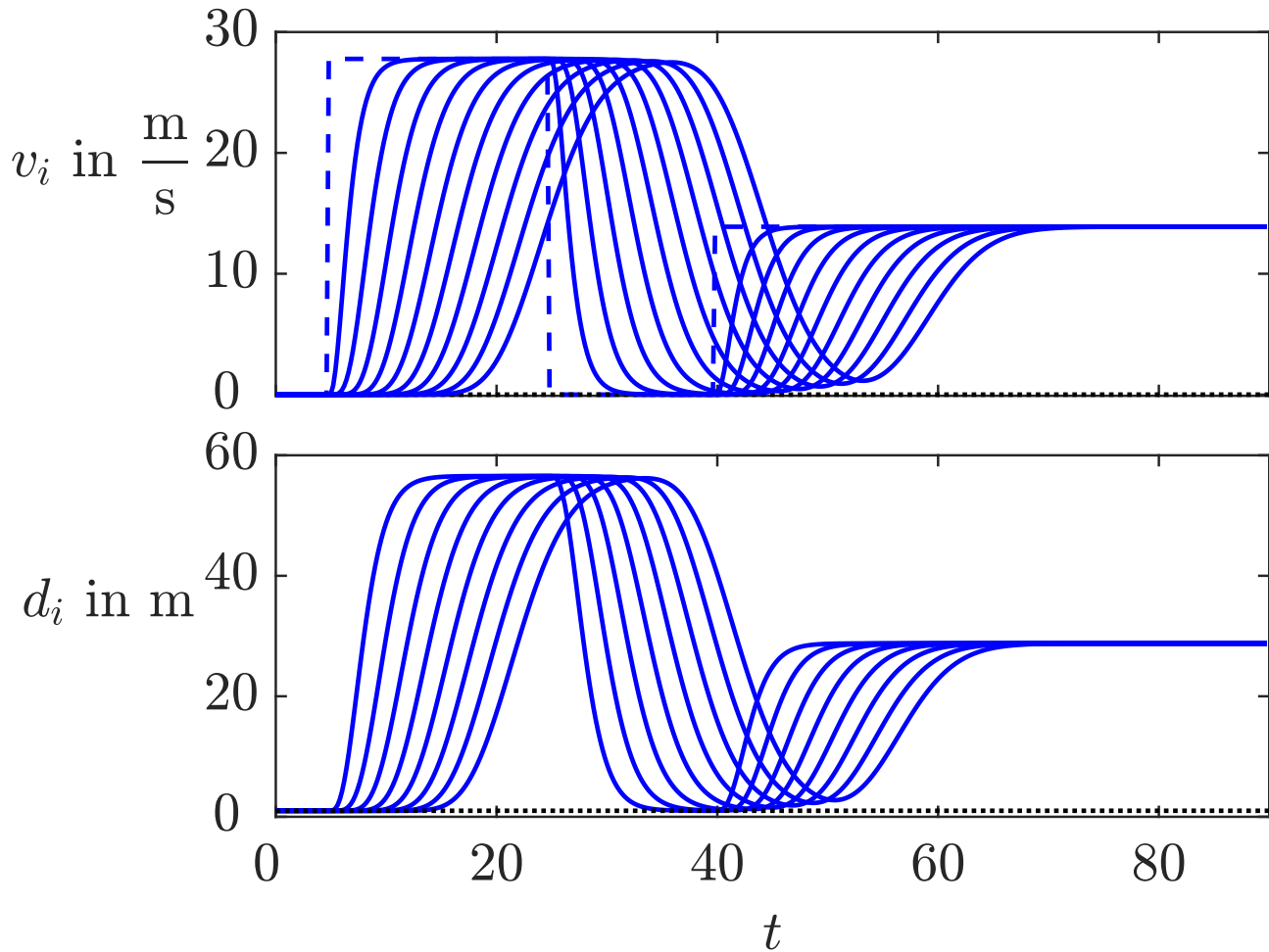
**Fig. 2: Controlled vehicle**

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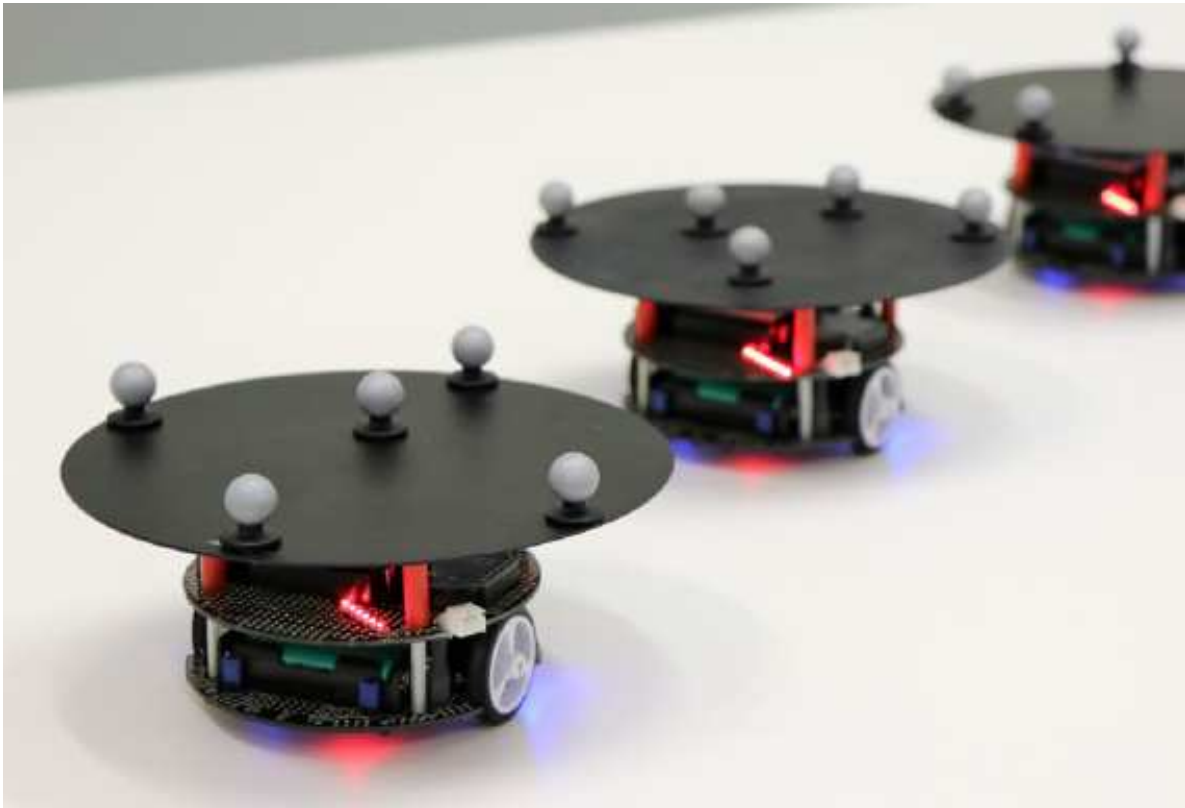
**Fig. 3: Impulse response of the controlled vehicle**

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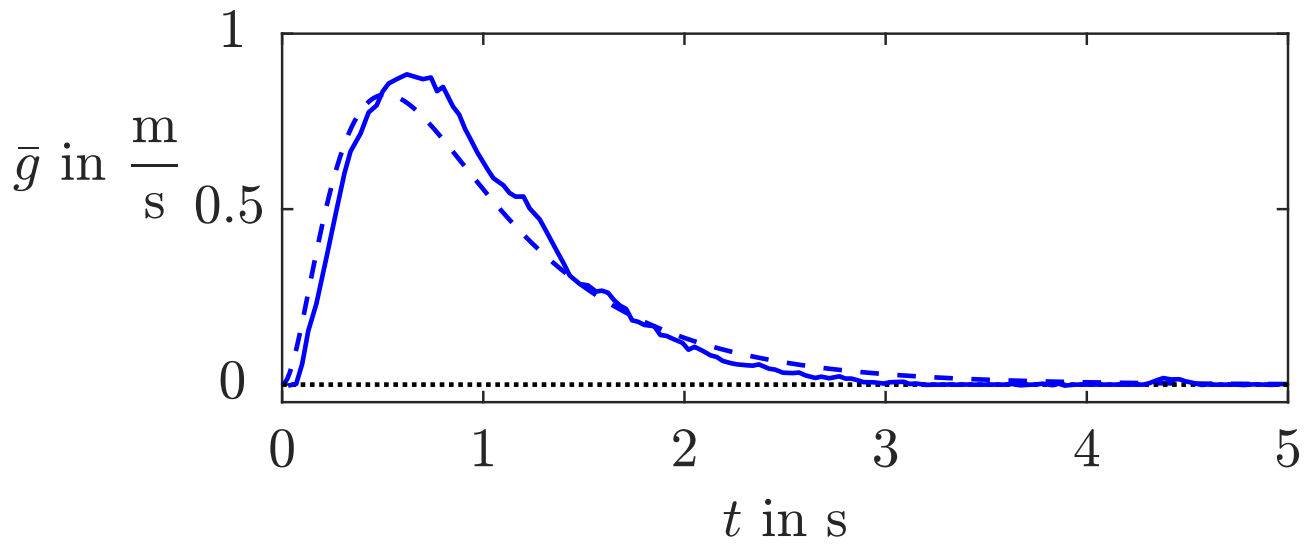
**Fig. 4: Behaviour of a platoon of ten vehicles**

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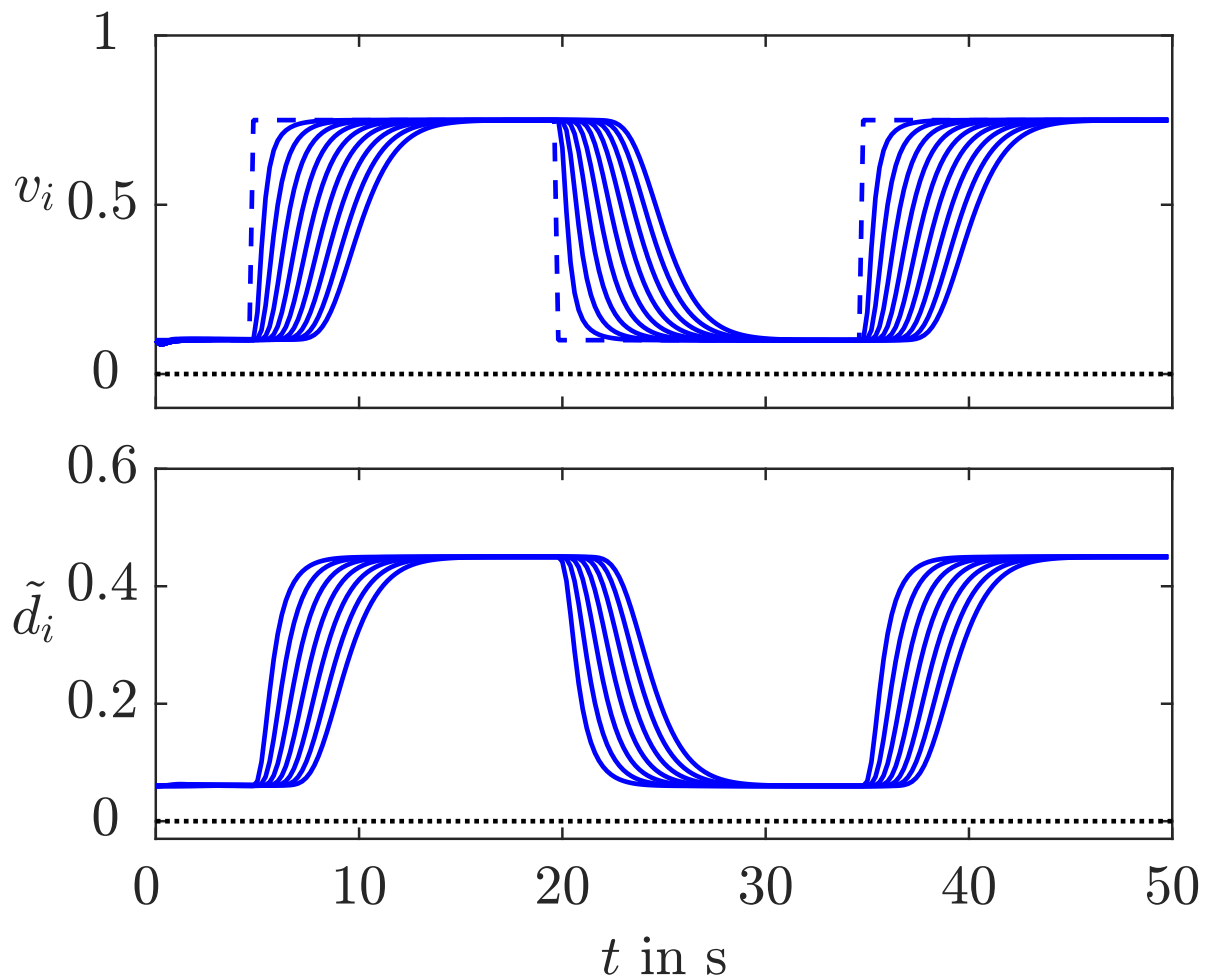
**Fig. 5: Robots used for the experiments**

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**Fig. 6: Impulse response of the model of the controlled vehicle (- - -) and experimental data (—)**

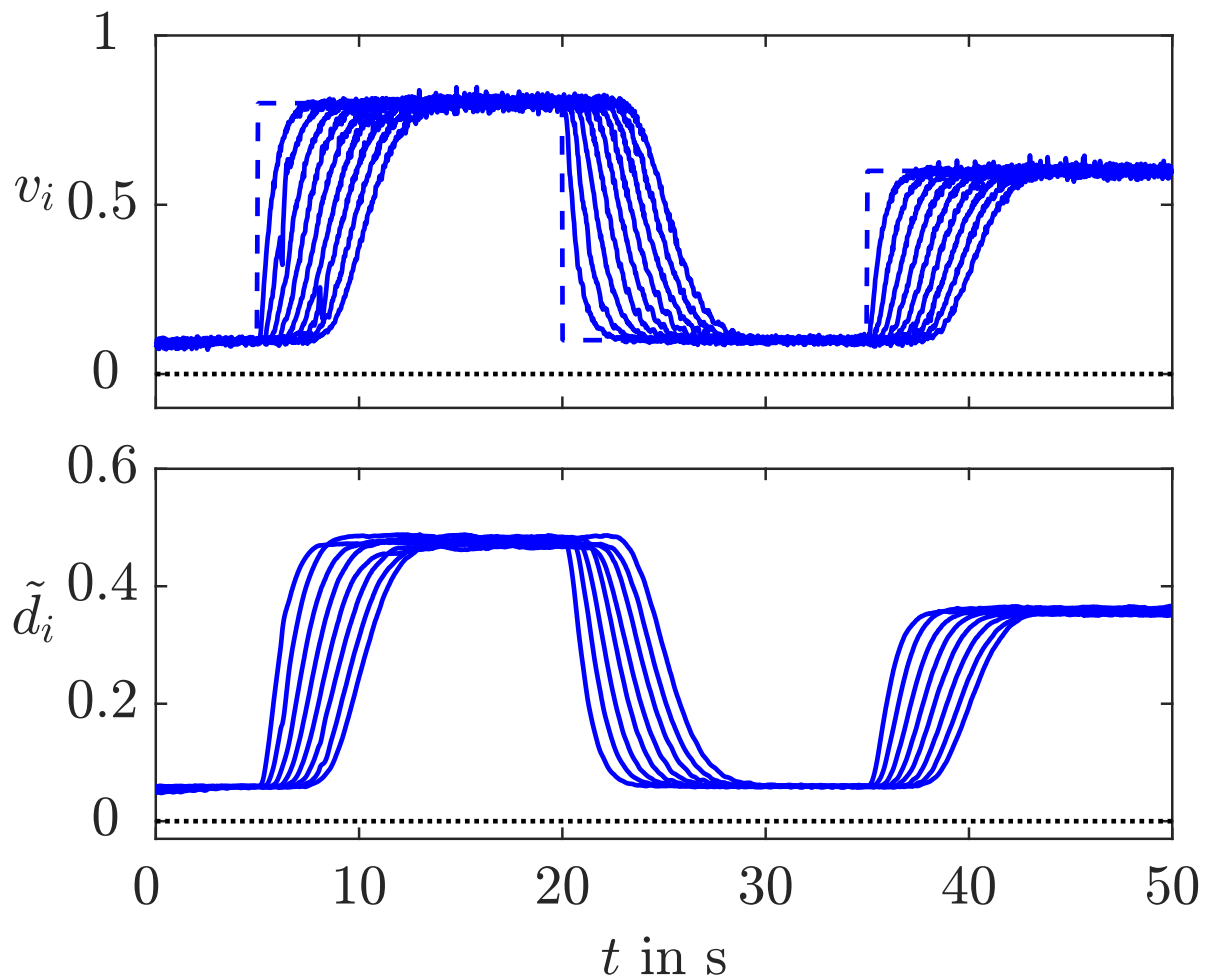
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**Fig. 7: Behaviour of a platoon with nine robots:  
Simulation results**

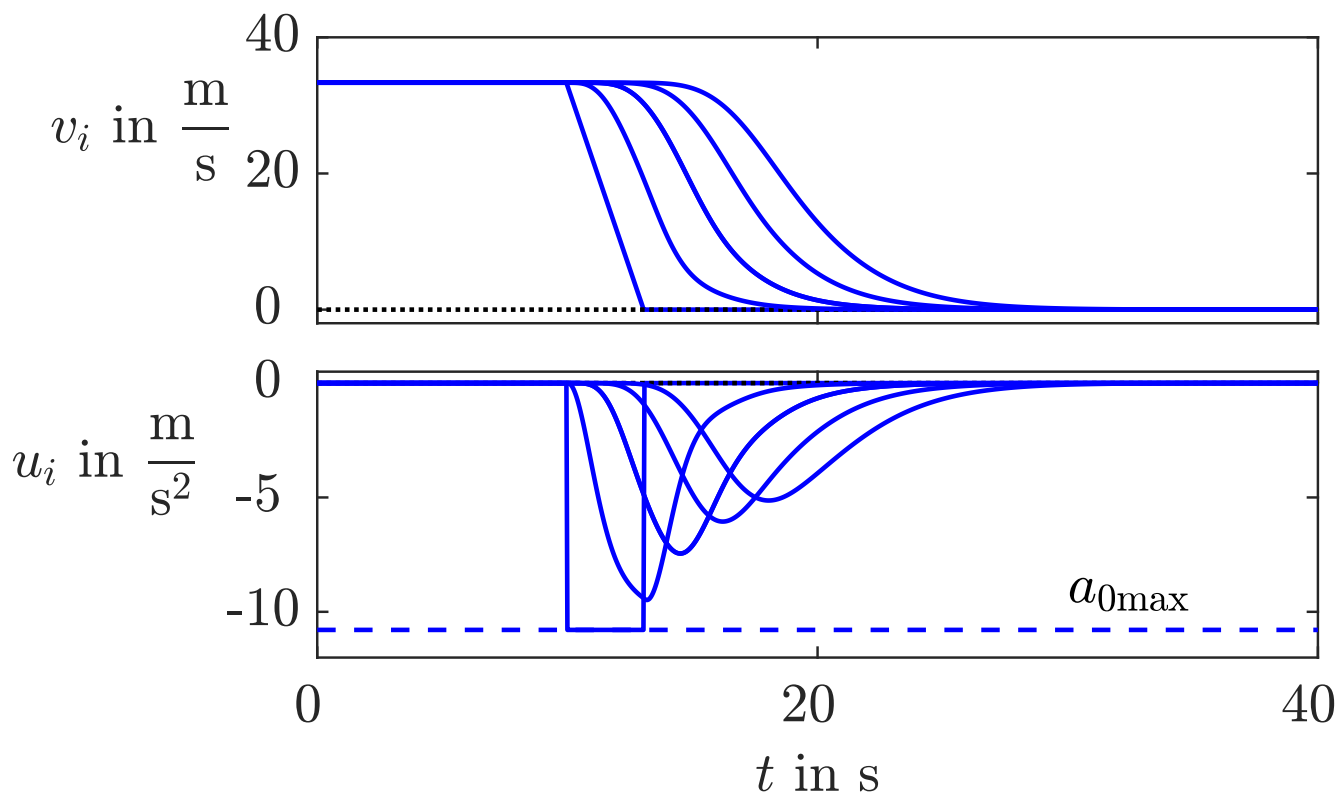
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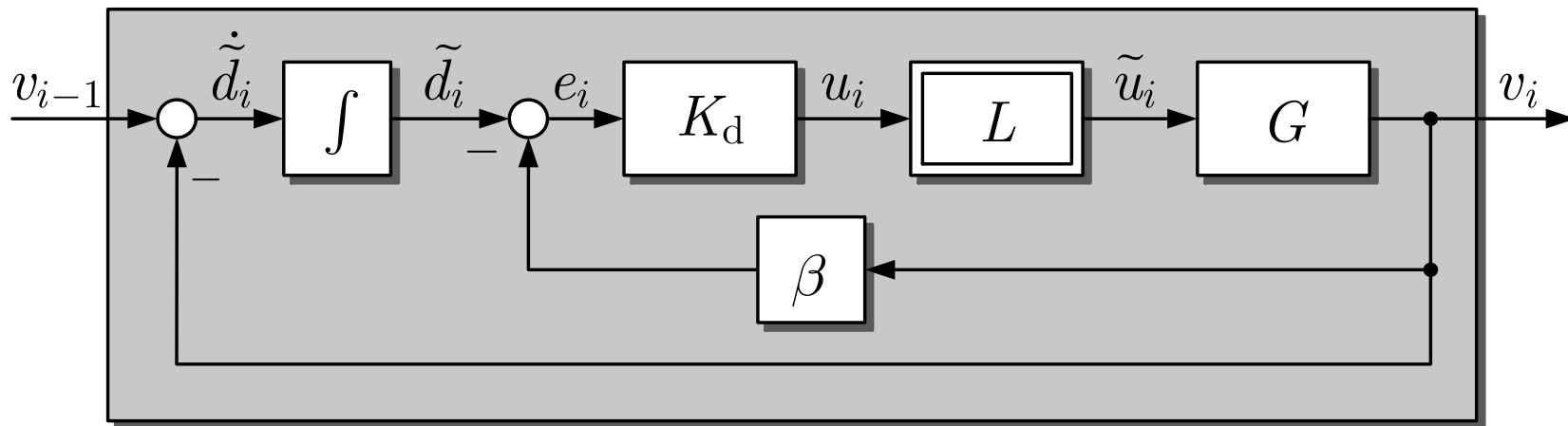
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Experimental results**

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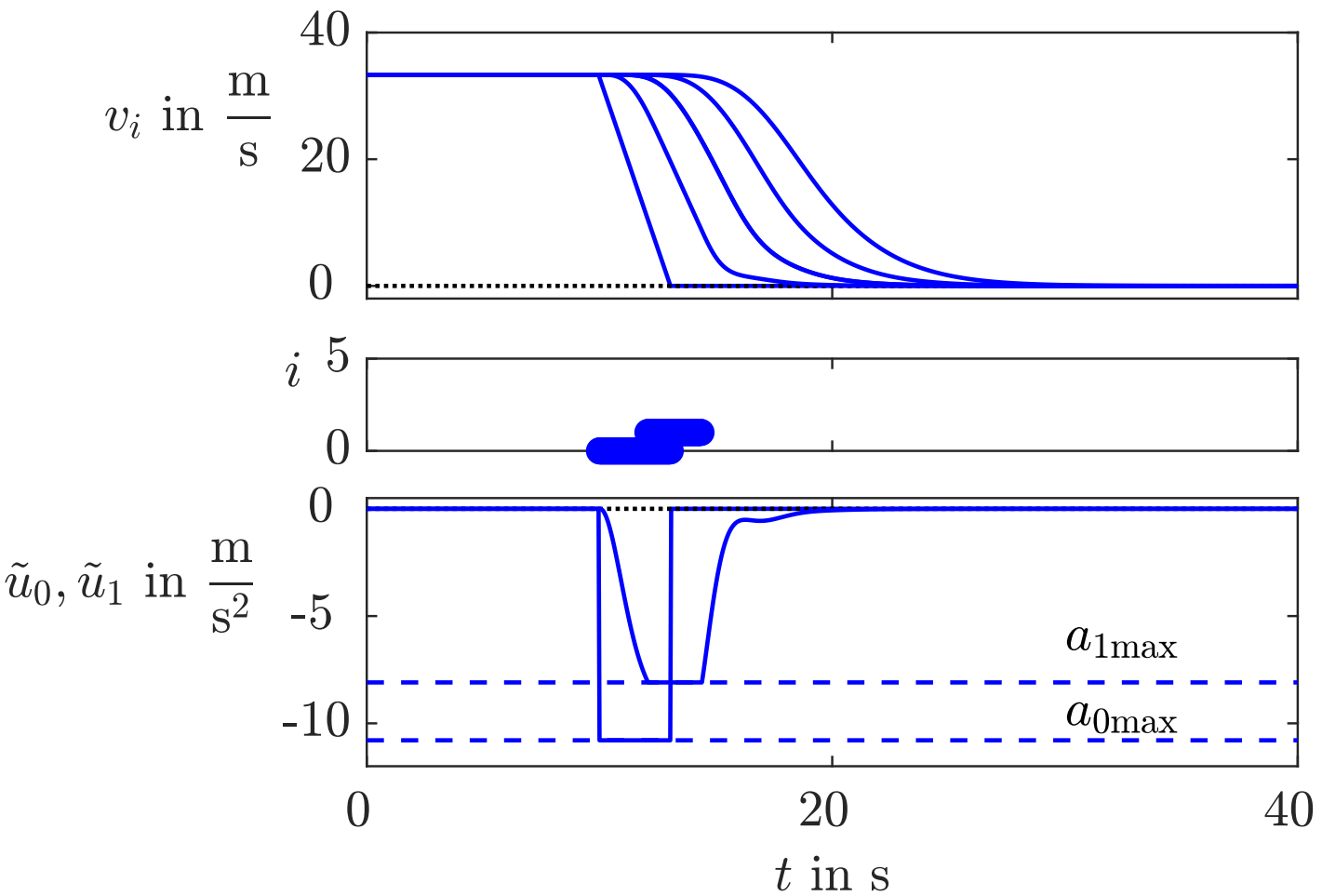
**Fig. 8: Behaviour of the linear vehicle platoon**

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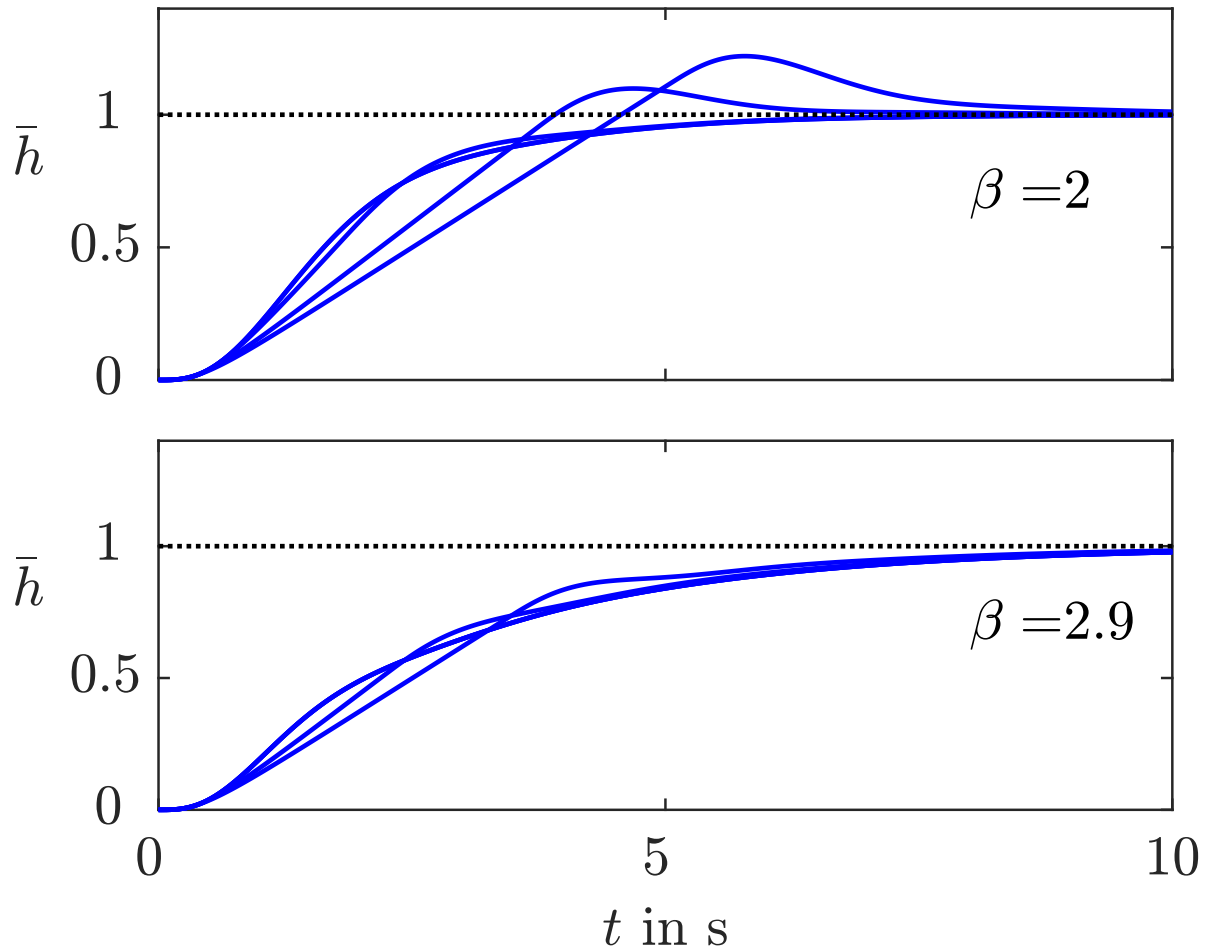
**Fig. 9. Vehicle model with nonlinearity to represent the limited acceleration**

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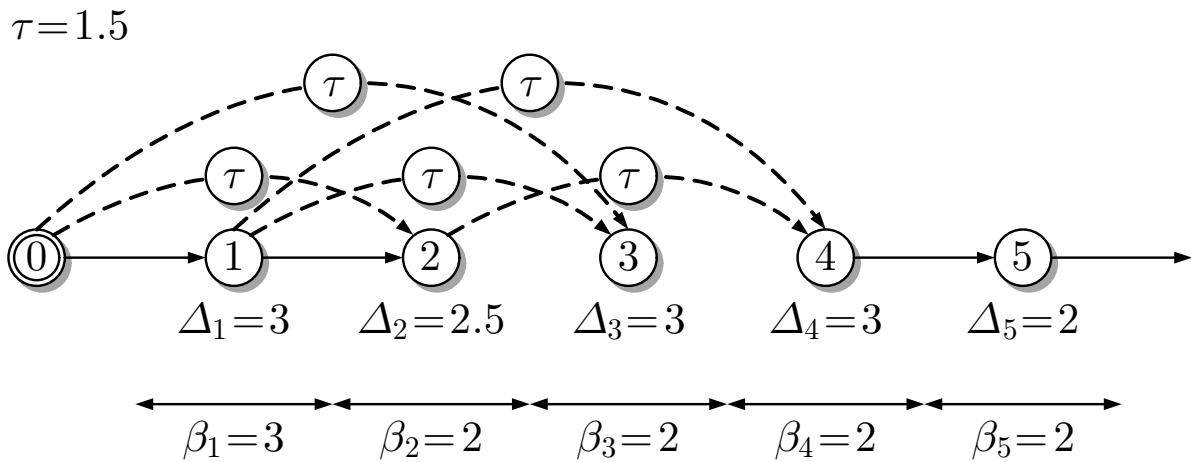
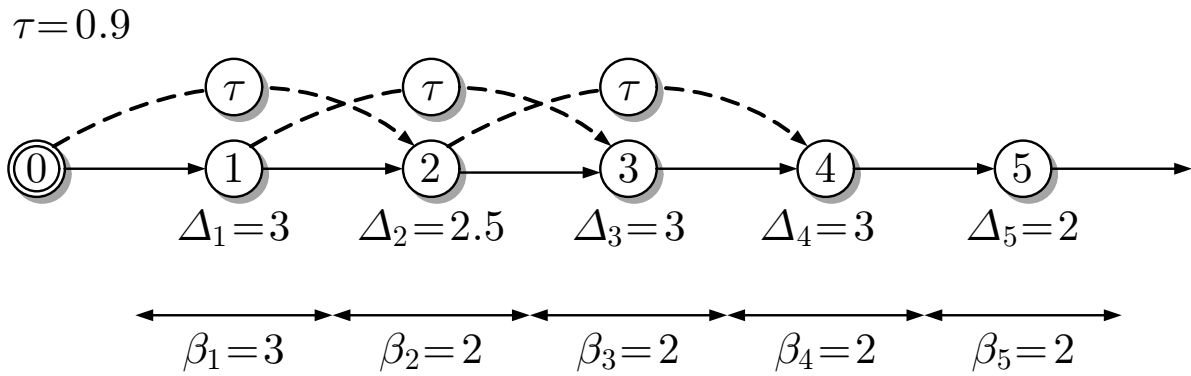
**Fig. 10: Braking manoeuvre with nonlinear vehicles**

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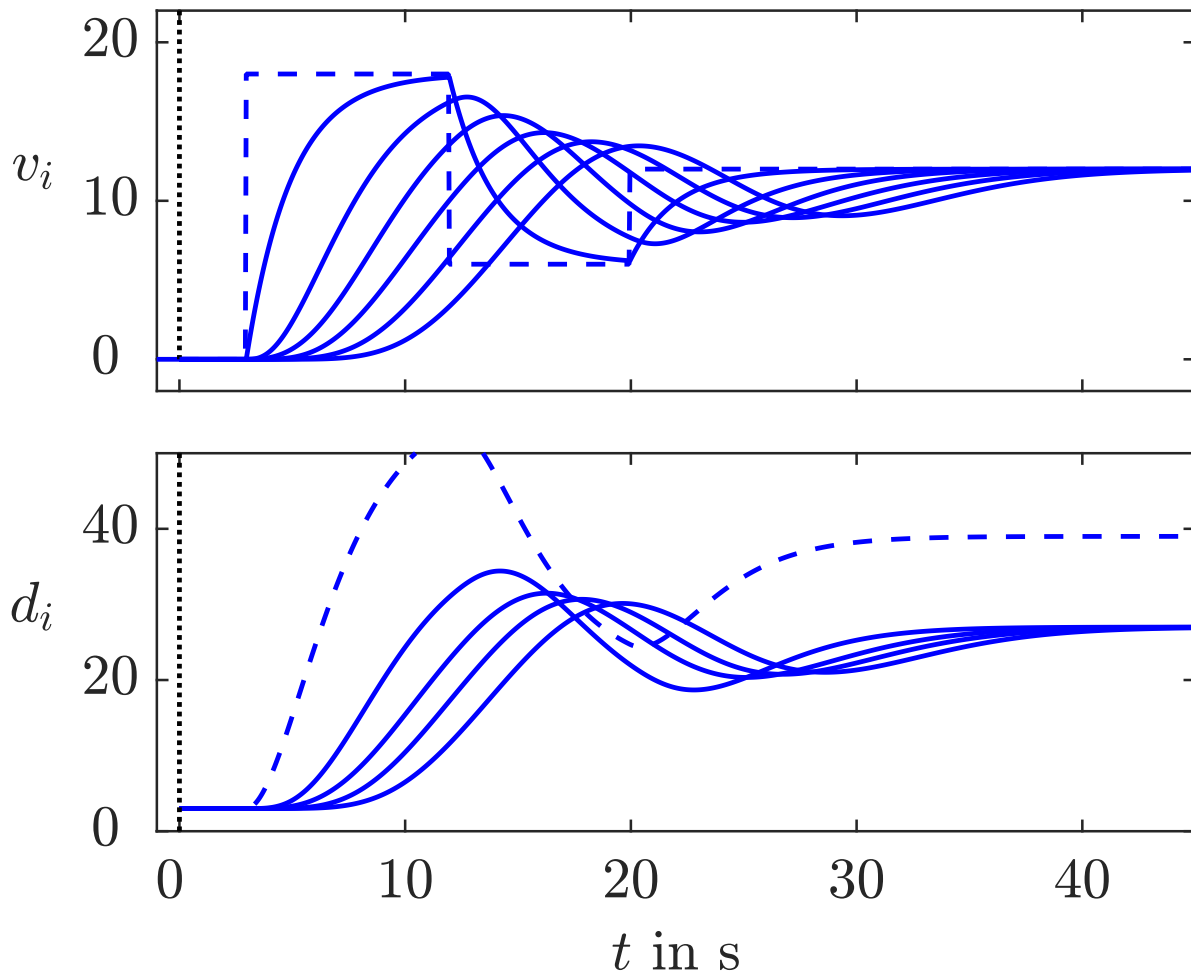
**Fig. 11: Normalised response of the controlled vehicle to stepwise changes of the local reference velocity  $v_{si}(t)$**

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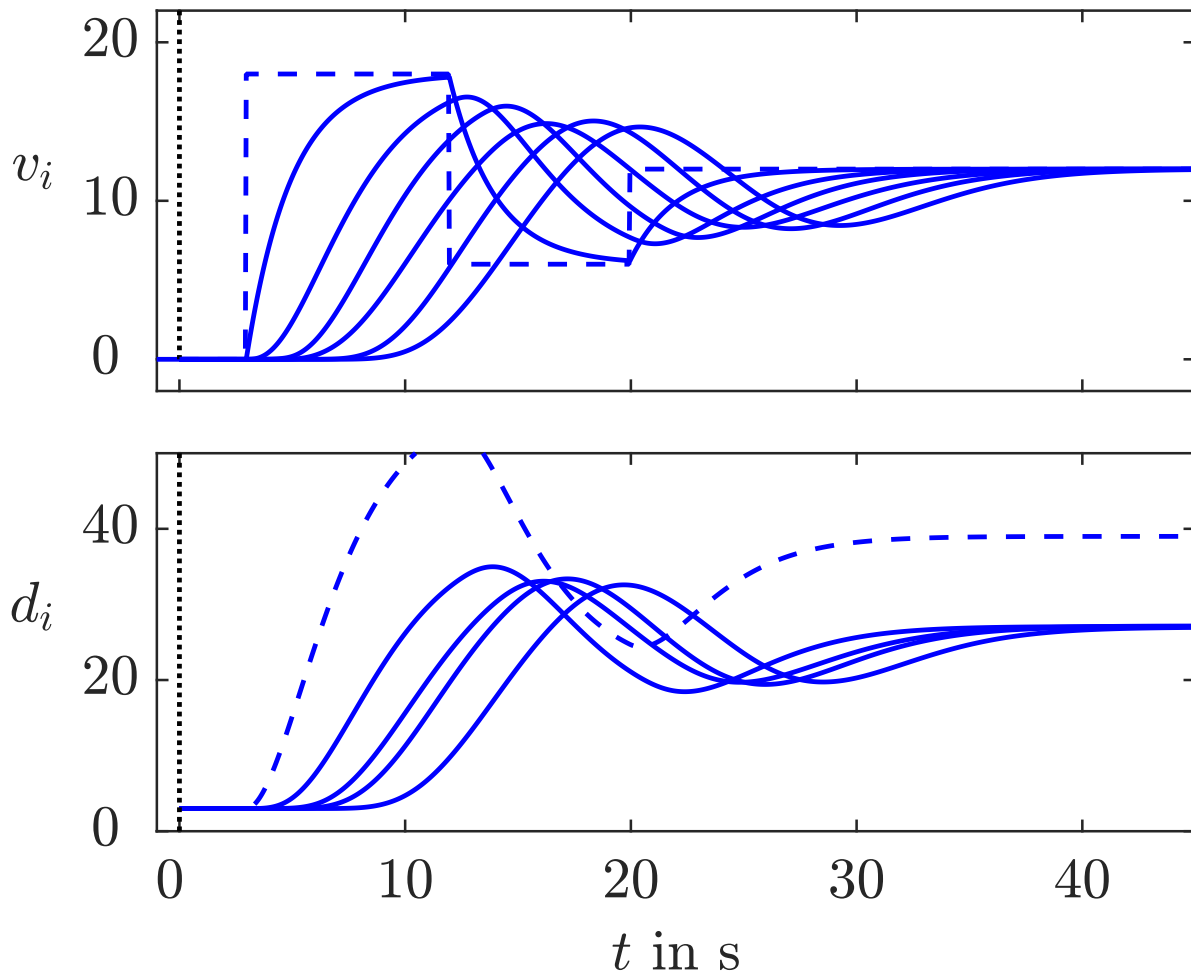
**Fig. 12: Communication graph of the CACC with time delay**

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**Fig. 13: Platoon with CACC without transmission delay**

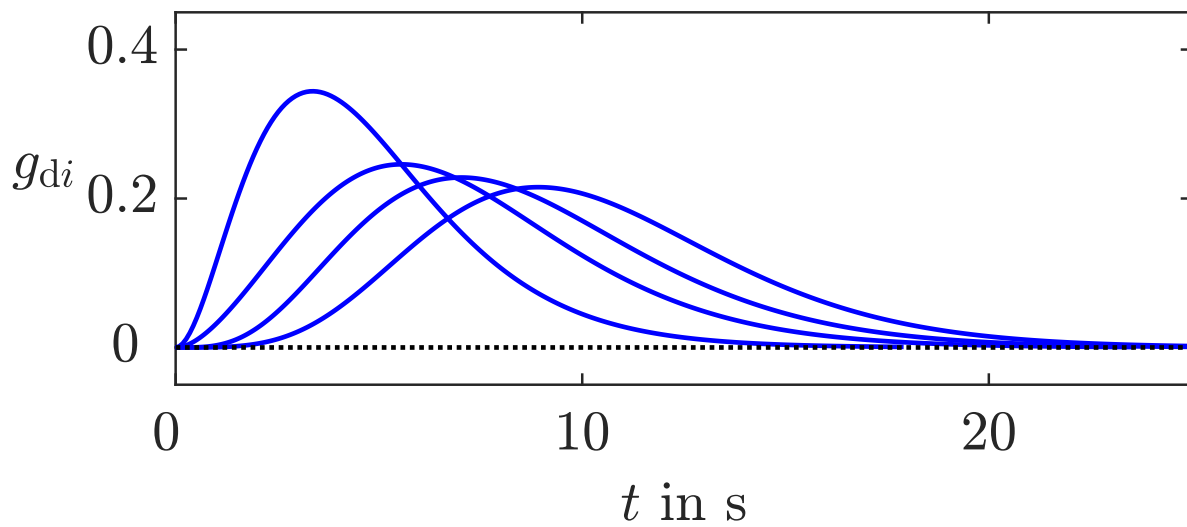
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**Fig. 13: Platoon with CACC with transmission delay  $\tau = 1.5$  s**

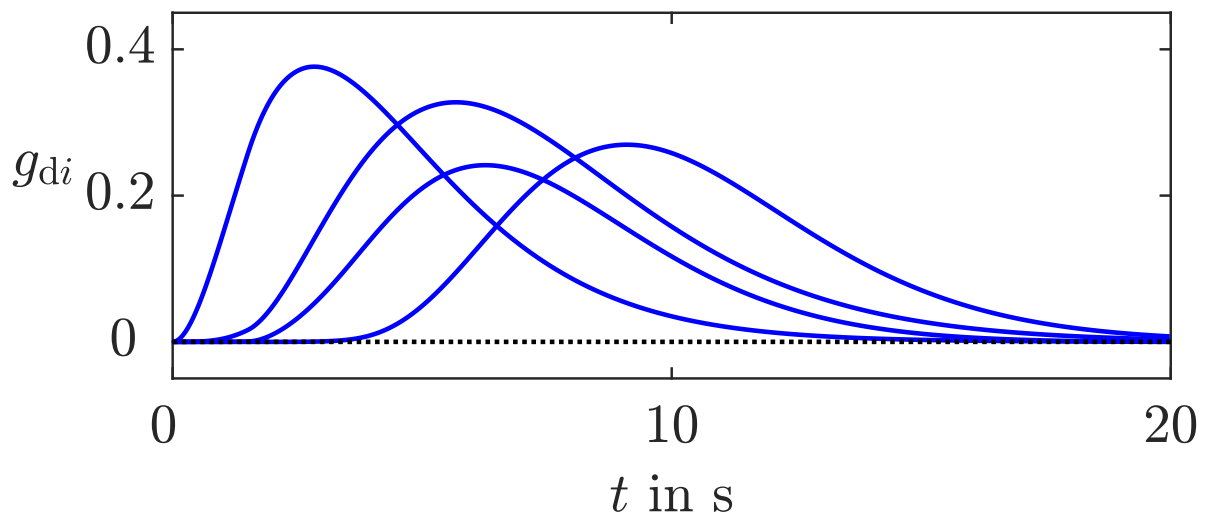
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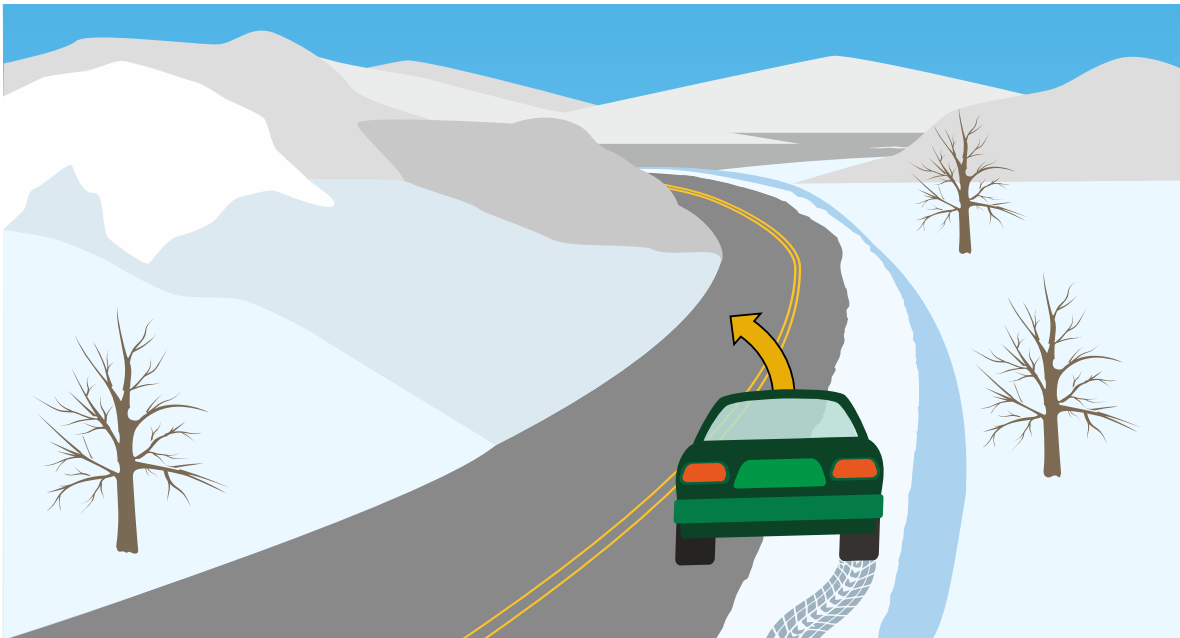
**Fig. 14: Collision avoidance test without transmission delay**

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**Fig. 14: Collision avoidance test with transmission delay  $\tau = 0.9$  s**

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**Fig. 0:**  $\mu$ -split braking

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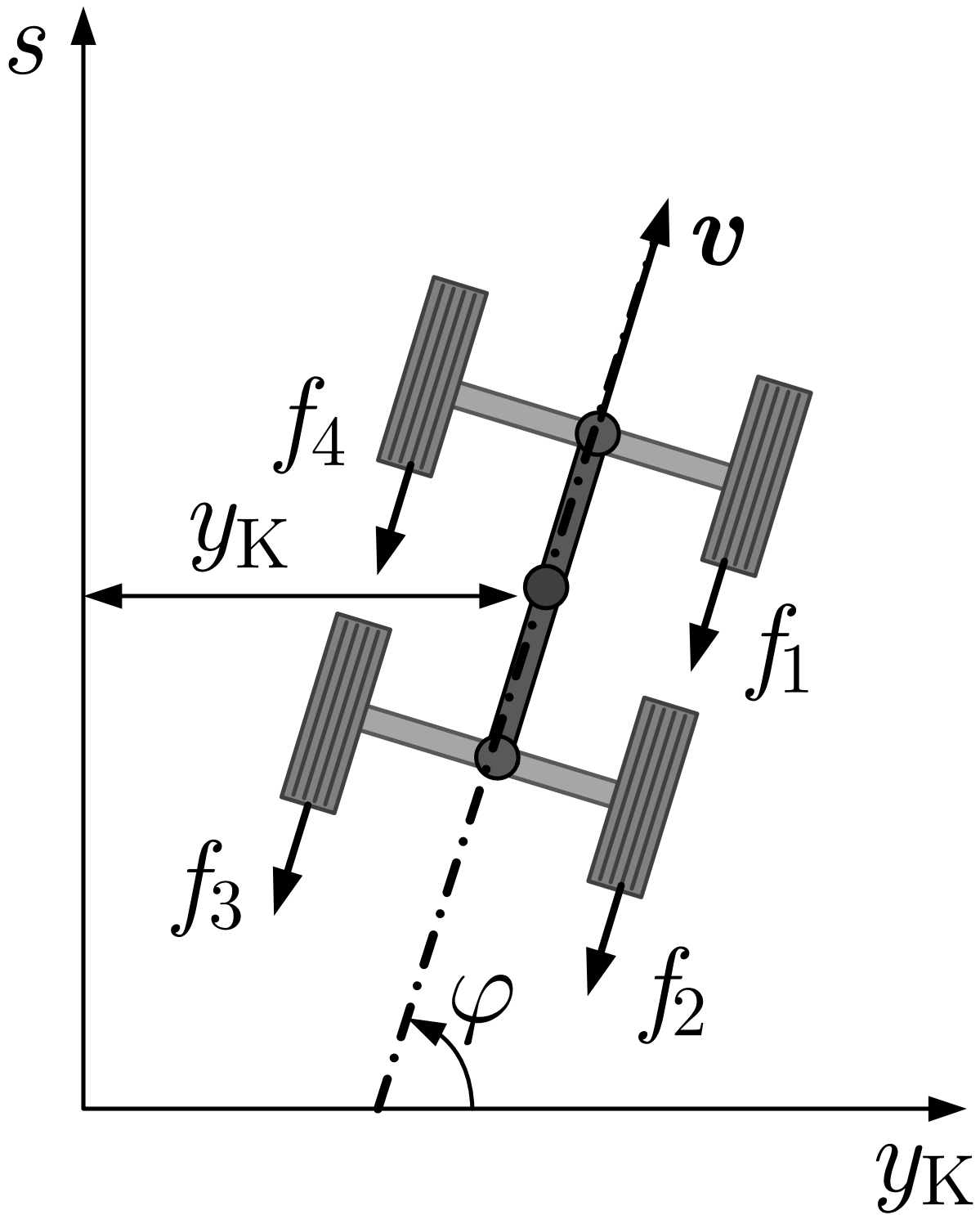
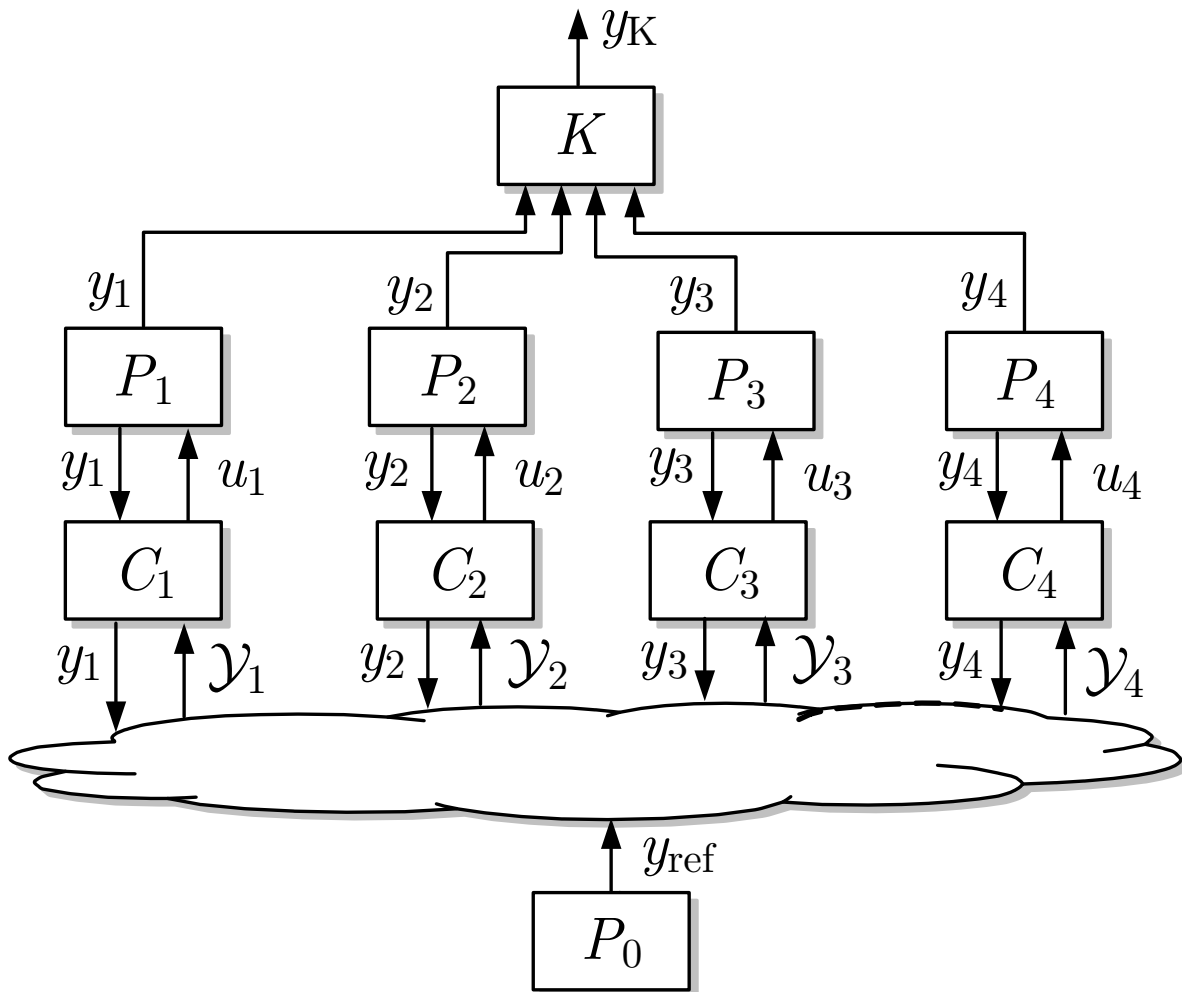
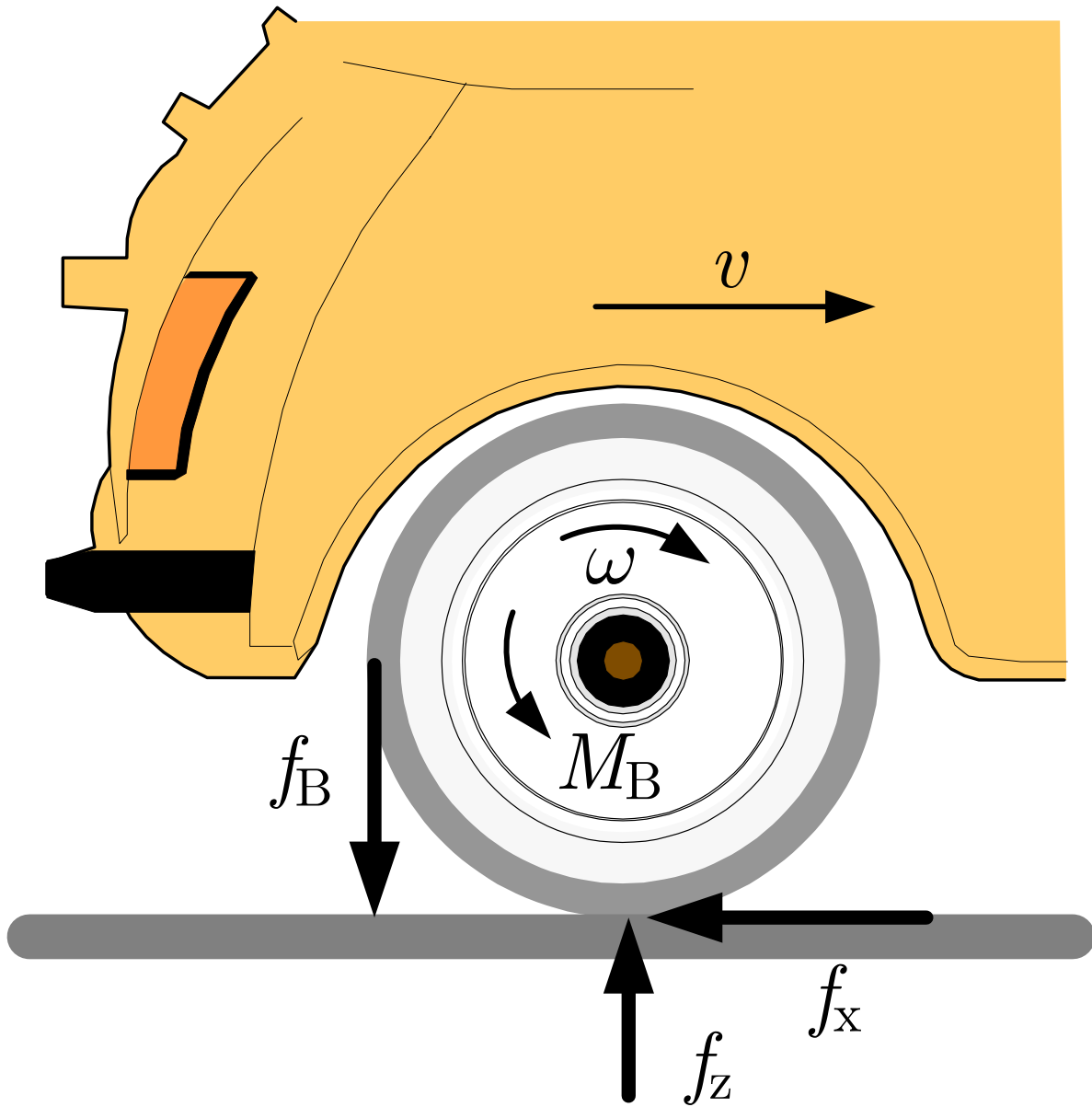


Fig. 1: Vehicle model



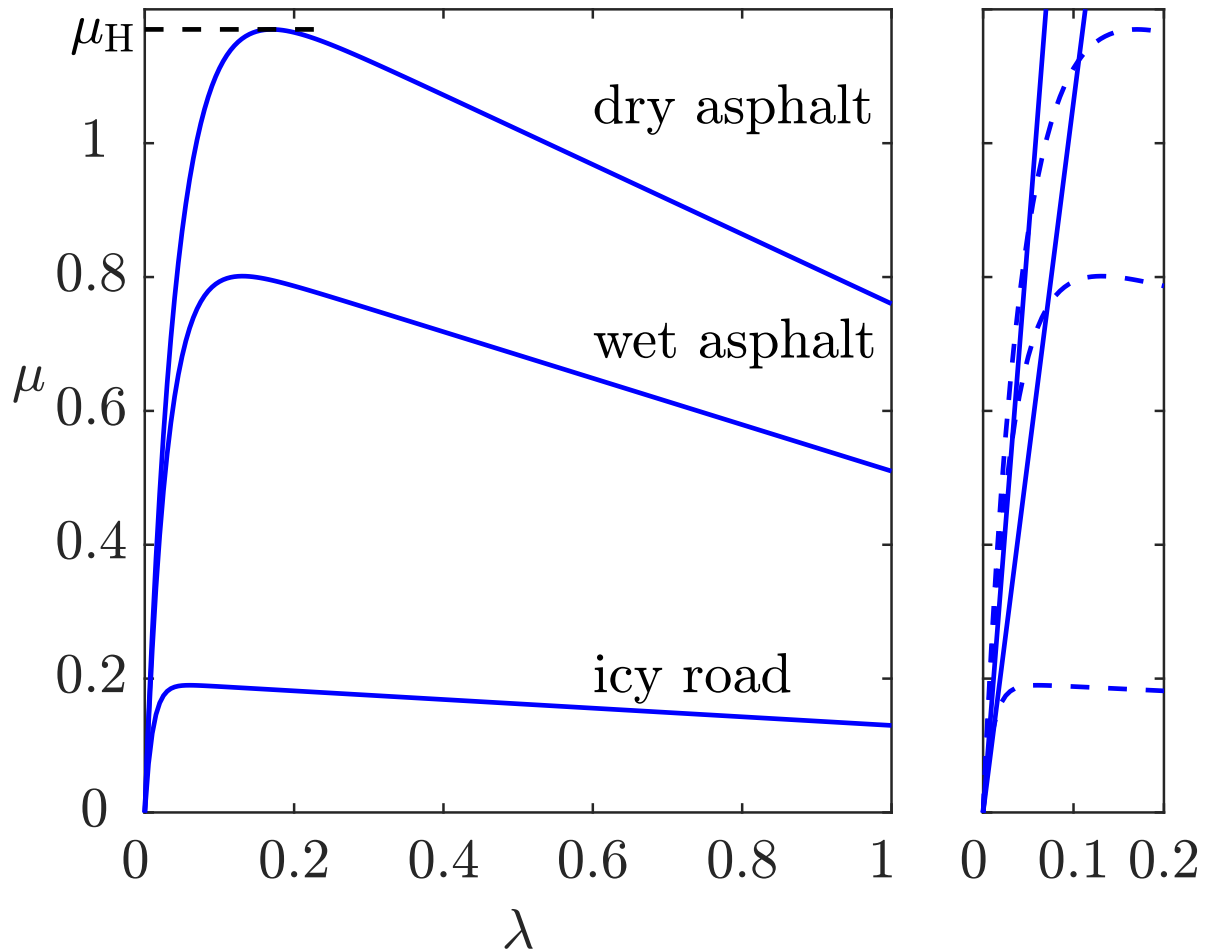
**Fig. 2:** Block diagram of the networked vehicle controller with the additional block  $K$  that generates the performance output  $y_K(t)$

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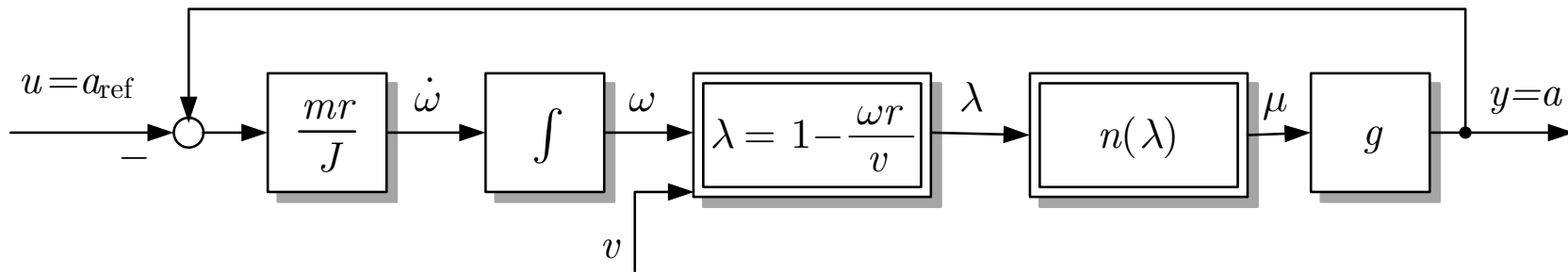


**Fig. 3:** Torques and forces acting on a wheel

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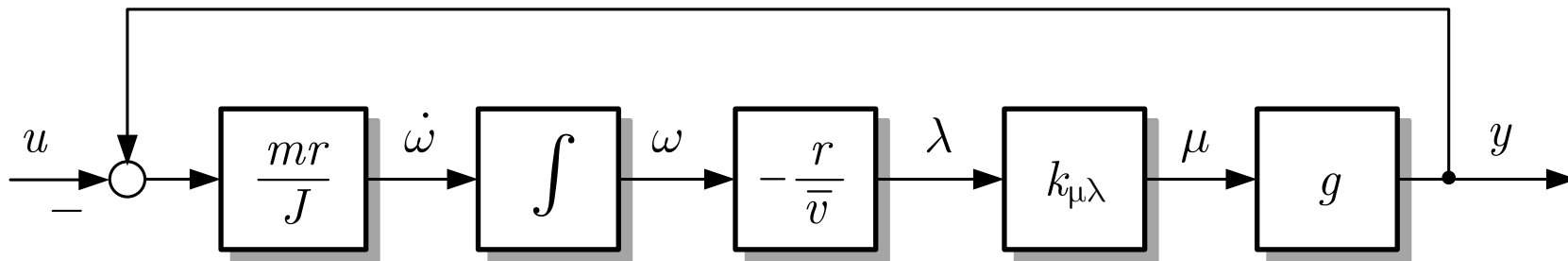
**Fig. 4: Friction-slip curve (left) and its approximation (4) (right)**



**Fig. 5. Nonlinear model of the  $i$ -th wheel**

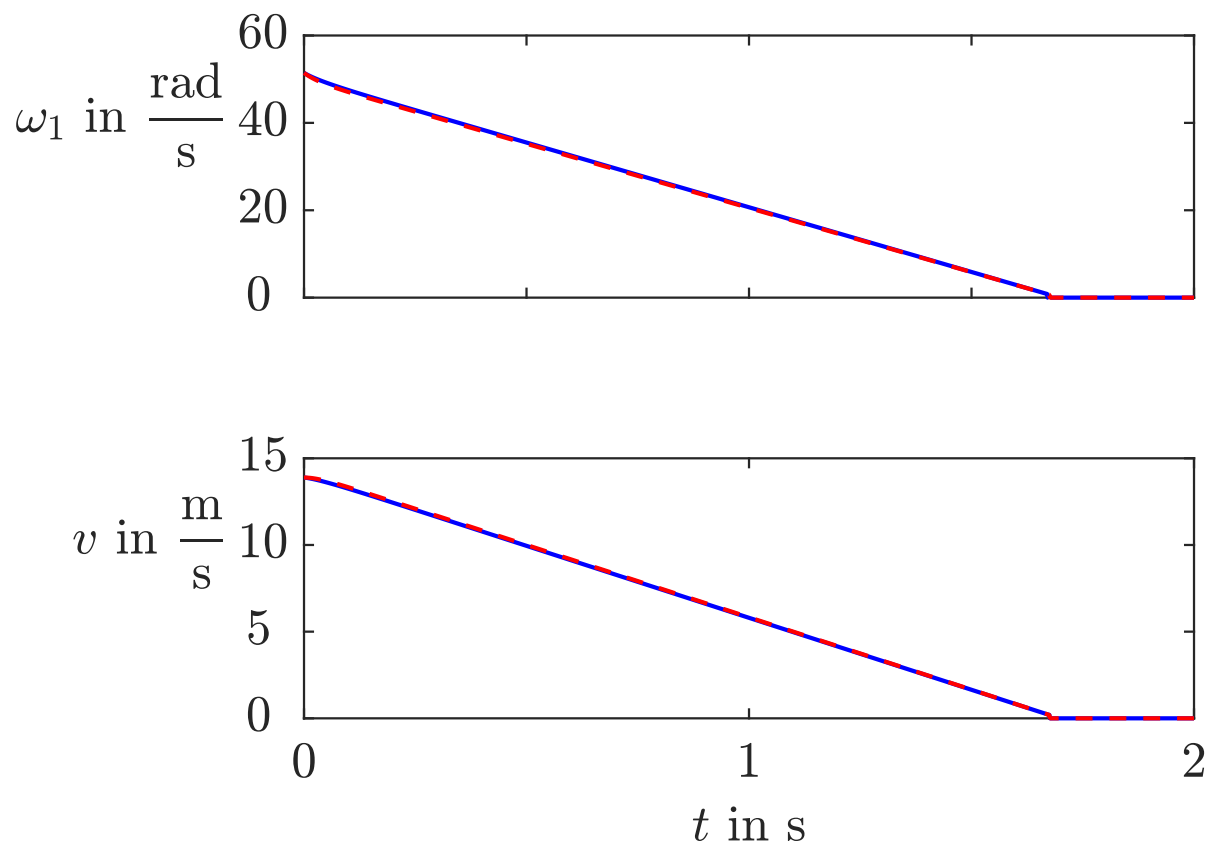
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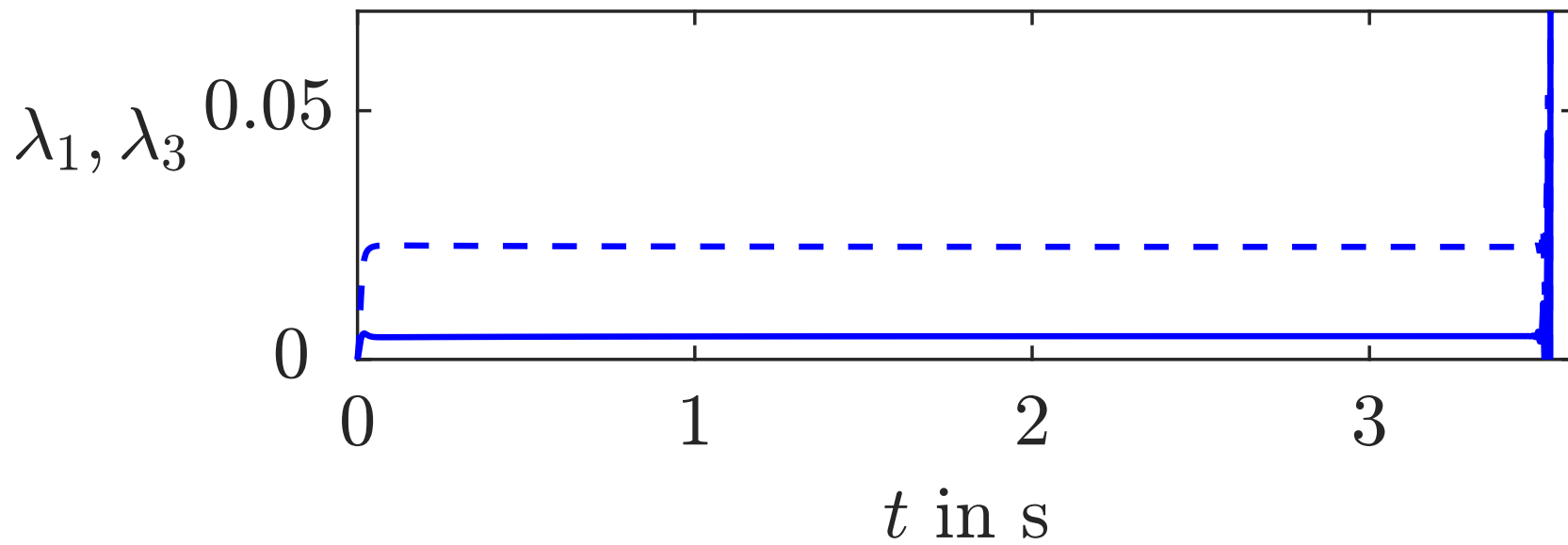
**Fig. 6.** Linearised model of the  $i$ -th wheel

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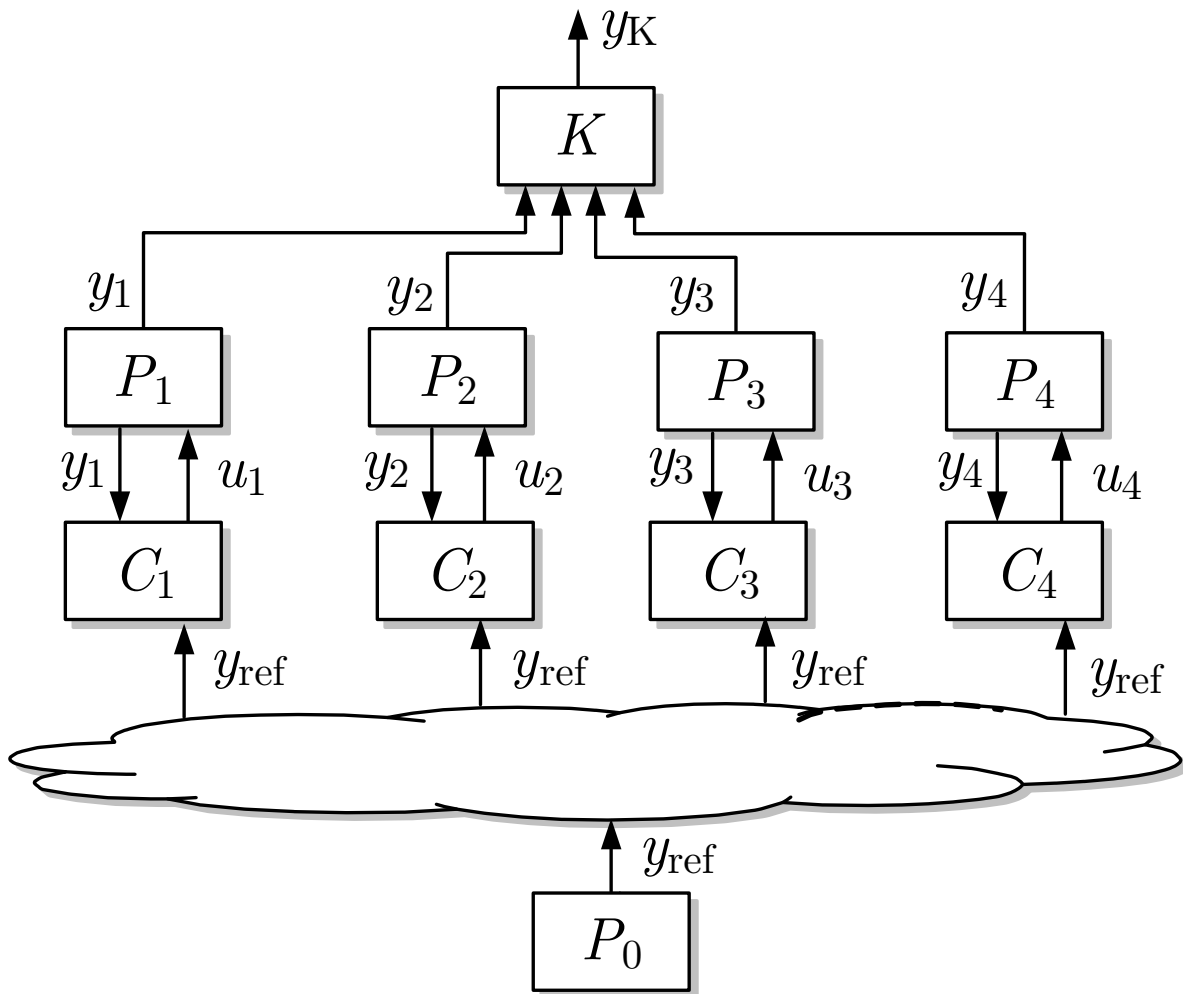
**Fig. 7: Angular velocity of the four wheels and vehicle velocity in a braking manoeuvre**

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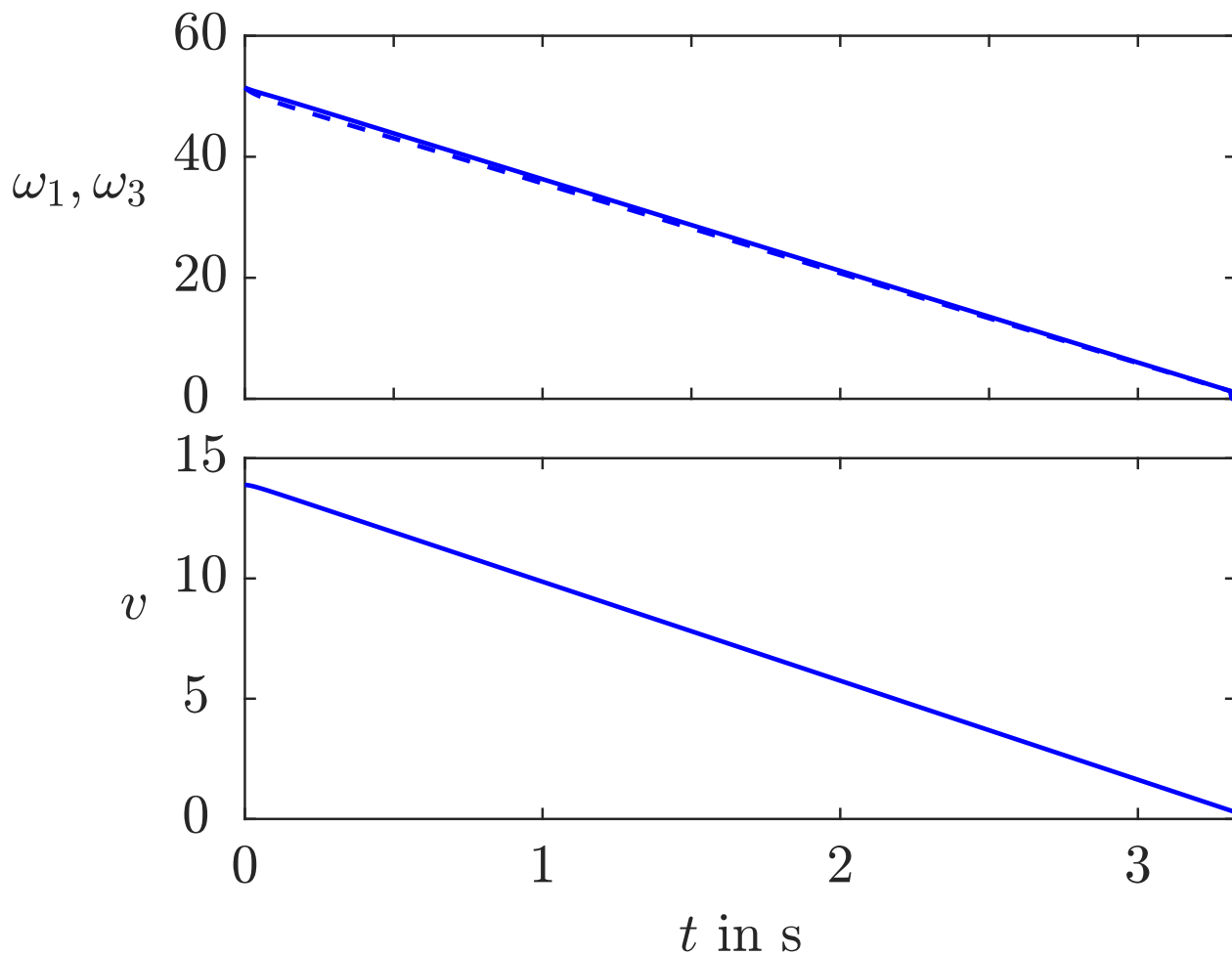
**Fig. 8. Slip in the braking manoeuvre of Fig. 7**

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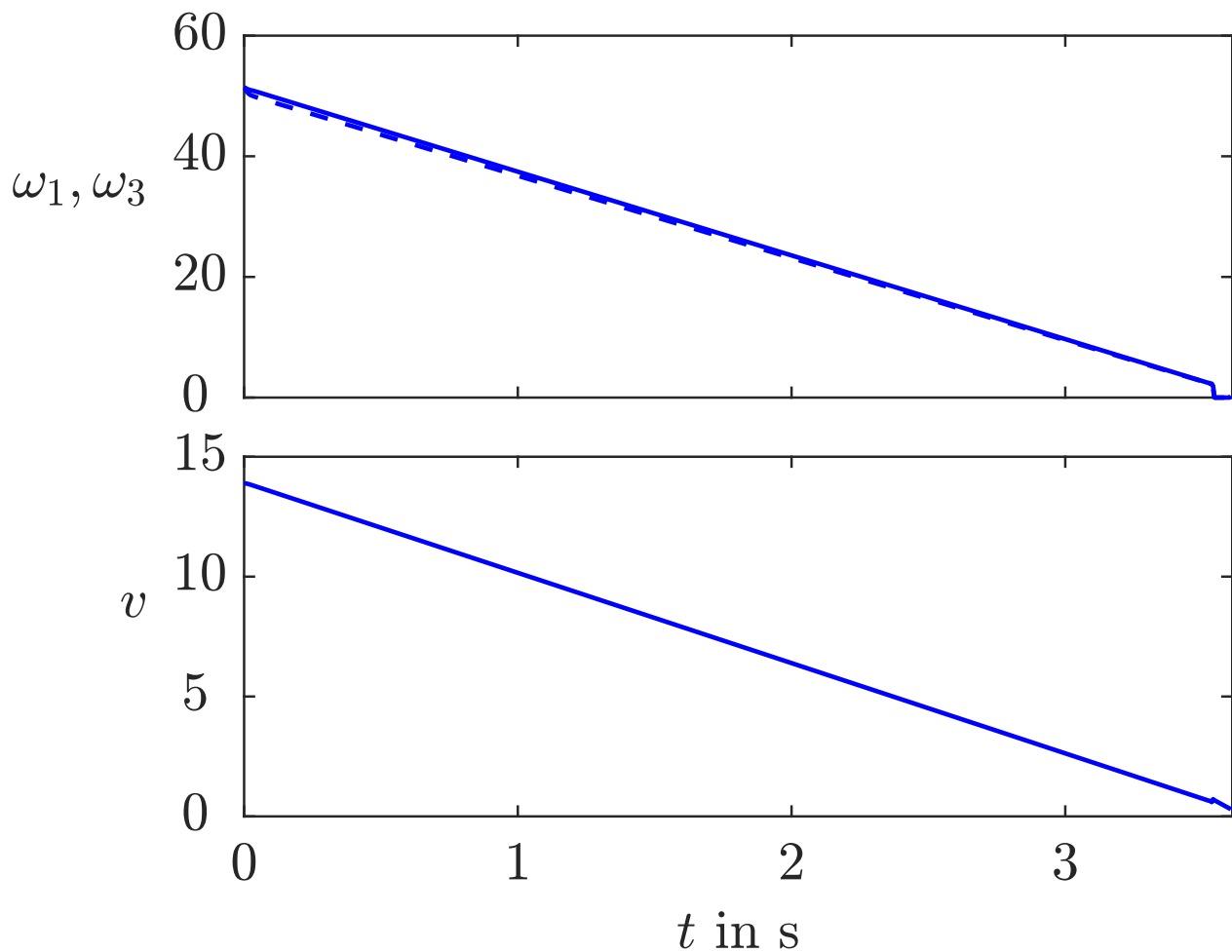
**Fig. 9: Braking system with decentralised controller**

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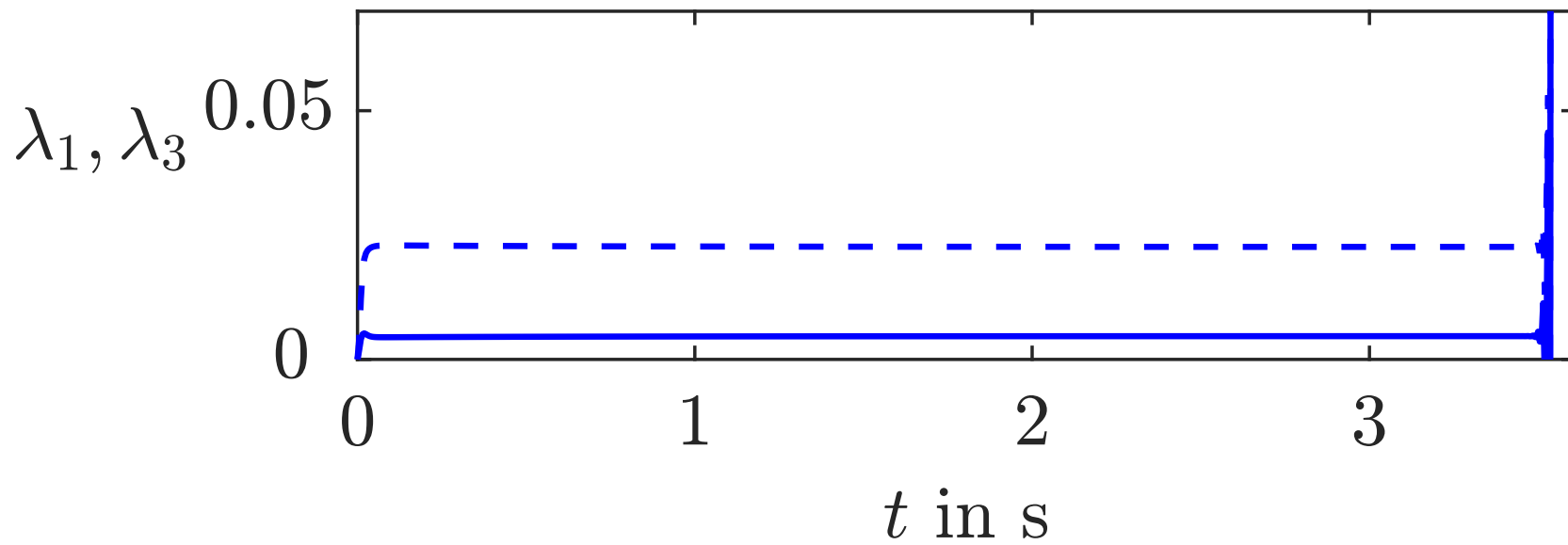
**Fig. 10: Angular velocity and vehicle velocity in a braking manoeuvre with decentralised controller**

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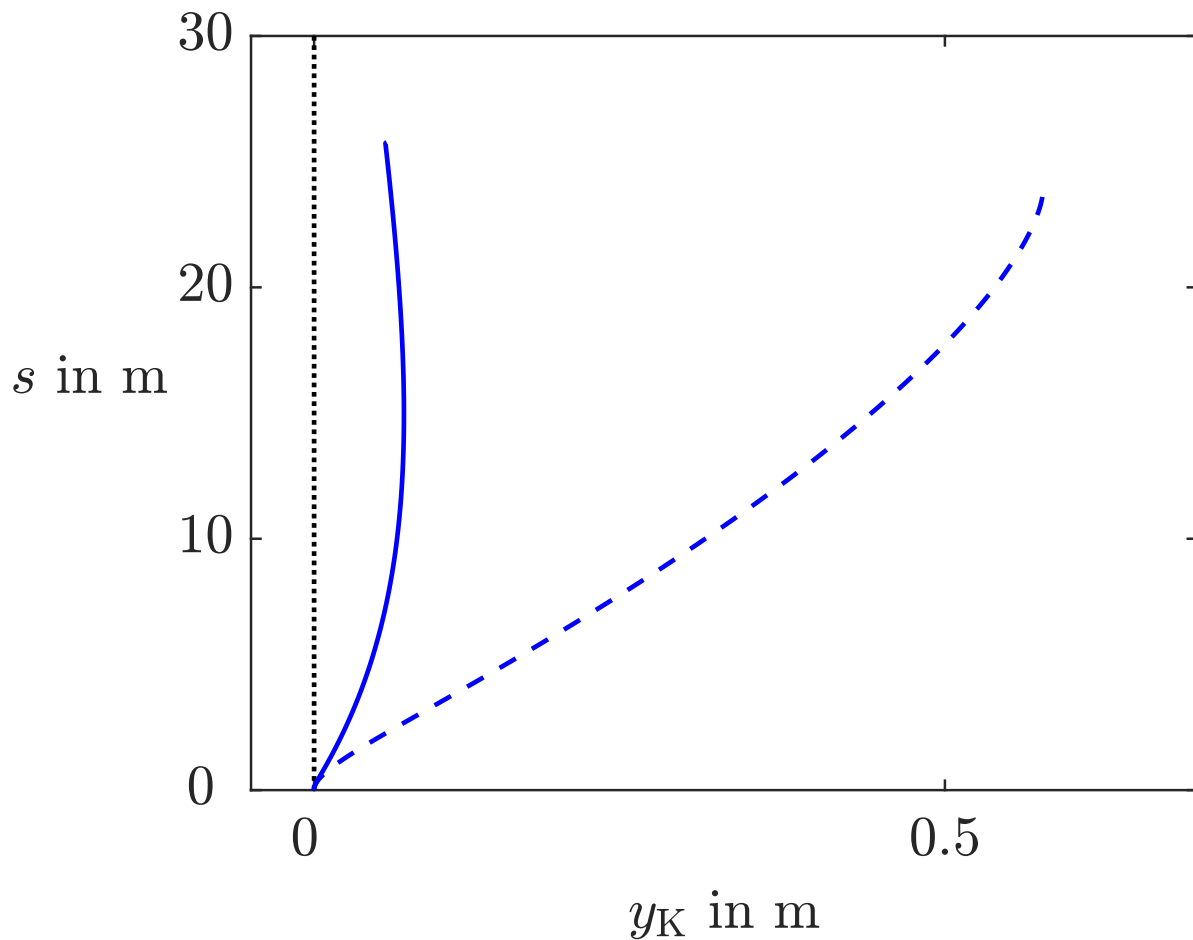
**Fig. 10: Angular velocity and vehicle velocity in a braking manoeuvre with networked controller**

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**Fig. 11. Slip of the wheels with different road conditions**

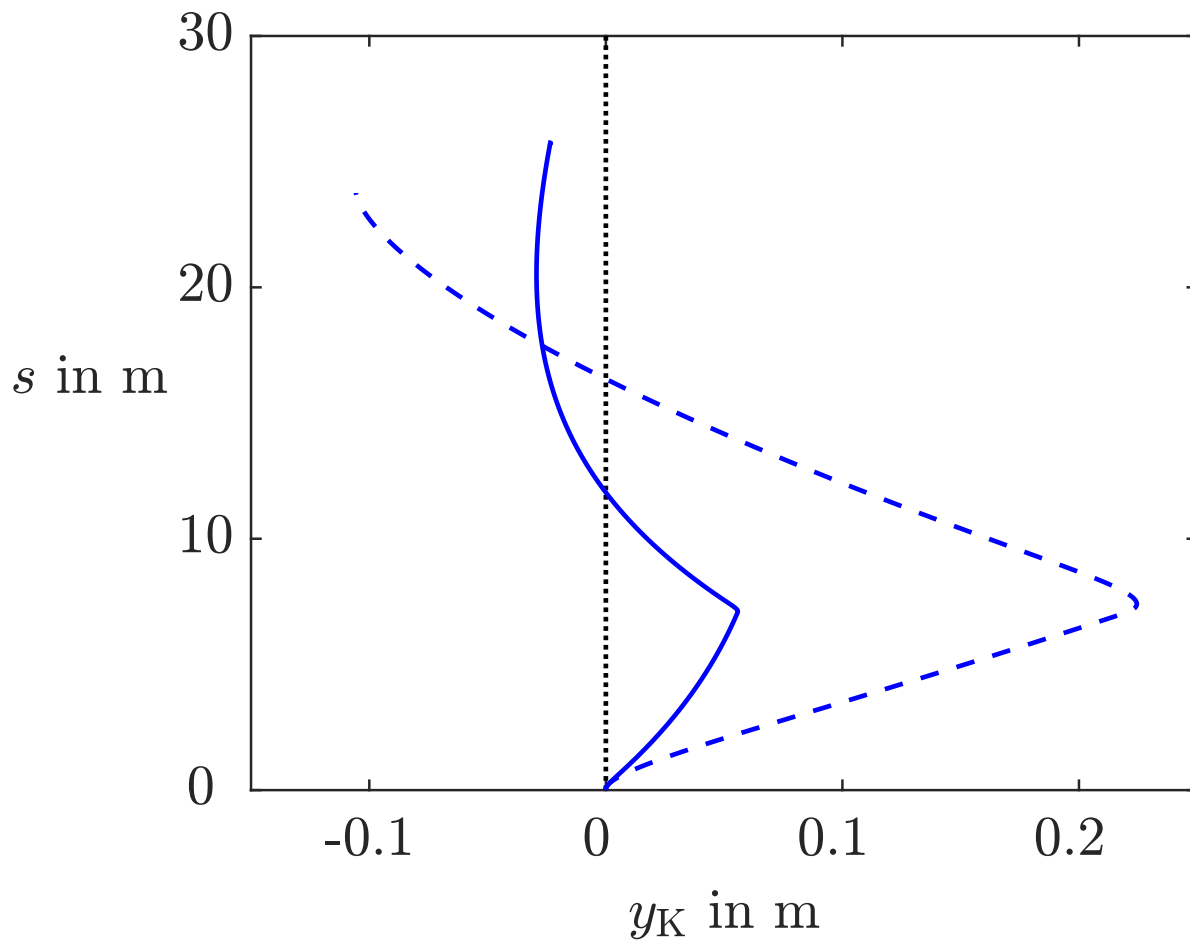
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**Fig. 12: Comparison of the vehicle movement for the decentralised controller (dashed line) and the networked controller (solid line) with constant road conditions**

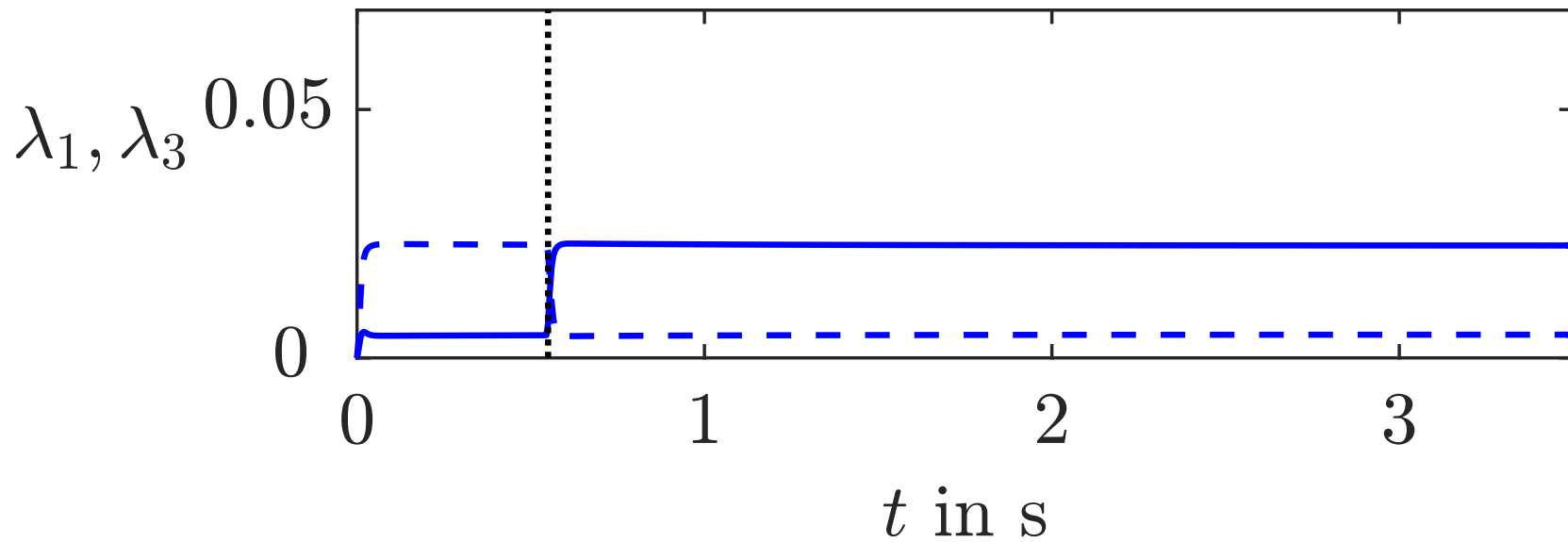
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**Fig. 12: Comparison of the vehicle movement for the decentralised controller (dashed line) and the networked controller (solid line) with changing road conditions**

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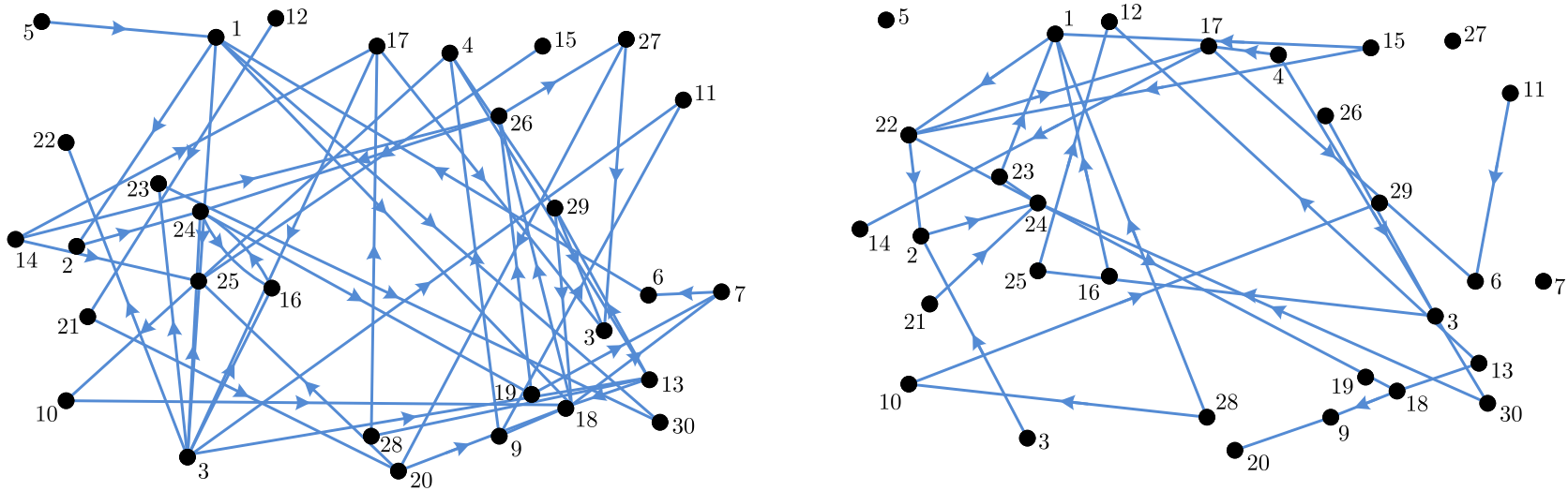
**Fig. 13. Slip of the wheels with changing road conditions**

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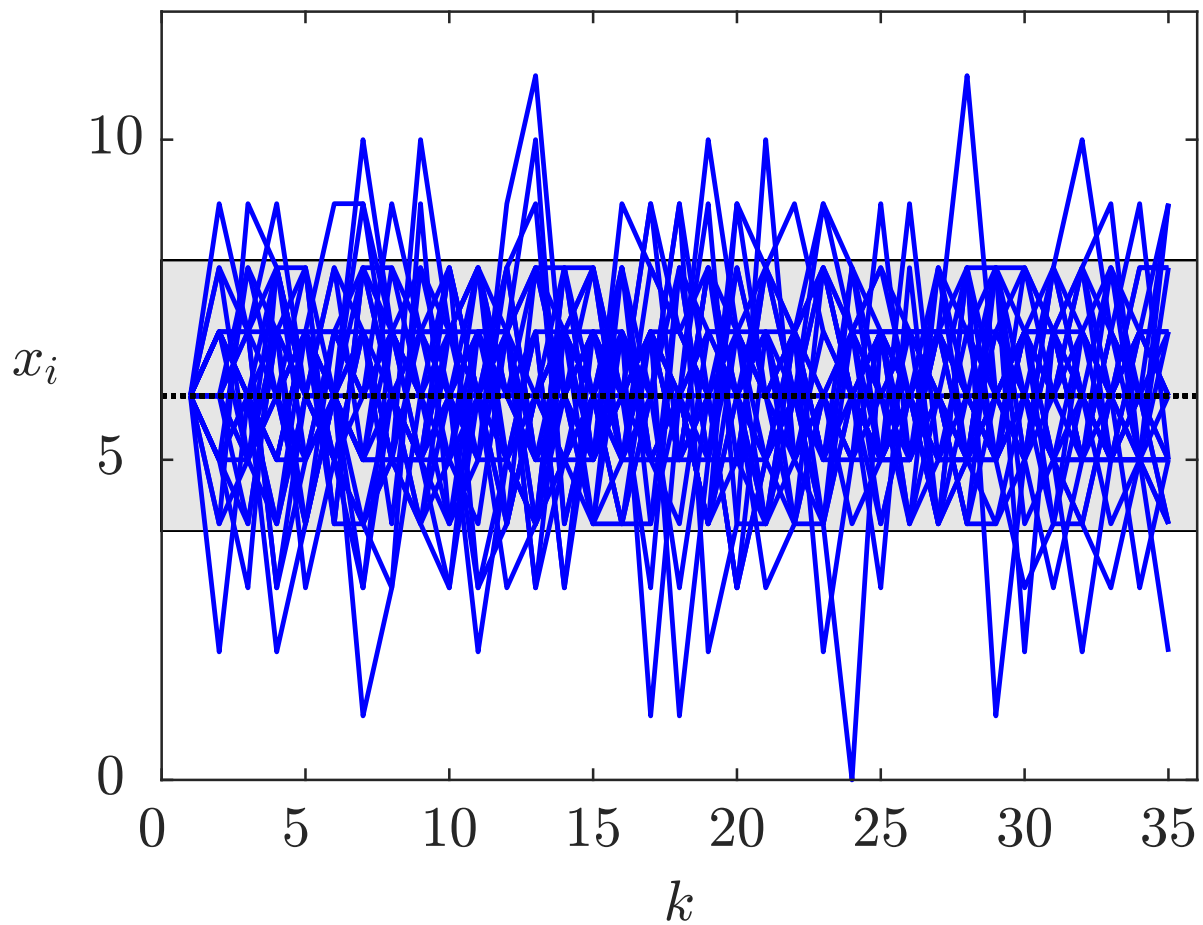
**Fig. 0:** Part of the plan of the bike-renting stations in Paris

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**Fig. 1.** Two realisations of the random graph for  $p = 0.04$

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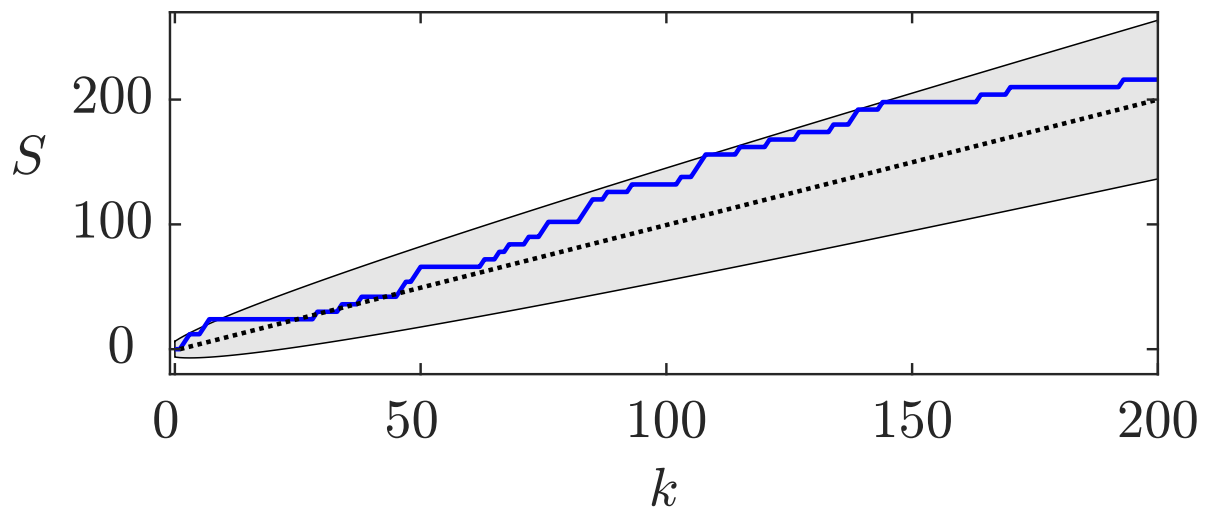
**Fig. 2: Simulation result: Number of bikes stored in the docking stations in the centre of Paris between 5 a.m. ( $k = 1$ ) and 10 p.m. ( $k = 35$ )**

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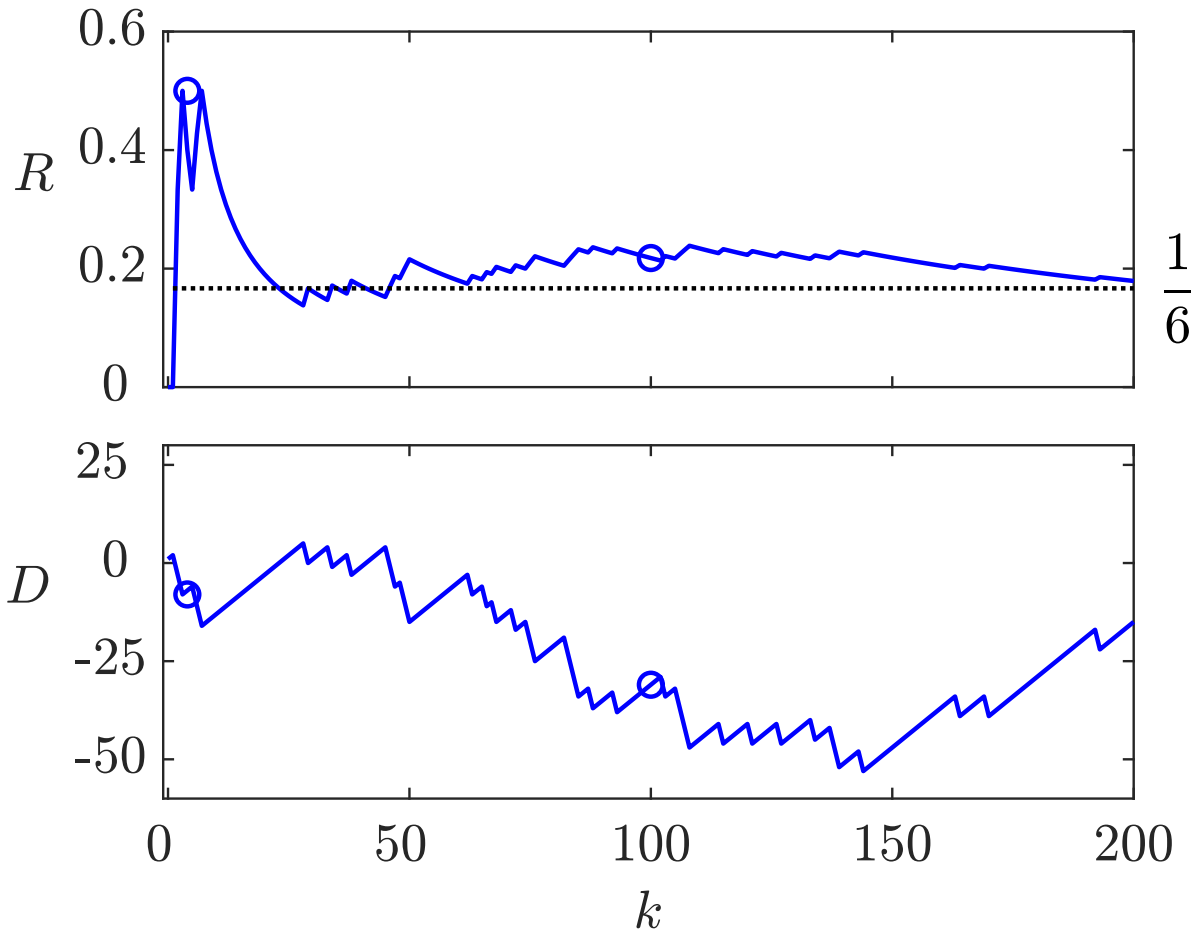
**Fig. 0: Dice throwing**

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**Fig. 1:** Tolerance band and a realisation of  $S(k)$

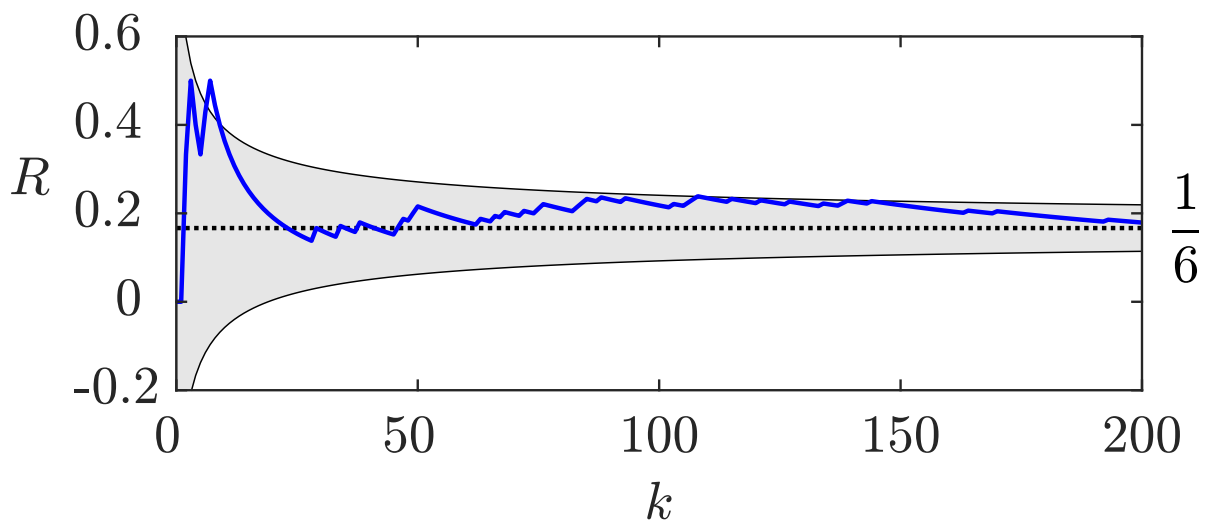
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**Fig. 2:** A realisation of the random sequence  $\{R(k), k \geq 0\}$

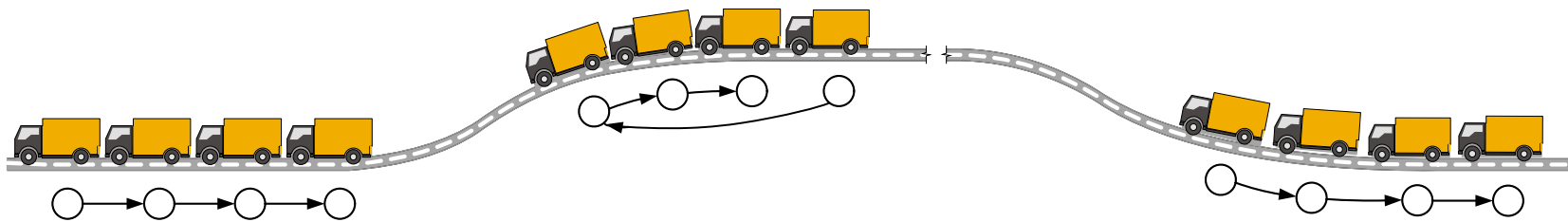
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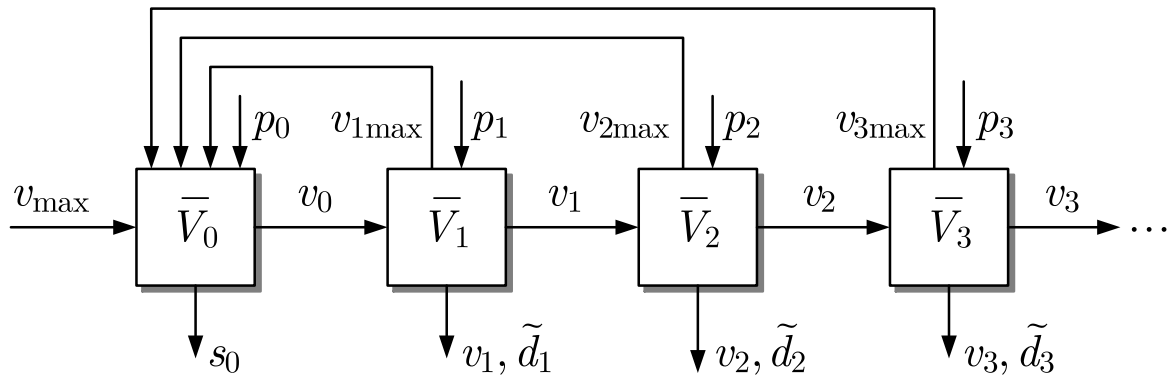
**Fig. 3: Tolerance band around the expected value**

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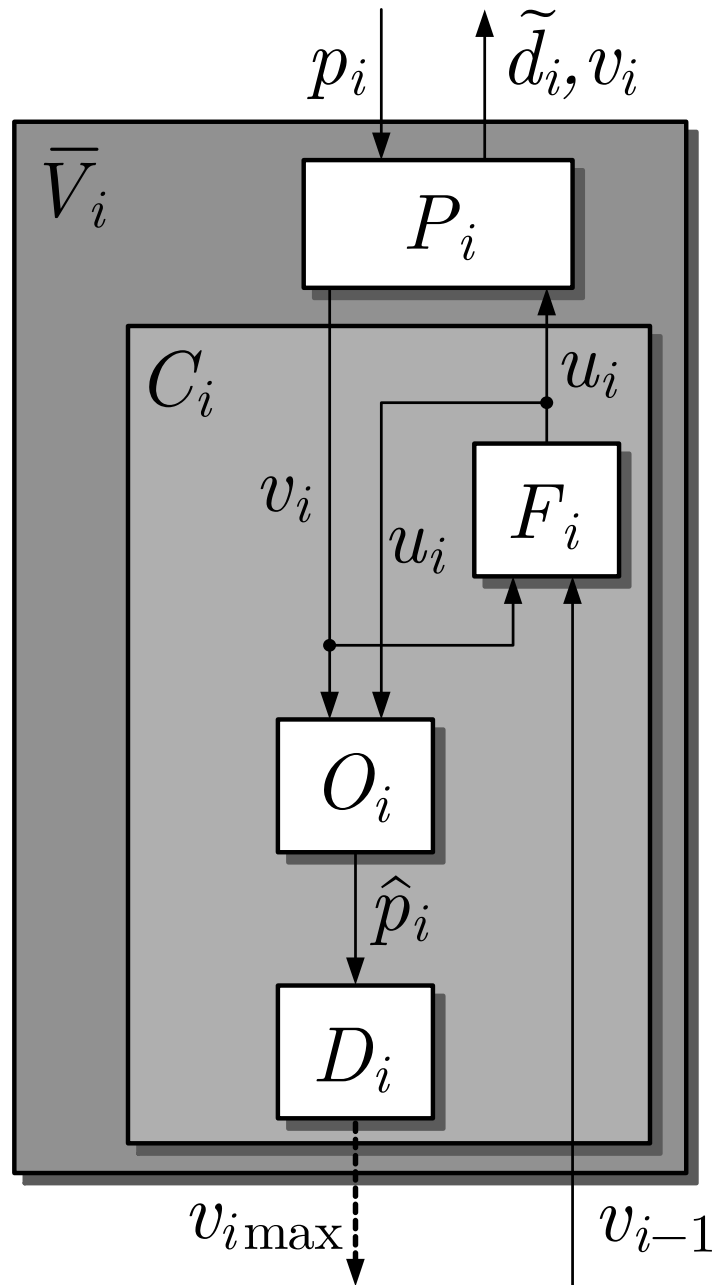
**Fig. 0. Truck platoon in a hilly terrain**

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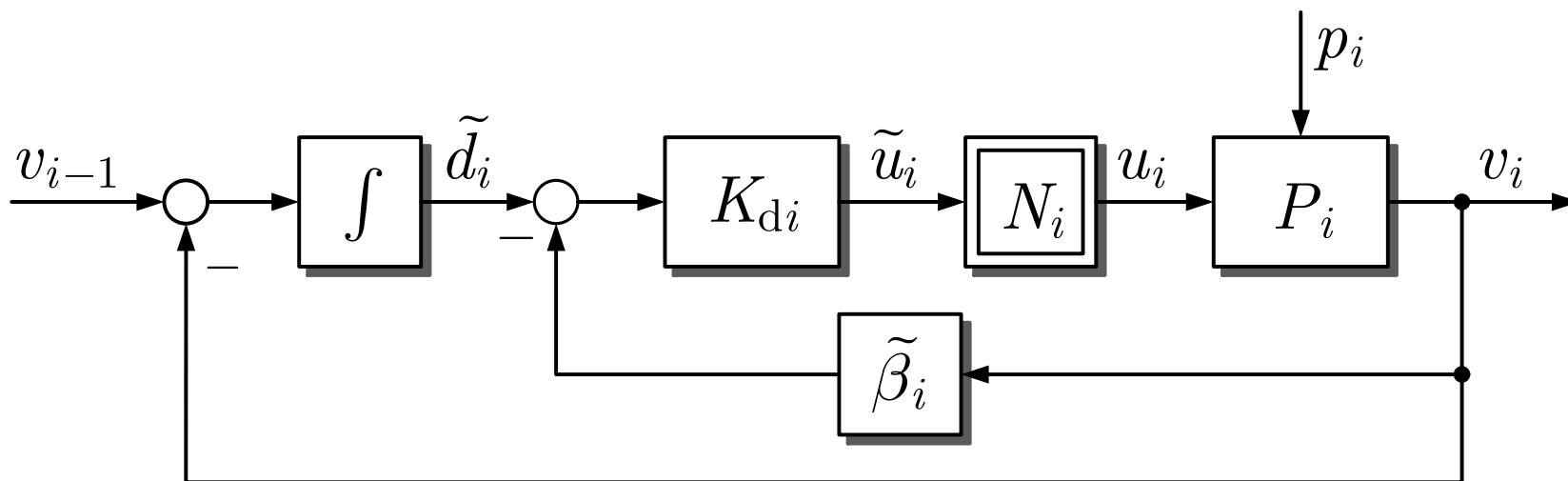
**Fig. 1: Block diagram of the truck platoon**

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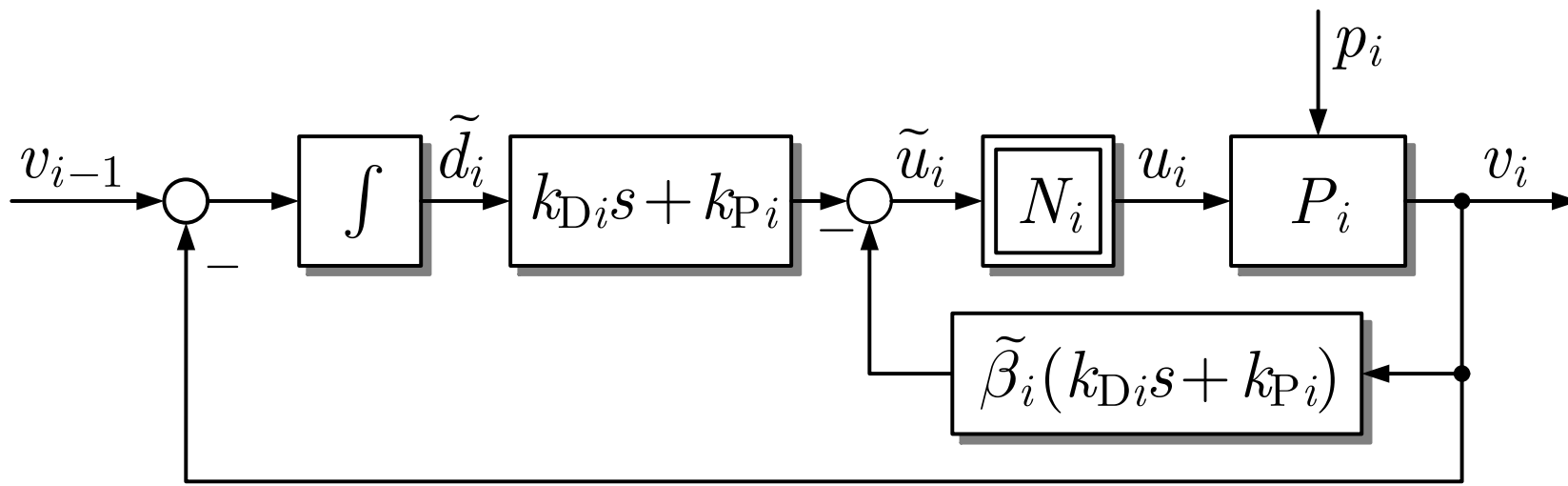
**Fig. 2. Structure of the truck controller**

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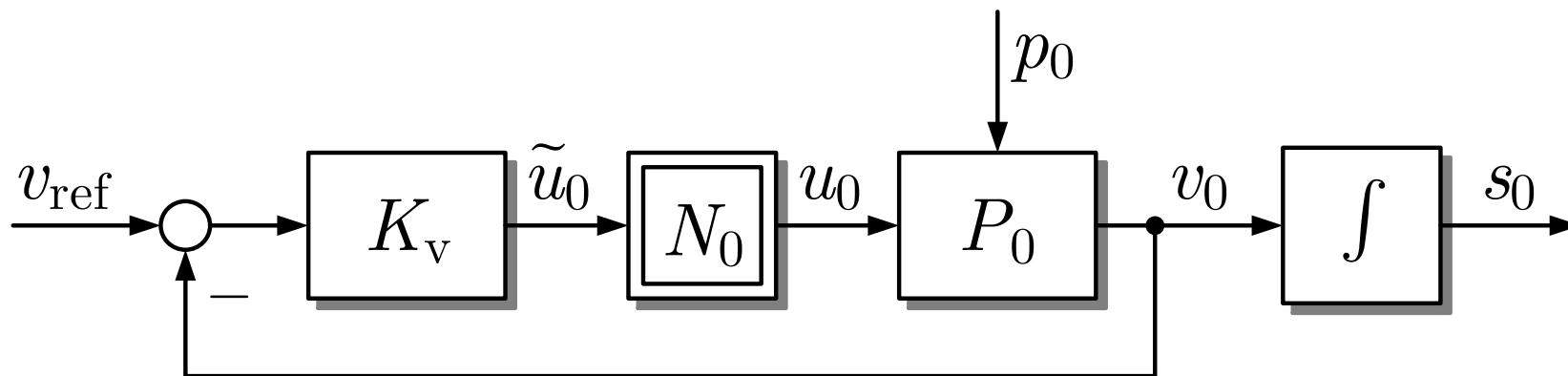
**Fig. 3. Truck with distance controller**

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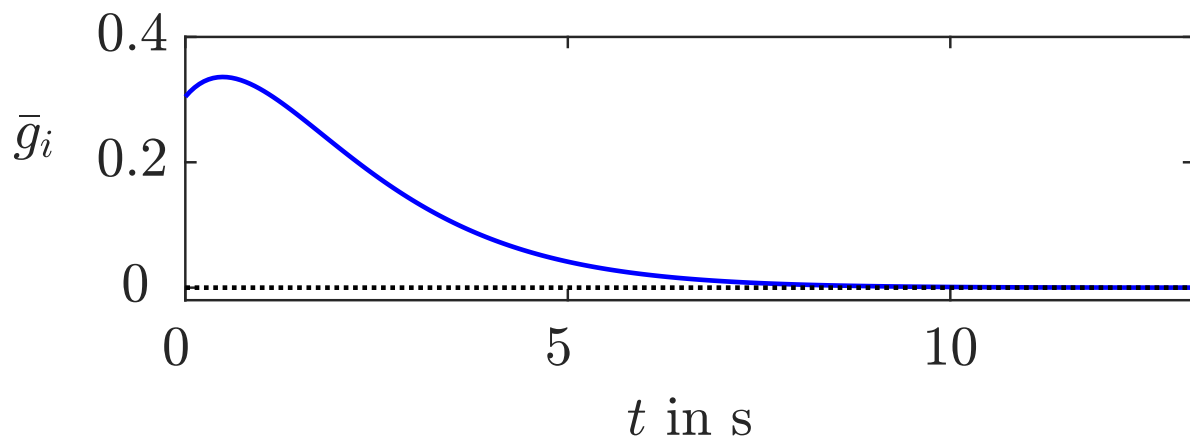
**Fig. 4. Transformed distance control loop**

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**Fig. 5.** First truck  $\bar{V}_0$  with velocity controller

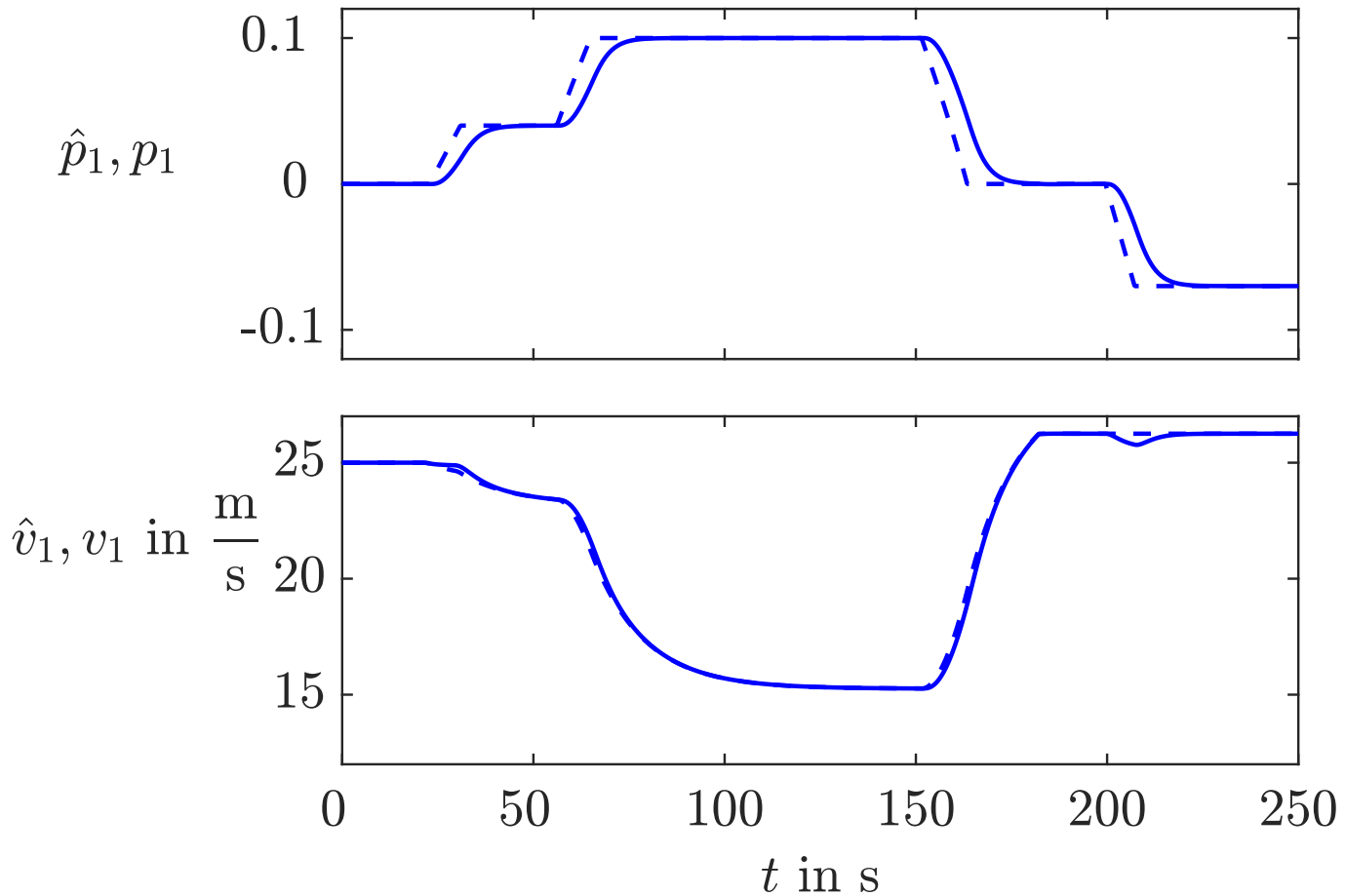
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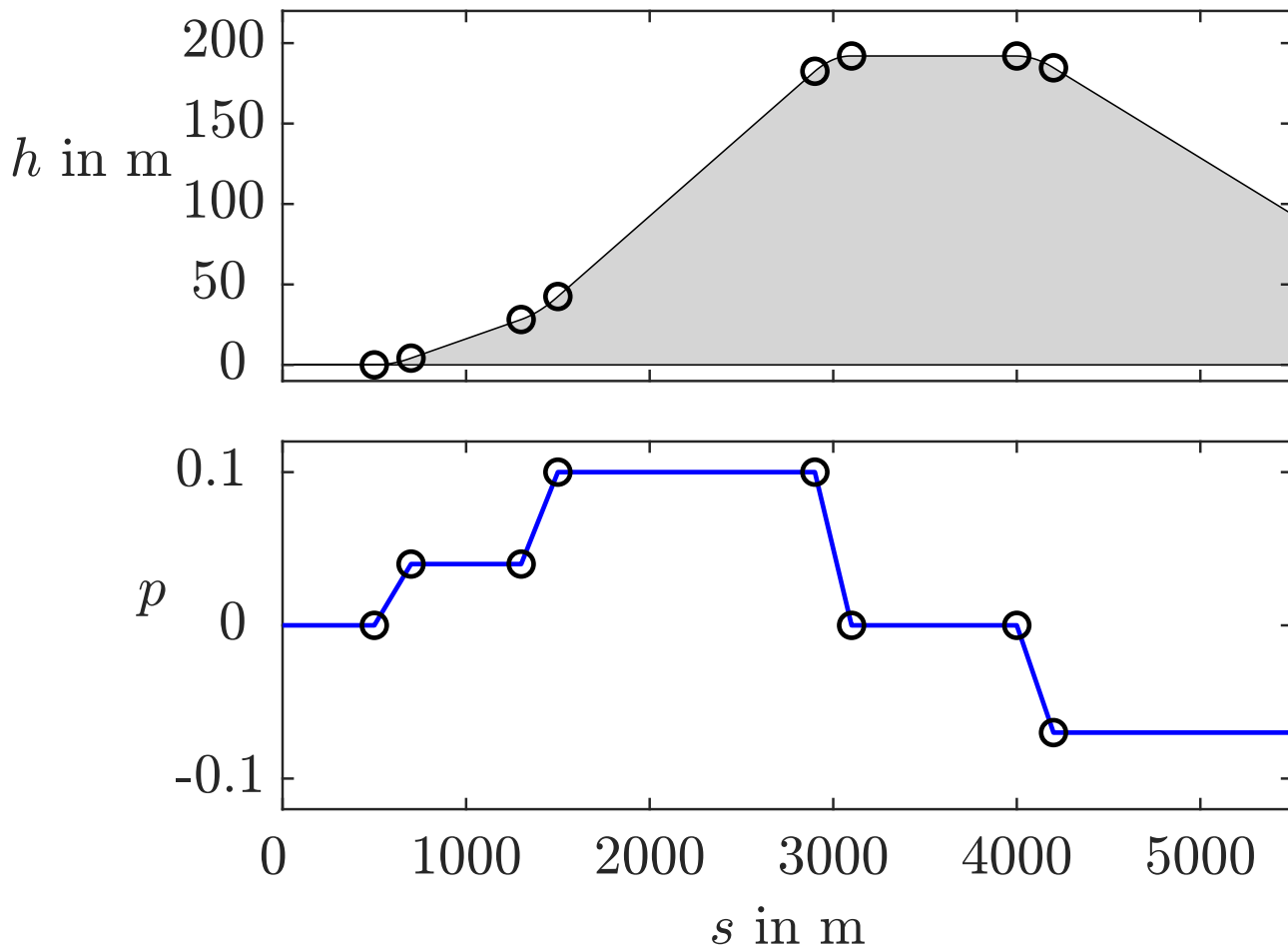
**Fig. 6: Nonnegative impulse response of the linear trucks**

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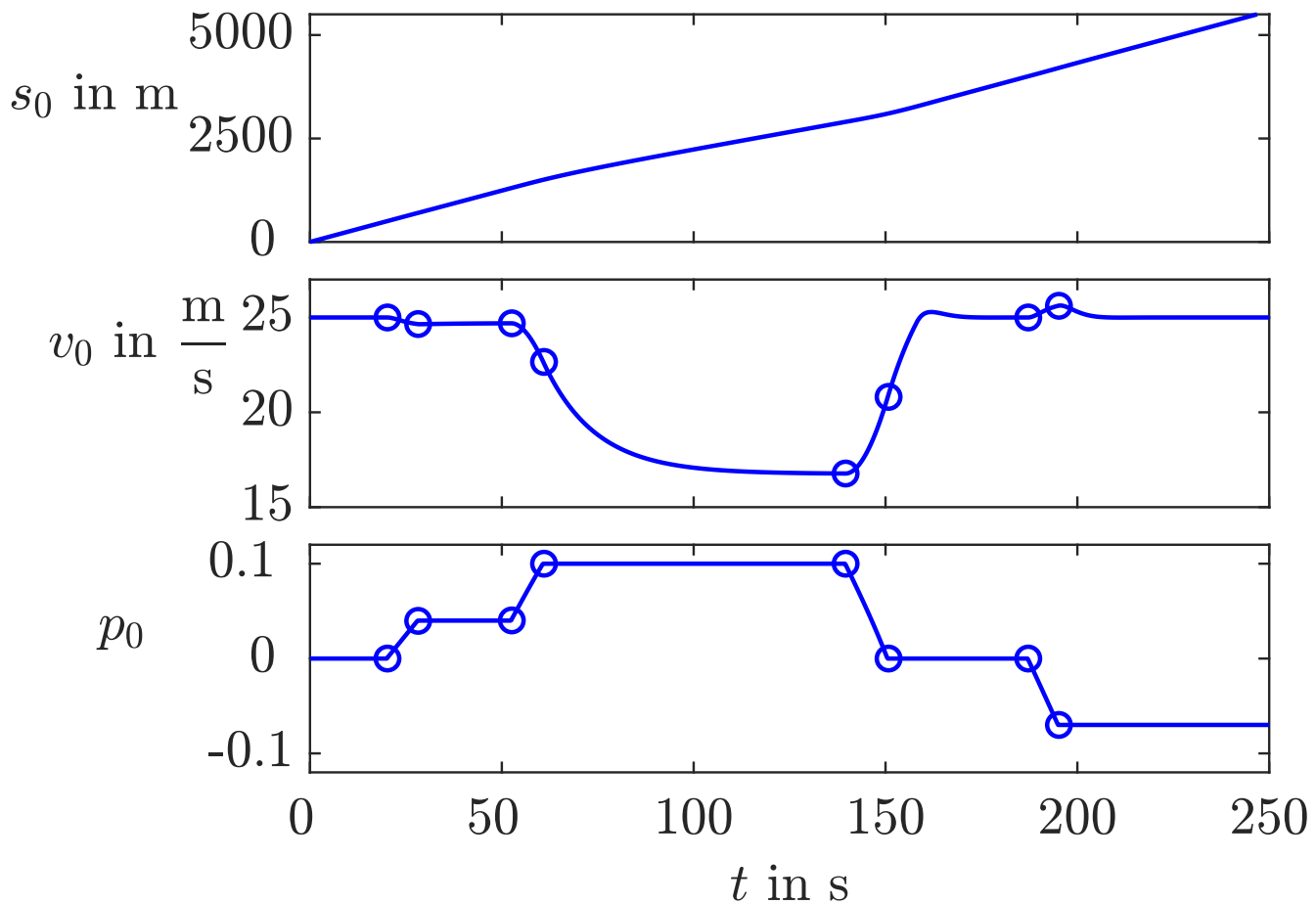




**Fig. 7: True (- - -) and estimated (—) disturbance and velocity of the first truck**

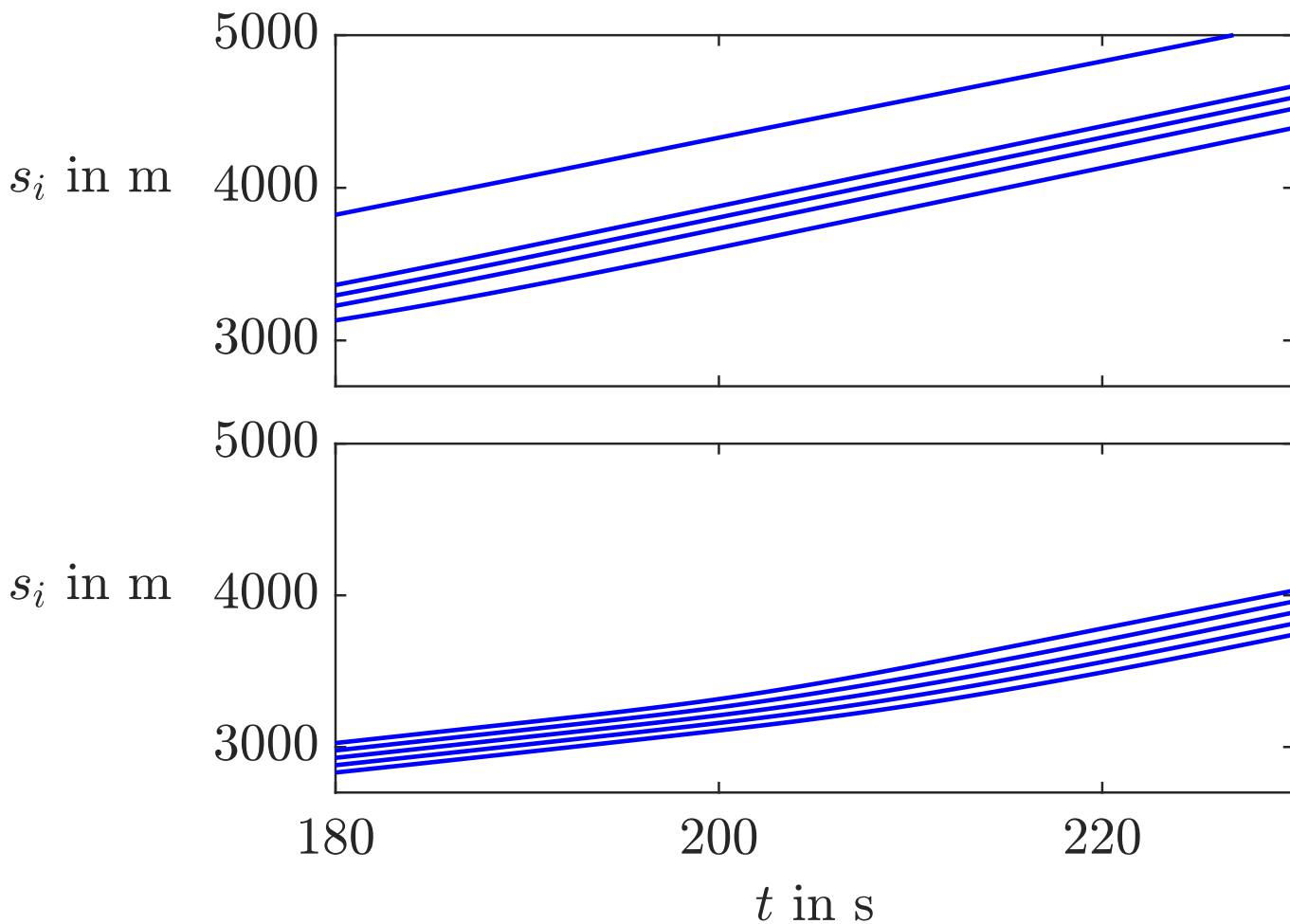


**Fig. 8: Road profile and disturbance**



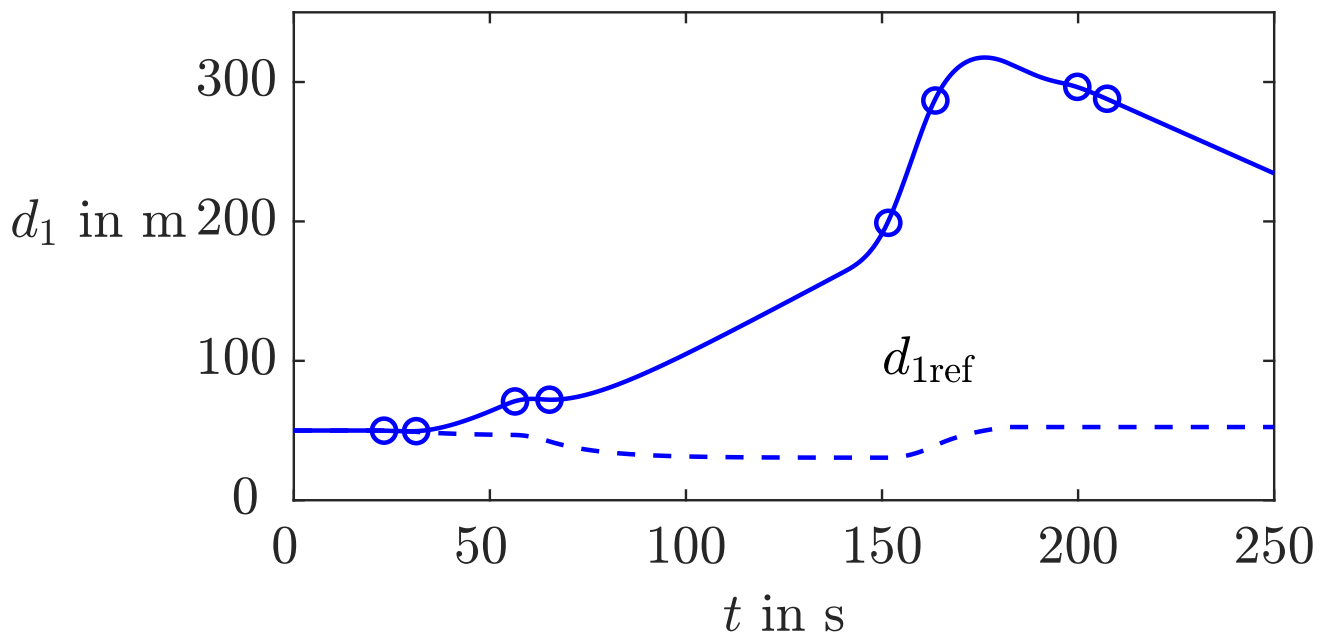
**Fig. 9:** Behaviour of the first truck for constant reference velocity  $v_{\text{ref}}(t) = v_{\text{max}}$

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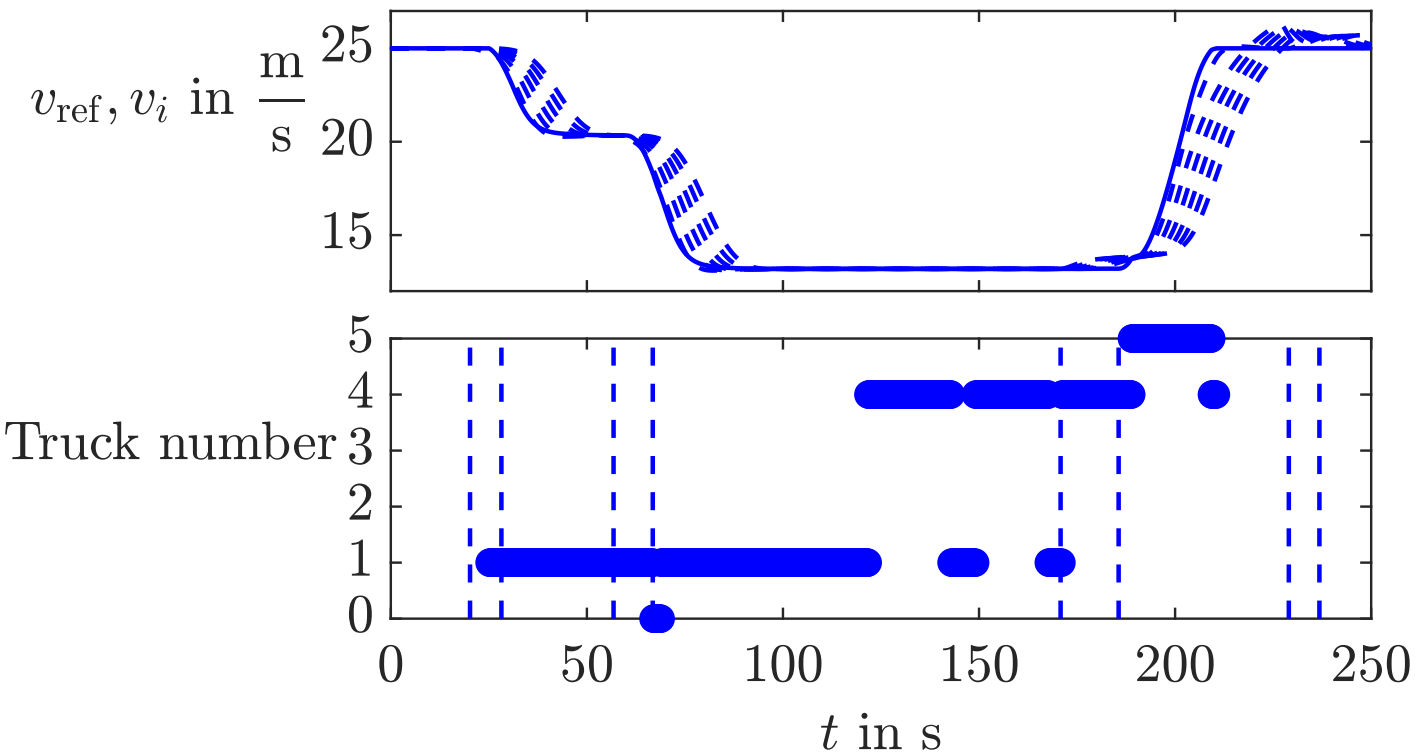


**Fig. 10: Platoon behaviour with ACC (top) and with self-organised ACC (bottom)**

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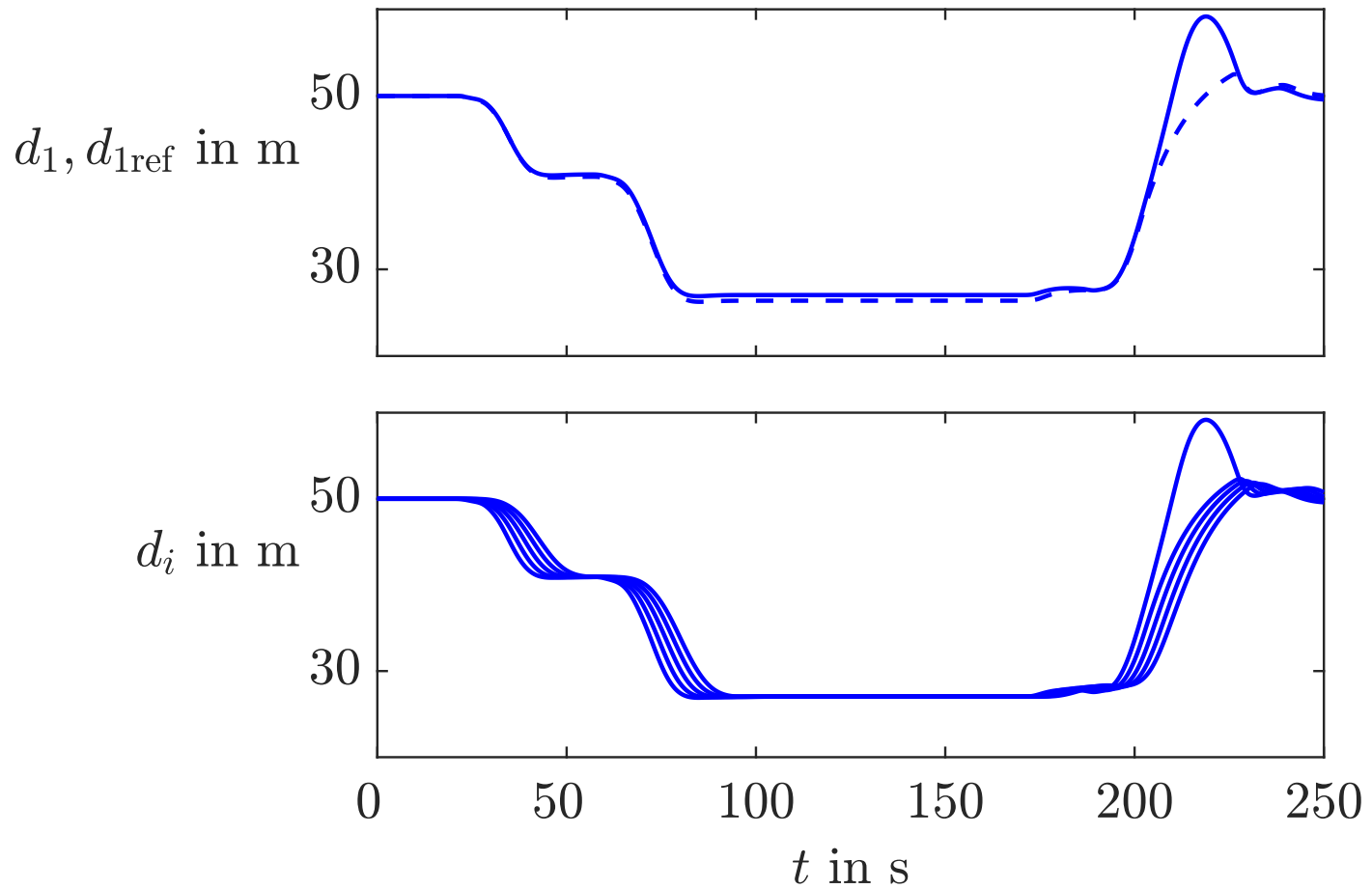


**Fig. 11: Distance between the first two trucks with ACC**



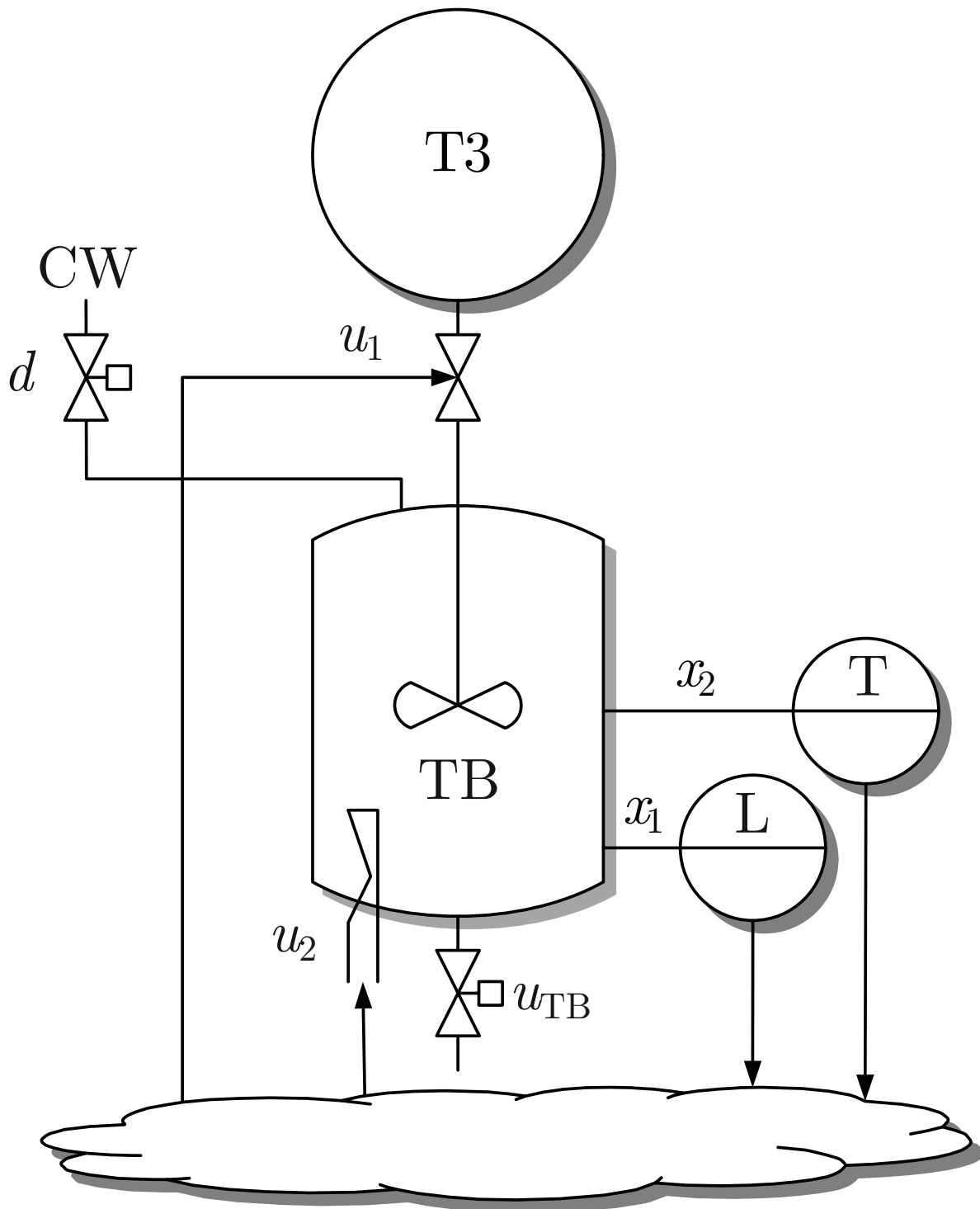
**Fig. 12: Behaviour of the truck platoon with self-organised ACC**

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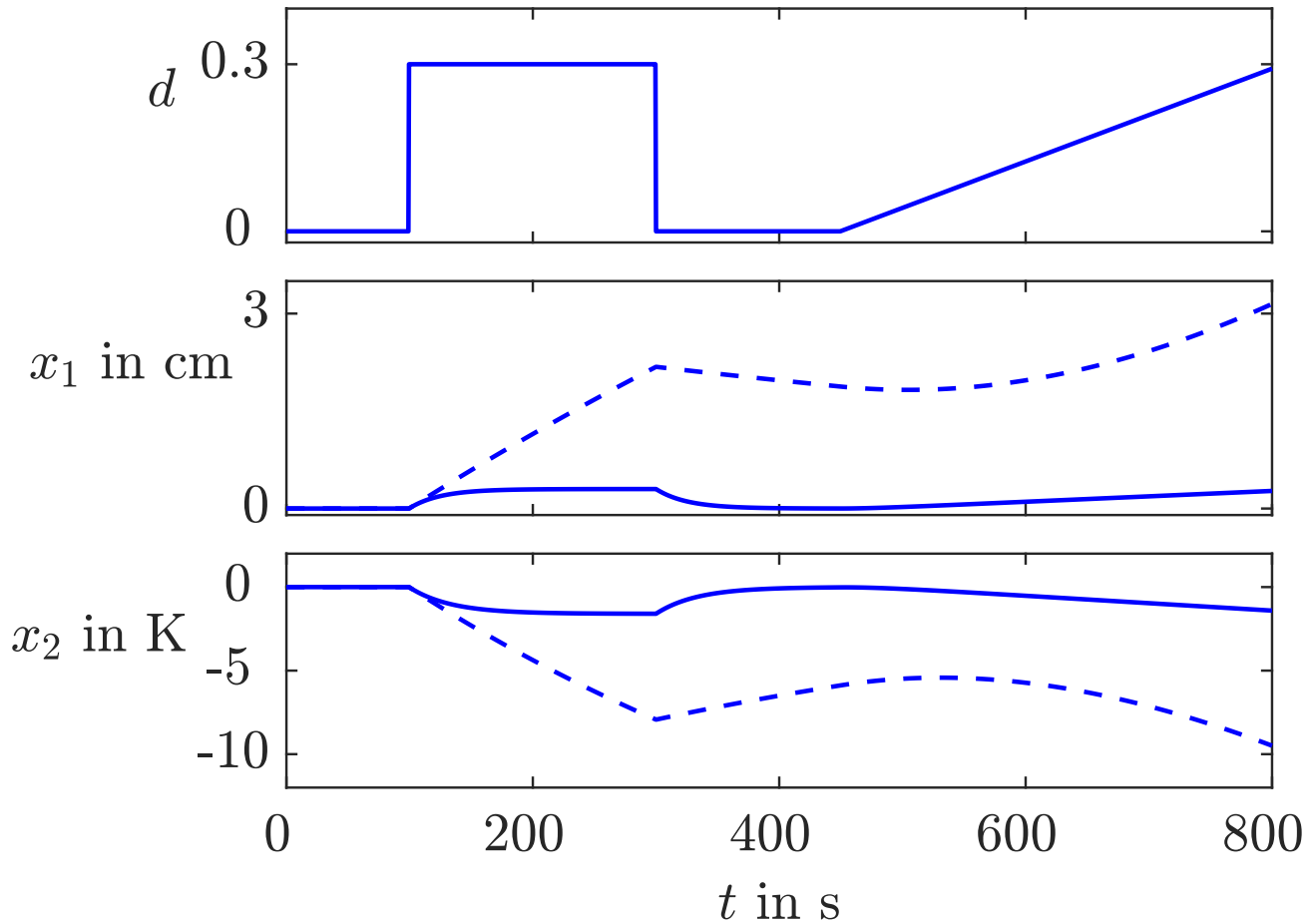
**Fig. 13: Vehicle distances in the platoon with self-organised ACC**

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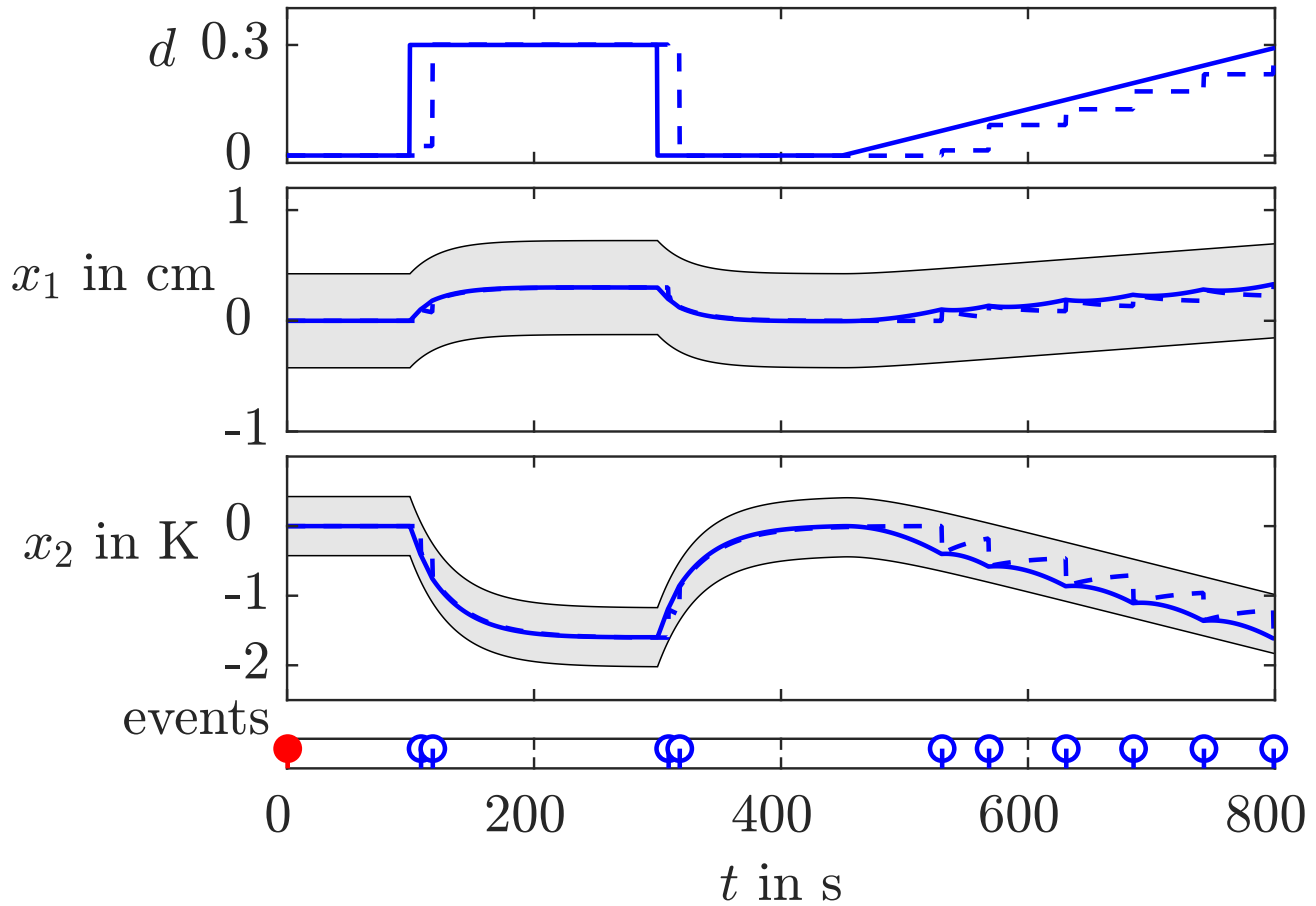
**Fig. 0: A thermo-fluid process**





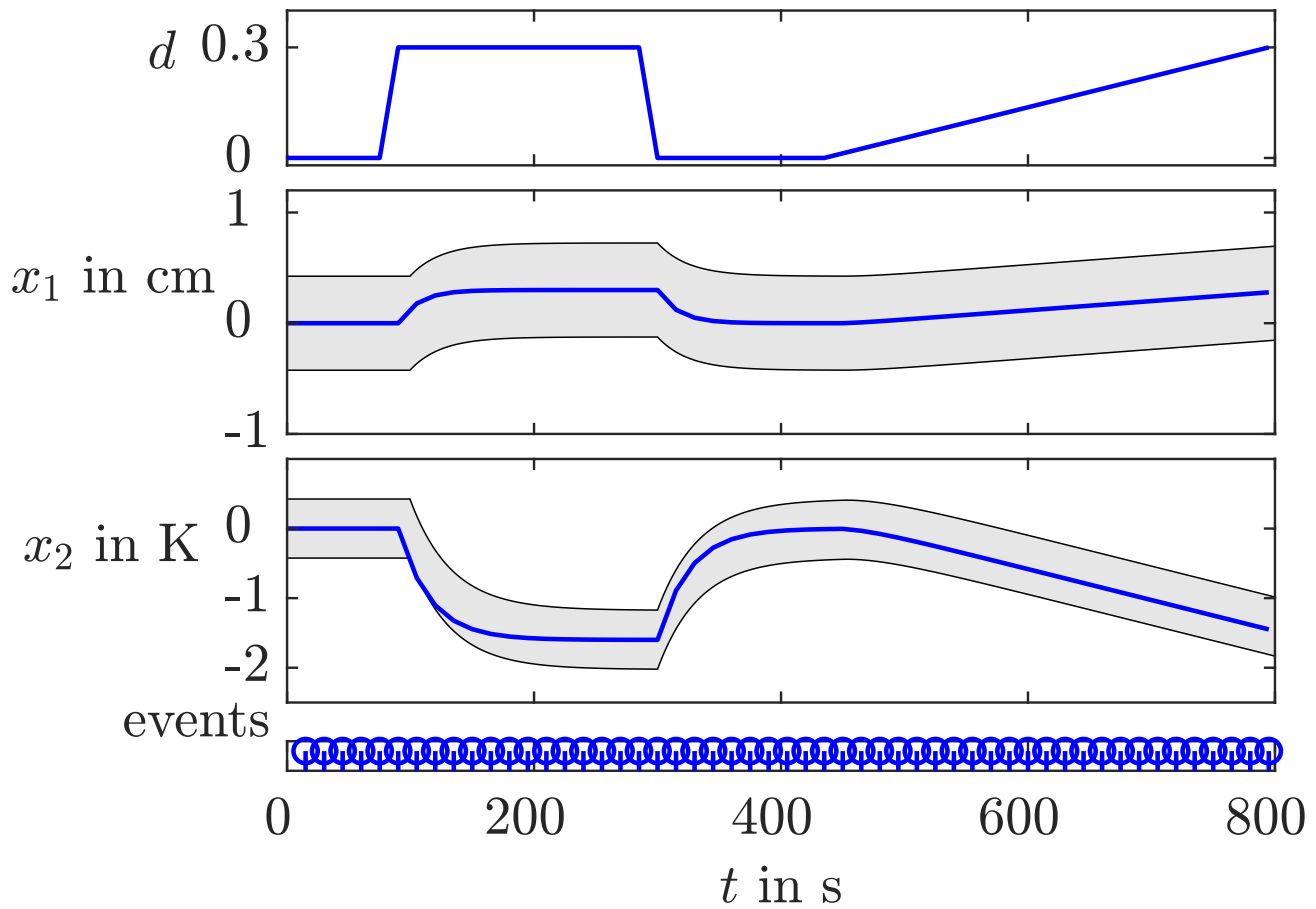
**Fig. 1: Disturbance behaviour of the plant (---) and of the continuous closed-loop system (—)**

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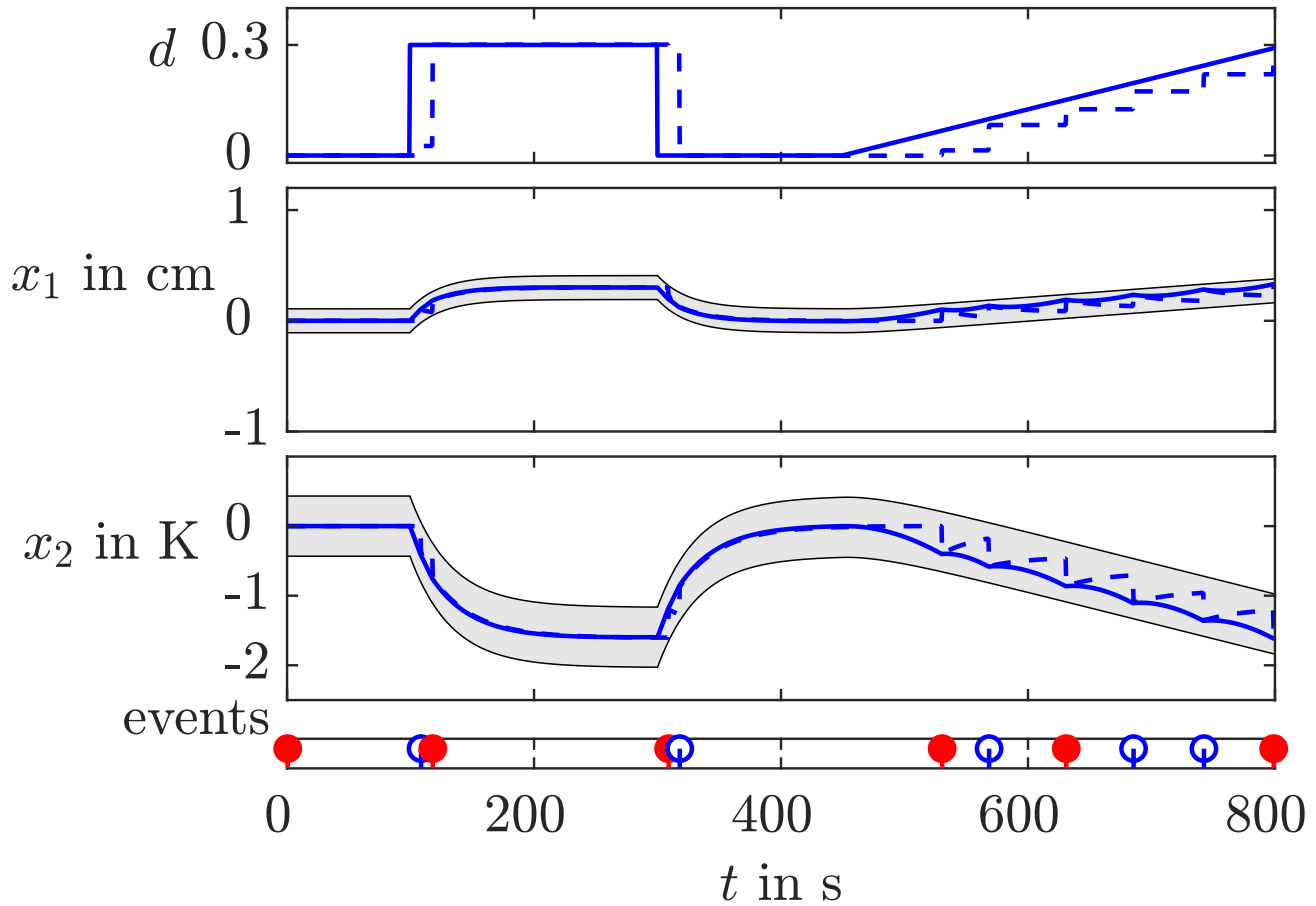
**Fig. 2: Behaviour of the event-triggered control loop**

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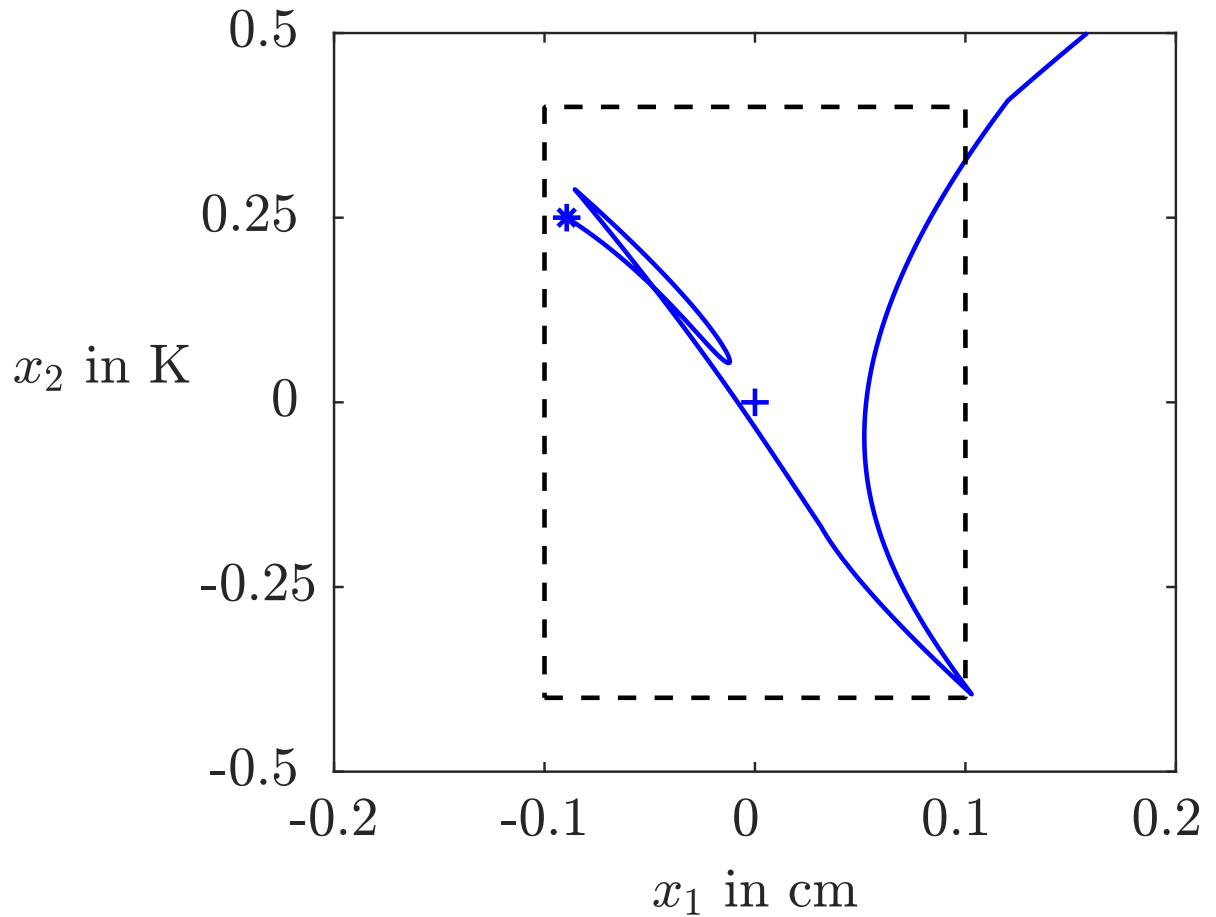
**Fig. 3: Sampled-data control loop**

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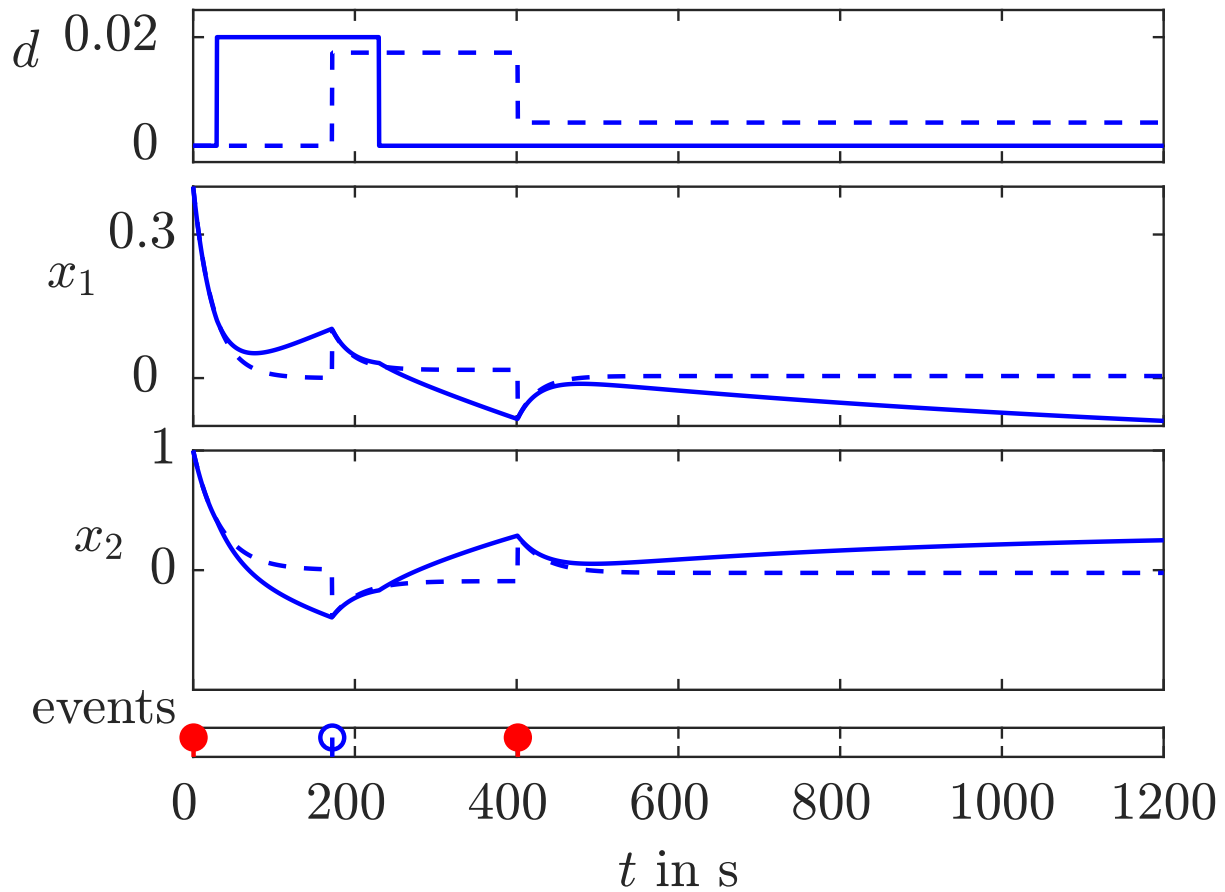
**Fig. 4: Behaviour of the event-triggered control loop with scaled norms**

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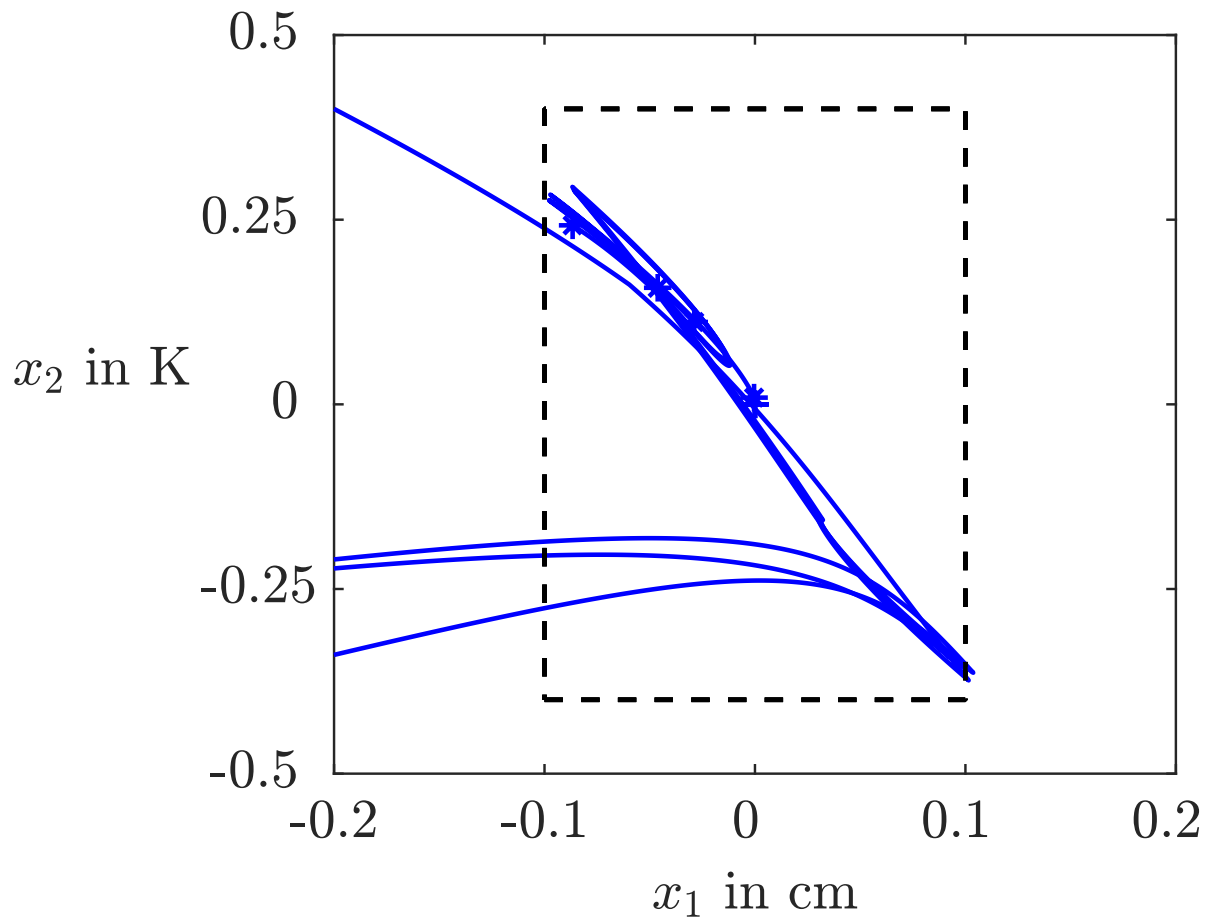
**Fig. 5: Long-time behaviour of the event-triggered control loop**

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**Fig. 5: Long-time behaviour of the event-triggered control loop**

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**Fig. 6: Practical stability of the thermo-fluid process**

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